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An Independent Component Analysis filtering approach for estimating continental hydrology in the GRACE gravity data

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Abstract:

An approach based on Independent Component Analysis (ICA) has been applied on a combination of monthly GRACE satellite solutions computed from official providers (CSR, JPL and GFZ), to separate useful geophysical signals from important striping undulations. We pre-filtered the raw GRACE Level-2 solutions using Gaussian filters of 300, 400, 500-km of radius to verify the non-gaussianity condition which is necessary to apply the ICA. This linear inverse approach ensures to separate components of the observed gravity field which are statistically independent. The most energetic component found by ICA corresponds mainly to the contribution of continental water mass change. Series of ICA-estimated global maps of continental water storage have been produced over 08/2002-07/2009. Our ICA estimates were compared with the solutions obtained using other post-processings of GRACE Level-2 data, such as destriping and Gaussian filtering, at global and basin scales. Besides, they have been validated with in situ measurements in the Murray Darling Basin. Our computed ICA grids are consistent with the different approaches. Moreover, the ICA-derived time-series of water masses showed less north-south spurious gravity signals and improved filtering of unrealistic hydrological features at the basin-scale compared with solutions obtained using other filtering methods.
1. Introduction

Continental water storage is a key component of global hydrological cycles and plays a major role in the Earth’s climate system via controls over water, energy and biogeochemical fluxes. In spite of its importance, the total continental water storage is not well-known at regional and global scales because of the lack of in situ observations and systematic monitoring of the groundwaters (Alsdorf and Lettenmaier, 2003).

The Gravity Recovery and Climate Experiment (GRACE) mission provides a global mapping of the time-variations of the gravity field at an unprecedented resolution of ~400 km and a precision of ~1 cm in terms of geoid height. Tiny variations of gravity are mainly due to redistribution of mass inside the fluid envelops of the Earth (i.e., atmosphere, oceans and continental water storage) from monthly to decade timescales (Tapley et al., 2004).

Pre-processing of GRACE data is made by several providers (University of Texas, Centre for Space Research - CSR, Jet Propulsion Laboratory - JPL, GeoForschungsZentrum - GFZ and Groupe de Recherche en Géodésie Spatiale - GRGS) which produce residual GRACE spherical harmonic solutions that mainly represent continental hydrology as they are corrected from known mass transfers using ad hoc oceanic models (i.e., Toulouse Unstructured Grid Ocean model 2D - T-UGOm 2D) and atmospheric reanalyses from National Centers for Environmental Prediction (NCEP) and European Centre for Medium Weather Forecasting (ECMWF). Unfortunately these solutions suffer from the presence of important north-south striping due to orbit resonance in spherical harmonics determination and aliasing of short-time phenomena which are geophysically unrealistic.

Since its launch in March 2002, the GRACE terrestrial water storage anomalies have been increasingly used for large-scale hydrological applications (see Ramillien et al., 2008; Schmitt et al., 2008 for reviews). They demonstrated a great potential to monitor extreme hydrological events (Andersen et al., 2005; Seitz et al., 2008; Chen et al., 2009), to estimate water storage variations in the soil (Frappart et al., 2008), the aquifers (Rodell et al., 2007; Strassberg et al., 2007; Leblanc et al., 2009) and the snowpack (Frappart et al., 2006; in press), and hydrological fluxes, such as basin-scale evapotranspiration (Rodell et al., 2004a; Ramillien et al., 2006a) and discharge (Syed et al., 2009).

Because of this problem of striping that limits geophysical interpretation, different post-processing approaches for filtering GRACE geoid solutions have been proposed to extract useful geophysical signals (see Ramillien et al., 2008; Schmidt et al., 2008 for reviews). These include the classical isotropic Gaussian filter (Jekeli, 1981), various optimal filtering
decorrelation of GRACE errors (Han et al., 2005; Seo and Wilson, 2005; Swenson and Wahr, 2006; Sasgen et al., 2006; Kusche, 2007; Klees et al., 2008), as well as statistical constraints on the time evolution of GRACE coefficients (Davis et al., 2008) or from global hydrology models (Ramillien et al., 2005). However, these filtering techniques remain imperfect as they require input non-objective \textit{a priori} information which are most of the time simply tuned by hand (e.g. choosing the cutting wavelength while using the Gaussian filtering) or based on other rules-of-thumb.

We propose another post-processing approach of the Level-2 GRACE solutions by considering completely objective constraints, so that the gravity component of the observed signals is forced to be uncorrelated numerically using an Independent Component Analysis (ICA) technique. This approach does not require \textit{a priori} information except the assumption of statistical independence of the elementary signals that compose the observations, \textit{i.e.}, geophysical and spurious noise. The efficiency of ICA to separate gravity signals and noise from combined GRACE solutions has previously been demonstrated on one month of Level-2 solutions (Frappart et al., 2010). In this paper, we use this new statistical linear method to derive complete time series of continental water mass change.

The first part of this article presents the datasets used in this study: the monthly GRACE solutions to be inverted by ICA and to be used for comparisons, and the \textit{in situ} data used for validation of our estimates over the Murray Darling drainage basin (~ 1 million of km²). This region has been selected for validation because of available dense hydrological observations.

The second part outlines the three steps of the ICA methodology. Then the third and fourth parts present results and comparisons with other post-processed GRACE solutions at global and regional scales, and \textit{in situ} measurements for the Murray Darling Basin respectively.

Error balance of the ICA-based solutions is also made by considering the effect of spectrum truncation, leakage and formal uncertainties.

