A new semi-empirical model for the oxidation of PAHs physisorbed on soot. I. Application to the reaction $\text{C}_6\text{H}_6 + \text{OH}$.

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**A new semi-empirical model for the oxidation of PAHs
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A new semi-empirical model for the oxidation
of PAHs physisorbed on soot. I. Application
to the reaction $C_6H_6 + OH$.

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Abstract

In the present paper, we have used a new semi-empirical method to characterize the oxidation by OH of a benzene molecule adsorbed on a soot surface modelled by a graphene-like cluster. This method is based on an electrostatic and induction contribution calculated at the SCF AM1 level associated with a sum of two-body dispersion terms of the $C^{(6)}/R^6$ form. This so-called AM1-D method has been used to compare the characteristics of the oxidation reaction for the adsorbed benzene with those of the corresponding reaction in the gas phase. The main conclusion of the present work is a clear inhibition of the oxidation process by the adsorption of the benzene molecule on the soot surface. This conclusion is in qualitative agreement with experimental observations, concerning however larger PAH molecules.

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Key words: semi-empirical method, soot, PAH, oxidation

* This paper is dedicated to the memory of our friend Jose Antonio Mejias who initiated our work on soot surfaces.

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1 Introduction

Polycyclic aromatic hydrocarbons (PAHs) are chemical pollutants ubiquitous in the atmosphere, aerosols, soils and sediments. They are mainly formed as by-products of combustion processes under oxygen-deficient conditions, and many of them and their degradation products are known or suspected allergen and carcinogens[1].

It has been long understood that the reactive fate of volatile PAHs (less than 3-4 rings) is governed by gas-phase reactions with the hydroxyl (OH) radical. However, due to their low vapor pressure and aromaticity, heavier PAHs are mostly adsorbed on fine carbonaceous particles[2] where they are subject of a wide range of heterogeneous chemical reactions depending on the particle composition[3–7]. This heterogeneous reactivity may thus be more important than the corresponding gas-phase reactions as sink for these compounds. Moreover, heterogeneous reactions of particle-bound PAHs may change the microphysical properties of the particle by making it more hygroscopic and hence modifying its cloud nucleation properties[8]. These heterogeneous reactions can also influence the atmospheric residence times of the carbonaceous particles and consequently their direct and indirect effects on climate[9,10].

During the incomplete combustion of carbonaceous fuels, PAHs are formed concurrently with soot particles and they play a significant role in soot formation and subsequent particle growth[11]. Soot is ubiquitous in the environment where it has been observed to comprise tens of percent of the total aerosol carbon in both rural and urban areas[12,13]. Because PAHs have a high affinity for carbonaceous materials, adsorption of PAHs on soot may be an important

mechanism affecting the gas-particle partitioning of PAHs[14].

Despite the importance of PAHs and soot particles interactions, their actual effect on the radiative and chemical budgets of the atmosphere is still poorly known and some of this uncertainty is due to the lack of knowledge about the physicochemical properties of the soot substrate[15,16]. Fresh soot particles consist of spherical primary carbonaceous particles that aggregate into larger clusters of fractal-like shape[17]. These primary particles are often made of nanocrystallites containing graphite-type layers arranged in an onion-like structure, with diameters ranging between 20 and 50 nm[18,19]. Soot particles are usually associated with organic and inorganic soluble material at their surfaces. One of the major problem is thus that soot is not a well-defined chemical substance[20]. Therefore, model particles are often used as a first approach to study atmospheric chemical processes as they are simpler and better characterized than natural particles[21,22]. There are several types of soot used for laboratory studies of atmospheric effects: commercial soot[23], spark-discharge soot[24,25], and soot resulting from the combustion of hydrocarbon fuels in different burners[26,27]. However, different types of soot differ in particle size, specific surface area, structure, and composition, and thus they may differ in chemical properties. As a consequence, studies of the physico-chemistry of PAHs on soot surfaces are very scarce. Up to now, there are only a limited number of controlled laboratory[28,29] or field[30,31] studies on the adsorption of gas-phase PAHs onto soot, and, to our best knowledge, there is only one paper devoted to the experimental study of the uptake of aromatic hydrocarbons onto soot with a known surface area, as a function of temperature and partial pressure[4].