2. Datasets

2.1. The GRACE data

The GRACE mission, sponsored by National Aeronautics and Space Administration (NASA) and Deutsches Zentrum für Luft- und Raumfahrt (DLR), has been collecting data since mid-2002. Monthly gravity models are determined from the analysis of GRACE orbit perturbations in terms of Stokes spherical harmonic coefficients, \textit{i.e.}, geopotential or geoid heights. The geoid is an equipotential surface of the gravity field that coincide with mean sea
level. For the very first time, monthly global maps of the gravity time-variations can be
derived from GRACE measurements, and hence, to estimate the distribution of the change of
mass in the Earth’s system.

2.1.1. The Level-2 raw solutions

The Level-2 raw data consist of monthly estimates of geo-potential coefficients adjusted for
each 30-day period from raw along-track GRACE measurements by different research groups
(i.e., CSR, GFZ and JPL). These coefficients are developed up to a degree 60 (or spatial
resolution of 333 km) and corrected for oceanic and atmospheric effects (Bettadpur, 2007) to
obtain residual global grids of ocean and land signals corrupted by a strong noise. These data
are available at: ftp://podaac.jpl.nasa.gov/grace/.

2.1.2. The destriped and smoothed solutions

The monthly raw solutions (RL04) from CSR, GFZ, and JPL were destriped and smoothed by
Chambers (2006) for hydrological purposes. These three datasets are available for several
averaging radii (0, 300 and 500 km on the continents and 300, 500 and 750 km on the oceans)

In this study, we used the Level-2 RL04 raw data from CSR, GFZ and JPL, that we filtered
with a Gaussian filter for radii of 300, 400 and 500 km, and the destriped and smoothed
solutions for the averaging radii of 300 and 500 km over land.

2.2. The hydrological data for the Murray Darling Basin

In the predominantly semiarid Murray Darling Basin, most of the surface water is regulated
using a network of reservoirs, lakes and weirs (Kirby et al., 2006) and the surface water stored
in these systems represent most of the total surface water (SW) present across the basin. A
daily time series of the total surface water storage in the network of reservoirs, lakes, weirs
and in-channel storage was obtained from the Murray-Darling Basin Commission and the
state governments from January 2000 to December 2008.

In the Murray Darling Basin, we derived monthly soil moisture (SM) storage values for the
basin from January 2000 to December 2008 from the NOAH land surface model (Ek et al.,
with the NOAH simulations being driven (parameterization and forcing) by the Global Land Data Assimilation System (Rodell et al., 2004b). The NOAH model simulates surface energy and water fluxes/budgets (including soil moisture) in response to near-surface atmospheric forcing and depending on surface conditions (e.g., vegetation state, soil texture and slope) (Ek et al., 2003). The NOAH model outputs of soil moisture estimates have a 1° spatial resolution and, using four soil layers, are representative of the top 2 m of the soil.

In situ estimates of annual changes in the total groundwater storage (GW) across the drainage basin were obtained from an analysis of groundwater levels observed in government monitoring bores from 2000 to 2008. Compared to earlier estimates by Leblanc et al. (2009), the groundwater estimates presented in this paper provide an update of the in situ water level and a refinement of the distribution of the aquifers storage capacity.

Assuming that (1) the shallow aquifers across the Murray-Darling drainage basin are hydraulically connected and that (2) at a large scale the fractured aquifers can be assimilated to a porous media, changes in groundwater storage across the area can be estimated from observations of groundwater levels (e.g., Rodell et al., 2007; Strassberg et al., 2007). Variations in groundwater storage ($\Delta S_{GW}$) were estimated from in situ measurements as:

$$\Delta S_{GW} = S_y \Delta H$$  (1)

where $S_y$ is the aquifer specific yield (%) and $H$ is the groundwater level (L$^{-1}$) observed in monitoring bores. Groundwater level data ($H$) were sourced from State Government departments that are part of the Murray-Darling Basin (QLD; Natural Resources and Mines; NSW; Department of Water and Energy; VIC; Department of Sustainability and Environment; and SA; Department of Water Land and Biodiversity Conservation). Only government observation bores (production bores excluded) with an average saturated zone <50 m from the bottom of the screened interval were selected. Deeper bores were excluded as they can reflect processes occurring on longer time scales (Fetter, 2001). A total of 6183 representative bores for the unconfined aquifers across the Murray Darling Basin were selected on the basis of construction and monitoring details obtained from the State departments. ~85% (5075) of the selected monitoring bores have a maximum annual standard deviation of the groundwater levels below 2 m for the study period (2000-2008) and were used to analyze the annual changes in groundwater storage during the period 2000 to 2008. The remaining 15% of the observation bores, with the highest annual standard deviation, were discarded as possibly under the immediate influence of local pumping or irrigation. The potential influence of irrigation on some of the groundwater data is limited because during
this period of drought, irrigation is substantially reduced across the basin. Changes in
groundwater levels across the basin were estimated using an annual time step as most
monitoring bores have limited groundwater level measurements in any year (50% of bores
with 5 measures per year). The annual median of the groundwater level was first calculated
for each bore and change at a bore was computed as the difference of annual median
groundwater level between two consecutive years. For each year, a spatial interpolation of the
groundwater level change was performed across the basin using a kriging technique. Spatial
averages of annual groundwater level change were computed for each aquifer group.
The Murray Darling drainage basin comprises several unconfined aquifers that can be
regrouped into 3 categories according to their lithology: a clayey sand aquifer group
(including the aquifers Narrabri (part of), Cowra, Shepparton, and Murrumbidgee (part of)); a
sandy clay aquifer group (including the aquifers Narrabri (part of), Parilla, Far west, and
Calivil (part of)); and a fractured rock aquifer group comprising metasediments, volcanics and
weathered granite (including the aquifers Murrumbidgee (part of), North central, North east,
Central west, Barwon, and Queensland boundary). The specific yield is estimated to range
from 5 to 10% for the clayey sand unconfined aquifer group (Macumber, 1999; Cresswell et
al., 2003; Hekmeijer and Dawes, 2003a; CSIRO, 2008); from 10 to 15% for the shallow
sandy clay unconfined aquifer group (Macumber, 1999; Urbano et al., 2004); and from 1 to
10% for the fractured rock aquifer group (Cresswell et al., 2003; Hekmeijer and Dawes,
2003b; Smitt et al., 2003; Petheram et al., 2003). In situ estimates of changes in GW storage
are calculated using the spatially averaged change in annual groundwater level across each
type of unconfined aquifer group and the mean value of the specific yield for that group using
(Eq. 1); while the range of possible values for the specific yield was used to estimate the
uncertainty.
Groundwater changes in the deep, confined aquifers (mostly GAB and Renmark aquifers) are
either due to: 1) a change in groundwater recharge at the unconfined outcrop; 2) shallow
pumping at the unconfined outcrop or 3) deep pumping in confined areas for farming
(irrigation and cattle industry). GRACE TWS estimates accounts for all possible sources of
influence, while GW in situ estimates only include those occurring across the outcrop. Total
pumping from the deep, confined aquifers was estimated to amount to -0.42 km$^3$.yr$^{-1}$ in 2000
(Ife and Skelt, 2004), while groundwater pumping across the basin was -1.6 km$^3$ in 2002–
2003 (Kirby et al., 2006). To allow direct comparison between TWS and in-situ GW
estimates, pumping from the deep aquifers was added to the in-situ GW time series assuming
the -0.42 km$^3$.yr$^{-1}$ pumping rate remained constant during the study period.
3. Methodology

3.1. ICA-based filter

ICA is a powerful method for separating a multivariate signal into subcomponents assuming their mutual statistical independence (Comon, 1994; De Lathauwer et al., 2000). It is commonly used for blind signals separation and has various practical applications (Hyvärinen and Oja, 2000), including telecommunications (Ritsaniemi and Joutsensalo, 1999; Cristescu et al., 2000), medical signal processing (Vigário, 1997; van Hateren and van der Schaaf, 1998), speech signal processing (Stone, 2004), and electrical engineering (Gelle et al., 2001; Pöyhönen et al., 2003).

Assuming that an observation vector $y$ collected from $N$ sensors is the combination of $P$ ($N \geq P$) independent sources represented by the source vector $x$, the following linear statistical model can be considered:

$$ y = Mx $$ (2)

where $M$ is the mixing matrix whose elements $m_{ij}$ ($1 \leq i \leq N$, $1 \leq j \leq P$) indicate to what extent the $j$th source contribute to the $i$th observation. The columns $\{m_j\}$ are the mixing vectors.

The goal of ICA is to estimate the mixing matrix $M$ and/or the corresponding realizations of the source vector $x$, only knowing the realizations of the observation vector $y$, under the assumptions (De Lathauwer et al., 2000):

1) the mixing vectors are linearly independent,
2) the sources are statistically independent.

The original sources $x$ can be simply recovered by multiplying the observed signals $y$ with the inverse of the mixing matrix also known as the “unmixing” matrix:

$$ x = M^{-1}y $$ (3)

To retrieve the original source signals, at least $N$ observations are necessary if $N$ sources are present. ICA remains applicable for square or over-determined problems. ICA proceeds by maximizing the statistical independence of the estimated components. As a condition of applicability of the method, non-Gaussianity of the input signals has to be checked. The central limit theorem is then used for measuring the statistical independence of the components. Classical algorithms for ICA use centering and whitening based on eigenvalue decomposition (EVD) and reduction of dimension as main processing steps. Whitening ensures that the input observations are equally treated before dimension reduction.
ICA consists of three numerical steps. The first step of ICA is to centre the observed vector, i.e., to subtract the mean vector $m = E\{y\}$ to make $y$ a zero mean variable. The second step consists in whitening the vector $y$ to remove any correlation between the components of the observed vector. In other words, the components of the white vector $\tilde{y}$ have to be uncorrelated and their variances equal to unity. Letting $C = E\{yy^t\}$ be the correlation matrix of the input data, we define a linear transform $B$ that verifies the two following conditions:

$$\tilde{y} = By \quad (4)$$

and:

$$E\{\tilde{y}\tilde{y}^t\} = I_p \quad (5)$$

where $I_p$ is identity matrix of dimension $P \times P$.

This is easily accomplished by considering:

$$B = C^{-\frac{1}{2}} \quad (6)$$

The whitening is obtained using an EVD of the covariance matrix $C$:

$$C = EDE^t \quad (7)$$

where $E$ is the orthogonal matrix of the eigenvectors of $C$ and $D$ is the diagonal matrix of its eigenvalues. $D = \text{diag}(d_1,\ldots,d_P)$ as a reduction of the dimension of the data to the number of independent components (IC) $P$ is performed, discarding the too small eigenvalues.

For the third step, an orthogonal transformation of the whitened signals is used to find the separated sources by rotation of the joint density. The appropriate rotation is obtained by maximizing the non-normality of the marginal densities, since a linear mixture of independent random variables is necessarily more Gaussian than the original components.