In a recent study, Esteve et al.[21] have characterized the role of OH, NO₂

and NO radicals on the reactivity of 11 polyaromatic compounds adsorbed on graphite particles chosen as a model of atmospheric carbonaceous particles. The results showed that the reaction of particulate-PAHs with NO is negligible under atmospheric conditions, whereas in the case of the NO₂ reaction, significant differences in the reactivities have been observed. Moreover, all PAHs present similar rate constants while reacting with OH, and, compared to the reactivity in the gas phase, the heterogeneous reaction with OH radicals seems to show a potential inhibiting effect of the graphite surface, meaning that the mechanisms may be sensibly different[21].

From a theoretical point of view, structural and energetic information on the interaction between PAHs and carbonaceous surfaces like soot is also very scarce, primarily due to the fact that these systems are too large for tractable *ab initio* calculations. Indeed, a theoretical realistic simulation of intermolecular forces requires high level electronic quantum calculations to account for dispersion effects. The expression "high level quantum calculations" means the use of very large basis sets and a precise description of the correlation energy. Even for a simple perturbative approach, double excitations on two interacting molecules are necessary to mimic (in general rather poorly) dispersion effects. Then, the most accurate methods for determining the geometry and binding energy of PAHs clusters are correlated quantum chemistry calculations that use very large correlation-consistent basis sets. Moreover, very large basis sets are necessary to minimize both the basis set convergence error and the basis set superposition error (BSSE). Such high-level calculations require a great amount of computational resources[32] and if they are possible for, i.e., benzene dimers[33], they are not conceivable for larger systems.

Recently, an interesting method - the Hartree-Fock Dispersion model (HFD)

- has been introduced by Gonzalez et al.[34,35] to calculate the structure and binding energy of aromatic clusters, following the work originally proposed by Hepburn et al.[36]. In this HFD method, the calculation of the intermolecular energies combines an *ab initio* self-consistent field (SCF) interaction energy with an empirical dispersion energy from the London theory, i.e., an analytical approach much more efficient to describe dispersion than the direct calculation from electronic correlation effects[34]. The accuracy of this method has been tested in computing the equilibrium geometries and the binding energies of the van der Waals dimers of benzene, naphthalene, anthracene, and pyrene, as well as those of the naphthalene trimer[35]. However, even the HFD method is prohibited for a theoretical characterization of the PAHs/soot interactions, when considering large size PAHs and/or large graphite clusters modelling the soot surface. We have thus introduced, in a recent paper[37], a new method where the SCF calculations are performed at a semi-empirical level by including explicitly the valence electrons only. This method, so called the SE-D method, combines the semi-empirical description of the electrostatic and induction interactions to a sum of two-body London dispersion terms of the $C^{(6)}/R^6$ form. The empirical parameters of this method have been fitted on a set of *ab initio* and experimental results for 22 PAHs dimers and mixed complexes, aiming at defining a transferable interaction potential for the calculations of dispersion energy between aromatic molecules and large graphite clusters[37]. Three sets of transferable parameters have thus been determined for combination with electrostatic and induction interactions performed at the AM1, PM3, or MNDO level of theory, with, however, slightly better results when the dispersion parameters are combined with the AM1 and PM3 methods than with the MNDO method[37,38].