Many algorithms of different complexities have been developed for ICA (Stone, 2004). The *FastICA* algorithm, a computationally highly efficient method for performing the estimation of ICA (Hyvärinen and Oja, 2000) has been considered to separate satellite gravity signals. It uses a fixed-point iteration scheme that has been found to be 10 to 100 times faster than conventional gradient methods for ICA (Hyvärinen, 1999).

We used the *FastICA* algorithm (available at [http://www.cis.hut.fi/projects/ica/fastica/](http://www.cis.hut.fi/projects/ica/fastica/)) to unravel the IC of the monthly gravity field anomaly in the Level-2 GRACE products. We previously demonstrated, on a synthetic case, that land and ocean mass anomalies are statistically independent from the north-south stripes using information from land and ocean models and simulated noise (Frappart et al., 2010). Considering that the GRACE Level-2 products from CSR, GFZ and JPL are different observations of the same monthly gravity
anomaly and, that the land hydrology and the north-south stripes are the independent sources, we applied this methodology to the complete 2002-2009 time series. The raw Level-2 GRACE solutions present Gaussian histograms which prevent the successful application of the ICA method. To ensure the non-Gaussianity of the observations, the raw data have been preprocessed using Gaussian filters with averaging radii of 300, 400 and 500 km as in Frappart et al. (2010).

3.2. Time-series of basin-scale total water storage average

For a given month \( t \), the regional average of land water volume \( \delta V(t) \) (or height \( \delta h(t) \)) over a given river basin of area \( A \) is simply computed from the water height \( \delta h_j \), with \( j=1, 2, \ldots \) (expressed in terms of mm of equivalent-water height) inside \( A \), and the elementary surface \( R_e^2 \delta \lambda \delta \theta \sin \theta_h \):

\[
\delta V(t) = R_e^2 \sum_{j \in A} \delta h_j (\theta_j, \lambda_j, t) \sin \theta_j \delta \lambda \delta \theta
\]  
(8)

\[
\delta h(t) = \frac{R_e^2}{A} \sum_{j \in A} \delta h_j (\theta_j, \lambda_j, t) \sin \theta_j \delta \lambda \delta \theta
\]  
(9)

where \( \theta_j \) and \( \lambda_j \) are co-latitude and longitude of the \( j^{\text{th}} \) point, \( \delta \lambda \) and \( \delta \theta \) are the grid steps in longitude and latitude respectively (generally \( \delta \lambda = \delta \theta \)). In practice, all points of \( A \) used in (Eq. 8 and 9) are extracted for the eleven drainage basins masks at a 0.5° resolution provided by Oki and Sud (1998), except for the Murray Darling Basin where we used basin limits from Leblanc et al. (2009).

3.3. Regional estimates of formal error

As ICA provides separated solutions which have Gaussian distributions, the variance of the regional average for a given basin is:

\[
\sigma_{\text{formal}}^2 = \frac{\sum_{k=1}^{L} \sigma_k^2}{L}
\]  
(10)

where \( \sigma_{\text{formal}} \) is the regional formal error, \( \sigma_k \) is the formal error at a grid point number \( k \), and \( L \) is the number of points used in the regional averaging.

If the points inside the considered basin are independent, this relation is slightly simplified:

\[
\sigma_{\text{formal}} = \frac{\sigma_k}{\sqrt{L}}
\]  
(11)
3.4. Frequency cut-off error estimates

Error in frequency cut-off represents the loss of energy in the short spatial wavelength due to the low-pass harmonic decomposition of the signals that is stopped at the maximum degree $N_1$. For the GRACE solution separated by ICA; $N_1=60$, thus the spatial resolution is limited and stopped at ~330 km by construction. This error is simply evaluated by considering the difference of reconstructing the remaining spectrum between two cutting harmonic degrees $N_1$ and $N_2$, where $N_2 > N_1$ and $N_2$ should be large enough compared to $N_1$ (e.g., $N_2=300$ in study):

$$\sigma_{\text{truncation}} = \sum_{n=0}^{N_1} \xi_n - \sum_{n=0}^{N_1} \xi_n^+ = \sum_{n=N_1}^{N_2} \xi_n$$  \hspace{1cm} (12)

using the scalar product

$$\xi_n^+ = \sum_{m=0}^{N} (C_{nm} A_{nm} + S_{nm} B_{nm})$$  \hspace{1cm} (13)

where $A_{nm}$ and $B_{nm}$ are the harmonic coefficients of the considered geographical mask, and $C_{nm}$ and $S_{nm}$ are the harmonic coefficients of the water masses.

3.5. Leakage error estimates

We define « leakage » as the portion of signals from outside the considered geographical region that pollutes the region’s estimates. By construction, this effect can be seen as the limitation of the geoid signals degree in the spherical harmonics representation. For each basin and at each period of time, leakage is simply computed as the average of outside values by using an « inverse » mask, which is 0 and 1 in and out of the region respectively, developed in spherical harmonics and then truncated at degree 60. This method of computing leakage of continental water mass has been previously proposed for the entire continent of Antarctica (Ramillien et al., 2006b), which revealed that the seasonal amplitude of this type of error can be quite important (e.g. up to 10% of the geophysical signals). In case of no leakage, this average should be zero (at least, it decreases with the maximum degree of decomposition). However, the maximum leakage of continental hydrology remains in the order of the signals magnitude itself.

4. Results and discussion

4.1. ICA-filtered land water solutions

The methodology presented in Frappart et al. (2010) has been applied to the Level-2 RL04 raw monthly GRACE solutions from CSR, GFZ and JPL, preprocessed using a Gaussian filter with a radius of 300, 400 and 500 km, over the period July 2002 to July 2009. The results of this filtering method is presented in Fig. 1 for four different time periods (March and
September 2006, March 2007 and March 2008) using the GFZ solutions Gaussian-filtered with a radius of 400 km. Only the ICA-based GFZ solution is presented since, for a specific radius, the ICA-based CSR, GFZ, and JPL solutions only differ from a scaling factor for each specific component. The ICA-filtered CSR, GFZ, and JPL solutions are obtained by multiplying the $j^{th}$ IC with the $j^{th}$ mixing vector (2). As the last two modes correspond to the north–south stripes, we present their sum in Fig. 1.

The first component is clearly ascribed to terrestrial water storage with variations in the range of ±450 mm of Equivalent Water Thickness (EWT) for an averaging radius of 400 km. The larger water mass anomalies are observed in the tropical regions, i.e., the Amazon, the Congo, the Ganges and the Mekong Basins, and at high latitudes in the northern hemisphere. The components 2 and 3 correspond to the north-south stripes due to resonances in the satellite’s orbits. They are smaller than the first component by a factor of 3 or 4 as previously found (Frappart et al., 2010).

The FastICA algorithm was unable to retrieve realistic patterns and/or amplitudes of TWS-derived from GRACE data preprocessed using a Gaussian filter with a radius 300 km for several months (02/2003, 06 to 11/2004, 02/2005, 07/2005, 01/2006, 01/2007, 02/2009). Some of these dates, such as the period between June and November 2004, correspond to deep resonance between the satellites caused by an almost exact repeat of the orbit, responsible for a significantly poorer accuracy of the monthly solutions (Chambers, 2006). As ICA is based on the assumption of independence of the sources, if the sources exhibit similar statistical distribution, the algorithm is unable to separate them.

A classical measure of the peakiness of the probability distribution is given by the kurtosis. The kurtosis $K_y$ is dimensionless fourth moment of a variable $y$ and classically defined as:

$$K_y = \frac{E\{y^4\}}{E\{y^2\}^2}$$  \hspace{1cm} (14)

If the probability density function of $y$ is purely Gaussian, its kurtosis has the numerical value of 3. In the followings, we will consider the excess of kurtosis ($K_y - 3$) and refer to the kurtosis as it is commonly done. So a variable $y$ will be Gaussian if its kurtosis remains close to 0.

The time series of the kurtosis of the sources separated using ICA are presented in Fig. 2 for different radii of Gaussian filtering (300, 400 and 500 km) of GRACE mass anomalies. The kurtosis of the sum of the 2nd and 3rd ICs, corresponding to the north-south stripes, is most of the time, close to 0; that is to say that the meridian oriented spurious signals is almost Gaussian. Almost equal values of the kurtosis for the 1st IC and the sum of the 2nd and 3rd ICs.
can be observed for several months. Most of the time, they correspond to time steps where the
algorithm is unable to retrieve realistic TWS (02/2003, 08/2004, 11/2004, 02/2005, 01/2006,
01/2007, 02/2009).

We also observed that the number of time steps with only one IC (the outputs are identical to
the inputs, i.e., no independent sources are identified and hence no filtering was performed)
increases with the radius of the Gaussian filter (none at 300 km, 2 at 400 km, 7 at 500 km).

In the following, as the ICA-derived TWS with a Gaussian prefiltering of 300 km, exhibits an
important gap of 6 months in 2004, we will only consider the solutions obtained after a
preprocessing with a Gaussian filter for radii of 400 and 500 km (ICA400 and ICA500).

4.2. Global scale comparisons

Global scale comparisons have been achieved with commonly-used GRACE hydrology
preprocessings: the Gaussian filter (Jekeli, 1981) and the destriping method (Swenson and
Wahr, 2006) for several smoothing radii.

4.2.1. ICA versus Gaussian-filtered solutions

Advantages of extracting continental hydrology using ICA after a simple Gaussian filtering
have to be demonstrated for the complete period of availability of the GRACE Level-2
dataset, as it was for one period of GRACE Level-2 data in Frappart et al., (2010). Numerical
tests of comparisons before and after ICA have been made to show full utility of considering a
post-treatment by ICA for signals separation. For the period 2003-2008, we present
correlation (Fig. 3) and RMS (Fig. 4) maps computed between the ICA400 (respectively
ICA500) and Gaussian-filtered solutions with a radius of 400 km (500 km), named in the
followings G400 (G500). High correlation coefficients are generally observed over land
(greater than 0.9), increasing with the smoothing radius, especially over areas with large
hydrological signals, i.e., Amazon, Congo and Ganges basins, boreal regions. On the contrary,
low correlation values, structured as stripes, are located over arid and semi-arid regions
(southwest of the US, Sahara, Saudi Arabia, Gobi desert, centre of Australia), especially for
GFZ and JPL solutions. These important RMS differences between Gaussian and ICA-based
solutions reveal that the GRACE signals still contains remaining stripes after the Gaussian
filtering. This justifies that extracting the useful continental hydrology signals requires a
further processing. For this purpose, ICA succeeds in isolating this noise in its second and
third components (as illustrated in Figure 1).
In Fig. 4, we observe that the spatial distribution of the RMS between ICA solutions and Gaussian solutions presents north-south stripes with values generally lower than 30 mm, except for some spots between ±(20 – 30°) of latitudes on the GFZ (Fig. 4c and d) and JPL (Fig. 4e and e) solutions. The ICA approach allows the filtering of remnant stripes present in the Gaussian solutions, especially for GFZ and JPL (Fig. 4c to f). These unrealistic structures (stripes and spots), which correspond to resonances in the orbit of the satellites, are clearly filtered out using the ICA approach (compare with Fig. 1). A more important smoothing due to a larger radius caused a decrease of the RMS between ICA and Gaussian solutions (Fig 4a, c and e). The RMS can reach 100 mm between ICA400 and G400 and only 65 mm between ICA500 and G500 for the GFZ solutions.