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3 It is worth mentioning that such an approach that aims at describ-
4 ing intermolecular interactions in large carbonaceous systems on the
5 basis of semi-empirical calculations shows similarities with meth-
6 ods recently developed to improve the semi-empirical description
7 of other systems for which refined quantum calculations are too
8 costly. For example, electrostatic and dispersion corrections have
9 been brought to the AM1 or PM3 semi-empirical energy to repro-
10 duce correctly the long-range behavior of the interaction potential
11 in hydrogen bonded systems[39–41]. Similarly, an atom-atom pair-
12 wise additive dispersion potential has also been recently added to
13 a semi-empirical description of the intermolecular interactions in
14 biomolecules[42].
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39 In the present paper, we make use of the SE-D method to characterize the ox-
40 idation mechanisms of PAH molecules adsorbed at the soot surface modelled
41 by a large carbon cluster of graphene type. Such a large cluster has been pre-
42 viously used to model soot surfaces interacting with water molecules using *ab*
43 *initio* approaches[43–45]. The theoretical backgrounds of our study are given
44 in Section 2, and, as a first application, the results of the detailed investigation
45 of the heterogeneous oxidation reaction of benzene adsorbed on soot are then
46 presented in Section 3. These results are compared with those obtained in the
47 gas phase and they are discussed on the basis of experimental observations in
48 Section 4.
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2 Theoretical backgrounds

2.1 The SE-D method

In this section, we briefly recall the main basis of the SE-D model[37,38]. In this model, a dispersion term (U_d) is added to a semi-empirical determination of the electrostatic and induction interactions to account for dispersion forces in the calculation of the total energy. This total energy for a PAH adsorbed on a carbonaceous particle modelling a soot surface is thus written as

$$U_{\text{SE-D}} = U_{\text{SE}} + f \times U_{\text{D}}, \quad (1)$$

where U_{SE} is the semi-empirical energy calculated at the AM1, PM3, or MNDO level of theory, U_{D} is the dispersion energy, and f is a damping function used to avoid singularities in the dispersion term at short intermolecular distances. Note that these semi-empirical methods are proposed to reproduce, within an given average accuracy, geometries, heats of formation and some other thermodynamical data. These quantities are mainly due to "chemical forces" which are responsible for bond energies i.e. energy differences between separated fragments and the interacting systems at equilibrium distances. However, due to the reduced basis set used (valence atomic orbitals), it is impossible to reproduce a long range quantum effect like dispersion. It is already almost impossible to do it with a "reasonably good" *ab initio* approach. On the contrary, long range electrostatic and induction effects, which are not at all quantum in nature but strictly classical, are included in a

more or less realistic way in the calculations by the self-consistent field procedure itself. The electrostatic interaction energy is given by the first SCF iteration and the induction energy at the SCF convergence since the electronic cloud, which corresponds to the average electronic field felt by each electron, reaches its final shape at the end of the SCF iterations. It turns out that the introduction of a sum of $-R^{-6}$ terms added at long distance to the SCF energy appears as an elegant way to include dispersion, even if it requires some "savoir-faire" for the estimation of these terms.

The dispersion contribution to the total energy is thus expressed as[46]

$$f \times U_D = - \sum_{i=1}^{N_g} \sum_{j=1}^{N_p} \frac{1}{(1 + e^{\alpha(R_0 - R_{ij})})} \times \frac{[C_i^{(6)} C_j^{(6)}]^{1/2}}{R_{ij}^6}, \quad (2)$$

where N_g and N_p are the total number of atoms on the carbonaceous surface and in the PAH molecule considered, respectively. R_{ij} is the interatomic distance between a surface atom i and the j th atom of the PAH molecule, and $C^{(6)}$ represents the two-body dispersion coefficients used to calculate the C-C, C-H and H-H interactions. The damping function $f(R_{ij})$ has the two-parameter hyperbolic tangent function form proposed by Gonzales et al.[34,35], in which α and R_0 are two empirical parameters that monitor the behavior of the damping function, and thus of the dispersion interaction, as a function of the interatomic distances R_{ij} .