4.2.2. ICA versus destriped and smoothed solutions

Similar to Fig. 3 and 4, we present correlation (Fig. 5) and RMS (Fig. 6) maps over the period 2003-2008; between ICA400 (ICA500 respectively) and destriped and smoothed solutions with radii of 300 km (DS300) and 500 km (DS500), made available by Chambers (2006). The correlation maps between ICA400 (respectively ICA500) and DS300 (DS500) exhibit very similar patterns compared with those presented in Fig. 3, except in the McKenzie Basin and Nunavut (northern Canada) where low correlation or negative correlations for GFZ and JPL solutions (Fig. 5c to f) are found.

The RMS differences between ICA and destriped and smoothed solutions present low values above 30° (or below -30°) of latitude (< 30 mm of EWT), with the exceptions of Nunavut in northern Canada and extreme values (up to 100 mm) in the tropics. This is clearly due to the low performance of the destripping method in areas close to Equator as previously mentioned by Swenson and Wahr (2006) and Klees et al. (2008). These extrema are especially present in the DS300 GFZ and JPL solutions. Some secondary maxima (up to 80 mm) are also noticed for the GFZ and the JPL solutions. These important differences correspond to north-south stripes that still appear in the destriped and smoothed solutions despite the filtering process (and that can be filtered out by applying an ICA approach – see the results for DS300 GFZ solution of March 2006 in Fig. 7). For an averaging radius of 500 km, the RMS between ICA500 and DS500 is lower than 20 to 30 mm, except for the Nunavut (Fig. 6b, d, f), along the Parana stream (40 to 50 mm in the CSR solutions – Fig. 6b), and along the Amazon and Parana streams (60 to 80 mm in the GFZ solutions – Fig. 6d).
These low spatial correlations suggest Gaussian-ICA provides at the least equivalent results on the continents to the smoothing-destriping method. Besides, it is interesting that both approaches are based on a pre-Gaussian filtering. Short wavelength differences between the maps obtained separately using ICA and destriping reveals the limitation of the destriping which generates artefacts in the tropics.

4.2.3. Trend comparisons

The effects of the stripes on the trends estimated using GRACE-based TWS is supposed to be significant. From the time-series of TWS anomaly grids derived from GRACE (using equation 1), the temporal trend, seasonal and semi-annual amplitudes were simultaneously fitted by least-square adjustment at each grid point over the period 2003-2008 (see Frappart et al., in press, for details). We present in Fig. 8 trends of TWS for ICA400 (Fig. 8a) and ICA500 (Fig. 8b), for G400 (Fig. 8c) and G500 (Fig. 8d), and for DS300 (Fig. 8e) and DS500 (Fig. 8f).

The trend estimates exhibit large differences in spatial patterns and the amplitude of the signal, especially between ICA and other processing methods. The most significant differences over land (except Antarctica) are located at high latitudes, over Scandinavia, and the Laurentide region, in the northeast of Canada. The ICA400 and ICA500 solutions present negative trends of TWS (Fig. 8a and b), whereas the G400 and G500 and the DS300 and DS500 present large positive trends (Fig. 8c to f). These two zones are strongly affected by the post-glacial rebound (PGR) which has a specific signature in the observed gravity field. This effect accounts for positive trends in these regions. According to the PGR models developed by Peltier (2004) and Paulson et al. (2007), its intensity can be greater in these regions than the trends measured by GRACE. For example, in the Nelson Basin, Frappart et al. (in press) found a trend of TWS from GRACE of (4.5 ± 0.2) mm/yr over 2003-2006, while model-based estimates of PGR represents 18.8 mm/yr in this region. As the space and time characteristics of the glacial isostatic adjustement (GIA) is different than the one from continental hydrology, the ICA approach may have separated it from the signals only related to the redistribution of water masses. Unfortunately, trends computed on the 2nd and 3rd ICs, and their sum does not exclusively correspond to GIA, but to a mixture of geophysical remaining signals and noise. It is also worth noticing that the gravity signature of the Sumatra event in December 2004, which is clearly apparent on the Gaussian-filtered solutions (Fig. 8c and d), is not visible in the 1st mode of the ICA solutions (Fig. 8a and b), but is present in the
sum of the 2nd and 3rd ICs. This confirms that the ICA is able to isolate a pure hydrological mode in the GRACE products.

A second important difference between ICA solutions and Gaussian-filtered and destriped and smoothed solutions concerns the impact of the filtering radius on the trends estimate. An increase of the filtering radius causes a smoothing of the solutions, and, consequently, a decrease of the intensity of the trends on Gaussian-filtered and destriped and smoothed solutions (Fig. 8c to f). On the contrary, the intensity of the trends increases with radius of prefiltering on the ICA solutions. The location of the extrema is also shifted. This change in the location is a side-effect of the prefiltering with the Gaussian filter. A better location of the trends is observed when a Gaussian-filter of 400 km of radius is used instead of 500 km (see for instance the trends pattern in the Amazon and Orinoco Basins in Fig. 8a and b).

4.3. Basin scale comparisons

Changes in total water volume were estimated for 27 drainage basins whose locations are shown in Fig. 9 (the corresponding areas are given in Table 1). ICA400 and ICA500 were used to compute regional TWS averages versus time (Eq. 8 and 9). These times-series were compared to the G400 and G500, and the DS300 and DS500 respectively. Examples of the Amazon, the Ob and the Mekong basins for ICA400, G400 and DS300 (GFZ solutions) are presented in Fig. 10. TWS exhibit very similar temporal patterns for all the types of filtering radii and basins. The correlation coefficients between the ICA and the Gaussian-filtered, or the ICA and the destriped and smoothed time series of TWS are greater than 0.9 for 21 out of 27 basins. For five other basins (Amur, Colorado, Hwang Ho, Parana, St Lawrence), most of the correlation coefficients are greater than 0.8 or 0.9, and the others (generally the correlation coefficients between ICA and destriped and smoothed GFZ solutions) greater than 0.65 or 0.7. The only exception is the McKenzie Basin where all the correlation coefficients between ICA and destriped and smoothed are lower than 0.75 ($r_{ICA400,DS300,JPL}$=0.45 and $r_{ICA500,DS500,JPL}$=0.51). For the GFZ solutions, some unrealistic peaks are present in the destriped and smoothed TWS time series for some periods (Fig. 10a, 10b and 10c). These peaks only appear on the Gaussian-filtered solutions for the smallest basins, such as the one of the Mekong river (Fig. 10c), but are not present in the ICA-filtered solutions. RMS difference between ICA-filtered solutions and the other type of solutions are generally lower than 30 mm of equivalent water height and logically decrease with the radius of filtering. Differences with ICA solutions are generally larger for the GFZ-based destriped solutions, especially in tropical
regions where the performances of the destriping are not the best and the hydrological signal the largest (Fig. 11).

We present an analysis of possible sources of error on the computation of regional averages versus time using the 300, 400, 500-km pre-filtered ICA solutions. This task is made on the longest available period of time for each center (CSR, JPL, GFZ), and for the 27 drainage basins (Table 1).

The formal error decreases with the number of points (see Eq. 10 and 11), the surface of the considered region, and the value of error $\sigma_k$ at each grid point. In the case of the Amazon Basin (~6 millions of km²), the formal error is only of 4.5 mm when $\sigma_k = 100$ mm of equivalent-water height. For the Dniepr river basin that represents the smallest surface of our chosen basins (~0.52 million of km²), the formal error reaches 12.3 mm. For the series of basins, the maximum values of formal errors on the regional average are in the range of 10-15 km³ of water volume per hundred of mm of error on the gridded points.

To estimate the frequency cut-off error or “omission error”, we made statistics of the numerical tests were performed to see what maximum error can be reached using Eq. 12. We computed this residual quantity for 300, 400 and 500 km-filtered ICA solutions and for each hydrological basin for $N_1=60$ and $N_2=300$. The maximum error is always less than 1 km³, as shown previously (Ramillien et al., 2006a), and it decreases with the filtering wavelength of the pre-processing. In other words, this error simply increases with the level of noise in the data. For the 300 km and 400 km pre-filtered solutions, the maximum values are found for the Amur River: 0.3 km³ (CSR), 0.1 km³ (JPL), and 0.8 km³ (GFZ), and 0.04 km³ (CSR), 0.09 km³ (JPL), 0.08 km³ (GFZ) respectively. While using the 500-km filtered solutions, the error of truncation is less than 0.005 km³.

The leakage error on the ICA solutions was computed per drainage basin (see section 3.5). The results are presented in Fig. 12 for the different centres and radii of Gaussian prefiltering of 300, 400 and 500 km. We observed that the leakage decreases with radius of filtering and is generally lower in the JPL solutions, which presents lowest peak to peak amplitudes. This leakage error is logically greater in areas where several basins with large hydrological signal are close, i.e., South America with the Amazon, the Parana, the Orinoco and the Tocantins, or tropical Asia with the Ganges, the Brahmaputra and the Mekong rivers. The leakage error is also greater for basins with small hydrological signals close to a predominant basin having important hydrological variations, i.e., the Okavango and the Zambezi with the Congo.

\section*{4.4. Basin scale validation}
GRACE observations were used to estimate variations in TWS over the Murray Darling Basin (see Fig. 13 for the location of the basin) at an interannual scale from January 2003 to December 2008. The annual variations in TWS from GRACE for different types of solutions were compared to the annual TWS computed as the sum of in situ observations (SW+GW) and NOAH outputs (SM). In the Murray-Darling River basin, GLDAS-NOAH simulations of SM range from 5 to 29% (in volumetric water content) across the basin for the study period, and are within typical values for monthly means at 1° resolution (Lawrence and Hornberger, 2007). Besides, Leblanc et al. (2009) show that, between 2003 and 2007, the linear rate of water changes for the GRACE TWS time series is similar to that observed for the annual total water storage from in situ observations and modeling. The combined annual anomalies of surface water, groundwater and soil moisture are highly correlated with the annual GRACE TWS (R = 0.94 and mean absolute difference =13 km$^3$ for the 2003–2007 period). These latter interannual field-based data are considered as the reference in the following analysis. The results are presented on Fig. 14 for the GFZ solutions. The ICA solutions generally present a temporal pattern closer to the so-called reference (i.e., the sum of in situ data for SW and GW and model outputs for SM). This temporal pattern and the associated dynamics do not change with the radius of filtering, which is not the case with the Gaussian filtered, and the destriped and smoothed solutions. None of the solutions are able to retrieve the minimum observed in 2007 in the reference dataset. It is important to notice that the largest part of the interannual variations of TWS comes from the GW reservoir. For this hydrological component, the water storage is derived from in situ measurements through Eq. (1), and is highly dependent on the specific yield coefficient; where averages of local measurements are used to determine ranges of regional-scale estimates. For the Murray Darling Basin, composed of several aquifers, this leads to a broad range of spatial variability for the GW estimates. This variability is around or greater than 20 km$^3$ for 2002, 2007 and 2008 and around 10 km$^3$ for 2003, 5 km$^3$ in 2004 and 2006, 2.5 km$^3$ in 2005. We present yearly deviations to the reference for the different considered solutions (Fig. 15) over 2003-2006, where the range of variability of the GW is lower. Generally, the absolute deviation of ICA-derived TWS to the reference is lower than 5 km$^3$, especially for solutions filtered at 400 km. At 500 km, the smoothing due to the preprocessing using a Gaussian filter is more important and explains the slight increase of the absolute deviation as the spatial resolution is degraded. The destriping method and the Gaussian filtering also exhibit good performances, even if
important deviations are sometimes observed (particularly with the Gaussian filter for a radius of 400 km).