The dispersion parameters α , R_0 , and $C_j^{(6)}$ of the SE-D approach have been fitted for the combination with a semi-empirical calculation of the SCF contribution to the interaction energy. These parameters have been proved to be

transferable from one PAH to another one[37,38]. Here, we choose the SE-D set of parameters suitable for use with the semi-empirical AM1 method because it has proven to give slightly more reliable results than the set of parameters suitable for use with the PM3 and MNDO methods (see Ref. [37]). However, the present study is not limited to the calculation of the interaction between PAHs and soot surface because it aims also at characterizing the oxidation of the adsorbed PAHs by the OH radical. We thus extend here the SE-D method to the calculations of the OH-PAH and OH-soot interactions, which are then written as

$$U_{\text{AM1-D}}^{\text{OH}} = U_{\text{AM1}}^{\text{OH}} - \sum_{i=1}^N \frac{1}{(1 + e^{\alpha^{\text{OH}}(R_0^{\text{OH}} - R_{i\text{O}})})} \times \frac{[C_{\text{O},i}^{(6)}]}{R_{i\text{O}}^6}, \quad (3)$$

where the semi-empirical calculations are performed at the AM1 level for the consistency with the calculations of the PAH-soot interactions. The sum over i includes the total number N of carbon atoms in the system considered (soot + PAH), and the $C_{\text{O},i}^{(6)}$ parameter for the oxygen-carbon interactions is taken from the literature[47]. Note that all the hydrogen atoms are neglected in the calculations of the OH-soot and OH-PAH interactions. **This assumption is based on the very weak contribution of these terms to the dispersion interactions in water-carbonaceous systems [48,49].** Determining the best values for the α^{OH} and R_0^{OH} parameters of the damping function is a delicate task which will be detailed below. All the parameters used in the present calculations are given in Table 1.

2.2 Energetics of the oxidation reaction

The mechanism of the oxidation reaction of PAH molecules by the OH radical is illustrated by the reaction scheme given in Figure 1.

In the first step of the reaction, a complex is formed between the reactants (the so-called pre-reactive complex, PRC) that, in the second step, transforms to the transition state (TS). Finally, the reaction results in the product that contains an sp^3 carbon atom and a π electron system with one missing electron. Defining the energies with respect to a reference state corresponding to the reactants far from each other, the PRC is located in an energy well (i.e., it corresponds to the negative energy E_1) while the TS corresponds to an energy barrier ($E_1 - E_2$) along the reaction path. Such a transition state formed with OH radical was found both theoretically and experimentally in the case of hydrocarbons[50], and aromatic hydrocarbons such as benzene[51–53], toluene[54] and phenol[55].

2.3 Kinetics of the oxidation reaction

The kinetics of the oxidation mechanism presented in Fig. 1 is governed by rate constants corresponding to the separate elementary reaction steps. The two first steps, schematized as

correspond to the formation of the PRC, characterized by the rate constant k_1 , and to the decay of the PRC to the reactants, governed by the rate con-

stant k_{-1} . Then, the formation of the product through the transition state is characterized by the rate constant k_2 as

Finally, it should be taken into account that the PRC can be quenched by collisions with neutral particles as,

This quenching step is characterized by the second order rate constant k_3 and M can be any neutral particle that does not experience any chemical transformation during the collision.

Then the global reaction rate for the oxidation process (i.e., the reaction rate for the formation of the product from the reactants) can be written in the following form:

$$r = \frac{d[\text{Product}]}{dt} = k_2[\text{PRC}] = k[\text{OH}][\text{PAH}]. \quad (7)$$

If we assume now that the PRC is in a quasi-steady state, then we arrive at the following expression for the total rate constant

$$k = \frac{k_1 k_2}{k_{-1} + k_2 + k_3[\text{M}]}. \quad (8)$$

We can make now two additional assumptions. First, we consider the existence of an equilibrium between the reactants and the PRC, such that the decay of

the PRC to reactants is much faster than the formation of the product, i.e.,

$$k_{-1} \gg k_2. \quad (9)$$

Moreover, under tropospheric conditions, the pressure is low enough so that the collisions with neutral particles are considerably rare events. We can thus assume that

$$k_2 \gg k_3[M]. \quad (10)$$

Finally, for the total rate constant, we obtain

$$k = k_2 \frac{k_1}{k_{-1}} = k_2 K, \quad (11)$$

where K is the equilibrium constant of the formation of the PRC. Note that we arrive at an expression similar to the one proposed by Atkinson and Cvetanovic for the characterization of the addition of O atoms to olefins[56].

2.4 Calculations of K and k_2

The canonical equilibrium constant K for a gas-phase process is given by

$$K = \frac{Q_{PRC}}{Q_{PAH}Q_{OH}} e^{-E_1/k_B T}, \quad (12)$$

where E_1 is the energy of the PRC with respect to the reference state (PAH + OH at an infinite distance from each other), T is the absolute temperature,

k_B is the Boltzmann constant, and Q_{PRC} , Q_{PAH} and Q_{OH} are the partition functions of the pre-reactive complex, the polycyclic aromatic hydrocarbon and the OH radical, respectively.

The reaction constant for the formation of the product according to the transition state (TST) theory is expressed as

$$k_2 = \frac{k_B T}{h} \frac{Q^\ddagger}{Q_{PRC}} e^{-(E_2 - E_1)/k_B T}, \quad (13)$$

where h is the Planck constant, E_2 is the energy of the transition state with respect to the reference state and $Q^\ddagger$ is the partition function of the transition state. According to Equation 11, the product of Equations 12 and 13 gives the total rate constant k

$$k = \frac{k_B T}{h} \frac{Q^\ddagger}{Q_{PAH} Q_{OH}} e^{-E_2/k_B T}, \quad (14)$$

expression in which E_1 no longer appears.

Because we are interested here in the modification of the rate constant k upon physisorption of the PAH on a carbonaceous particle modelling a soot surface, we rather choose to evaluate the ratio of the total rate constant of the oxidation in the gas phase to the one associated with the oxidation in the adsorbed phase, as

$$\frac{k^{ads}}{k^{gas}} = \frac{Q_{PAH}^{gas}}{Q_{PAH}^{ads}} \frac{Q_{OH}^{gas}}{Q_{OH}^{ads}} \frac{Q_{\ddagger,ads}^\ddagger}{Q_{\ddagger,gas}^\ddagger} e^{\frac{-(E_2^{ads} - E_2^{gas})}{k_B T}}. \quad (15)$$

3 Results and discussion

As a first application, we investigate here the details of the heterogeneous oxidation reaction of benzene adsorbed on a soot particle modelled by a large cluster of 80 carbon atoms arranged in fused benzene rings as in a graphene sheet. Note that, as in our previous studies[43–45], the dangling bonds of this cluster have been saturated with hydrogen atoms, and the cluster will thus be referred below as the $C_{80}H_{22}$ cluster. For these adsorbed species, the calculations have been performed with the AM1-D method.

3.1 Determination of the α and R_0 parameters for O-C interactions

First, we have determined the values of the α^{OH} and R_0^{OH} parameters of the damping function used for the calculations of the dispersion contributions to the AM1-D method (see Equation 3) in the following way. We performed AM1 calculations to characterize the PRC and the TS corresponding to the oxidation reactions of benzene by OH in the gas phase. The results, given in Table 2, show that the equilibrium distance for the PRC is larger than 3.0 Å, and that the equilibrium distance for the corresponding TS is equal to 2.08 Å. To set up our SE-D model, we can thus reasonably think that the dispersion interactions between the incoming OH and the reacting benzene molecule play a significant role above 3.0 Å only, and should vanish between 2.1 and 3.0 Å. This leads us to choose a R_0 value equal to 2.75 Å for the O–C interactions in the OH–benzene system. The corresponding value of the α parameter has been chosen accordingly to ensure a smooth removing of the dispersion interactions between 2.0 and 3.0 Å [38]. Note that the R_0 values

defined here are in agreement with values previously fitted in the literature on the basis of DFT calculations[52]. Note also that we will assume in the following that the parameters selected here for the O–C dispersion interactions are transferable to the calculations of the interactions between OH and soot.