5. Conclusion

The ICA-based approach is a very efficient method for successfully separating TWS from noise in the GRACE Level-2 data. We demonstrated that this method is more robust than classical filtering methods, such as the Gaussian filtering or the destriping. Comparisons at a global-scale showed that the ICA-based solutions present less north-south stripes than Gaussian and destriped solutions on the land, and more realistic hydrological structures than the destriped solutions in the tropics. Trend maps over 2003-2008 have also been computed. The corresponding trend maps present more realistic trend patterns than those obtained with other types of solutions (see for example over the Amazon and Orinoco Basins with the 400 km radius of prefiltering). ICA filtering seems to allow the separation of the GIA from the TWS as negative trends were found over the Laurentides and Scandinavia. Unfortunately, this important geophysical parameter does not appear clearly in an ICA mode yet. The major drawback of this approach is that it can not directly be applied to the GRACE Level-2 raw data, as a first step of prefiltering is required. In this study, we applied a Gaussian filtering which deteriorates the location of the important water mass patterns. This aspect of the pre-treatment to be improved and highlights the necessity to replace the Gaussian filter used for preprocessing the GRACE Level-2 raw data by one more suited to improve the quality of the GRACE-derived TWS and thus obtain trustworthy estimate of the trends.

At the basin-scale, the ICA-based solutions allowed us to filter out the unrealistic peaks present in the time-series of TWS obtained using classical filtering for basins with areas lower than one million km². Among the ICA-based solutions, the JPL solutions are less affected by leakage compared with other solutions. JPL solutions also exhibit the lowest peak-to-peak amplitudes. The error balance of the GRACE-derived TWS is dominated by the effect of the leakage.

Validation with *in situ* measurements was performed in the Murray Darling Basin where broad networks of *in situ* measurements of SW and GW are available. The ICA-based solutions are in better agreement with *in situ* data compared with the other types of solutions, especially where prefiltering at a 400 km of radius. The maximum deviations are lower by a factor two or three compared with the other filtering methods.

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References


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**Table 1:** The 29 drainage basins considered in this study sorted by decreasing area.

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**Figure 1:** GRACE water storage from GFZ filtered with a Gaussian filter of 400 km of radius. (Top) First ICA component corresponding to land hydrology and ocean mass. (Bottom) Sum of the second and third components corresponding to the north–south stripes. (a) March 2006, (b) September 2006, (c) March 2007, (d) March 2008. Units are millimeters of EWT.

**Figure 2:** Time series of the kurtosis of the mass anomalies detected by GRACE after Gaussian filtering for radii of a) 300 km, b) 400 km, c) 500 km.

**Figure 3:** Correlation maps over the period 2003-2008 between the ICA-filtered TWS and the Gaussian-filtered TWS. Left column: ICA400-G400 (a: CSR, c: GFZ, e: JPL). Right column: ICA500-G500 (b: CSR, d: GFZ, f: JPL).

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Figure 6: RMS maps over the period 2003-2008 between the ICA-filtered TWS and the destriped and smoothed TWS. Left column: ICA400-DS300 (a: CSR, c: GFZ, e: JPL). Right column: ICA500-DS500 (b: CSR, d: GFZ, f: JPL).

Figure 7: GRACE water storage from GFZ destriped and smoothed with a Gaussian filter of 300 km of radius for March 2006. (Top) First ICA component corresponding to land hydrology. (Bottom) Sum of the second and third components corresponding to the north–south stripes.

Figure 8: Trend maps over the period 2003-2008 of TWS using the GFZ solutions a) ICA400, b) ICA500, c) G400, d) G500, e) DS300 and f) DS500.

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Figure 12: Standard deviation of the leakage error (mm) per basin (sorted by decreasing area of drainage basin) over the period October 2002 – July 2009 for the ICA solutions.

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Figure 15: Yearly deviation over 2003-2006 from in situ + model TWS of GRACE-derived TWS filtered with different approaches at a) 400 km of filtering (300 km for the destriped solutions) and b) 500 km. In blue, the ICA solutions (dark blue: CSR, blue: GFZ, light blue: JPL), in green, the Gaussian solutions (dark green: CSR, green: GFZ, light green: JPL), and the destriped and smoothed solutions (red: CSR, orange: GFZ, yellow: JPL).
### Tables

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Figures

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