3.2 Analysis of the OH+PAH energy profile

Here, we present the optimized geometries and adsorption energies of the PRC and TS corresponding to the oxidation of benzene by OH when the benzene molecule is adsorbed on the surface of a $C_{80}H_{22}$ cluster. Note that we have considered only the situation in which the OH radical comes from the gas phase even for the reaction taking place in the adsorbed phase (i.e., the OH radical arrives perpendicularly to the cluster surface). Indeed, preliminary calculations have shown that the OH radical is captured by the cluster when arriving parallel to its surface, such as the oxidation reaction cannot take place[38]. Moreover, the results obtained for the adsorbed species have also been compared with the results of the same kind of calculations performed on gas phase systems with both AM1 and AM1-D methods.

As an illustration of the obtained results, the optimized geometries of the PRC and TS are given in Fig. 2 for the benzene+OH system adsorbed on the $C_{80}H_{22}$ cluster. This figure shows that the OH radical approaches the benzene molecule along a direction perpendicular to a C–C bond, in a symmetric position with respect to the two C atoms. This PRC geometry is also found when performing the optimization for the gas phase system using both AM1-D and AM1(i.e., without the dispersion contribution) methods. Upon further approach, OH slightly rotates and deviates from its symmetric position, such

as the optimized TS geometry corresponds to the attachment of OH directly on one C atom of the benzene molecule. Similar features are calculated both for the gas phase and for the adsorbed phase systems, using both AM1 and AM1-D methods. Note that these geometries are very similar to those obtained from DFT calculations characterizing the oxidation reaction in the gas phase[52].

The energy values corresponding to these optimized geometries are given in Table 2 together with the O–C (nearest C atom) distances. First, the values given in Table 2 show that the energy values obtained with the method AM1-D **are algebraically lower than the corresponding AM1 values without any dispersion contribution. This result is not surprising since dispersion is an attractive interaction. Also, for the same reason, the O–C distances are shorter when using the AM1-D method, but only for the PRC**, showing the greater influence of the dispersion interactions on the PRC than on the TS geometries due to the damping function. Furthermore, **the energy values obtained for the adsorbed systems (with the AM1-D method) are algebraically lower than the energy values calculated for the corresponding systems in gas phase with the same method,** as a consequence of the attractive interaction between the adsorbed system and the soot surface which thus tends to stabilize the different steps of the oxidation reaction.

3.3 Kinetics of the oxidation reaction : ratio of the rate constants

Before calculating the different partition functions in Equation 15, we have characterized separately the various motions of the benzene molecule and of

the TS complex in the gas phase and on the soot surface.

As an illustration of the corresponding results, we give in Fig. 3 the energy curves obtained upon rotating the adsorbed benzene molecule around the z axis, perpendicular to the surface of the $C_{80}H_{22}$ cluster (Fig. 3a) and around the x axis parallel to this surface (Fig. 3b). The energy barriers for the rotational motion around the z axis (Fig. 3a) are three times smaller than the $k_B T$ value at room temperature, and, as a consequence this rotational motion can be considered as a free rotation in our calculations. In a similar way, Fig. 3b shows that the energy variations upon slightly tilting the admolecule around the x axis can be easily represented by considering the admolecule as a 1D harmonic oscillator. In fact, this detailed study shows that all the various motions of the adsorbed benzene molecule and TS can be described, in a first approach, either by free motions as in gas phase or by the rigid rotor and harmonic oscillator approximations. This leads to the following assumptions :

- the translational partition functions in the directions which are parallel to the $C_{80}H_{22}$ cluster surface (direction x and y) are the same in the adsorbed phase and in the gas phase, due to the very weak interaction potential corrugation of the cluster surface,
- for the same reason, the rotation around the z direction in the adsorbed phase can be approximated by a free rotor.
- by contrast, the translation in the z direction (i.e. perpendicular to the surface) as well as the rotations around the x and y axes are hindered due to the presence of the cluster surface and have to be treated as vibrational motions.

Moreover, on the basis of the energy calculations presented above, we can use the following additional approximations to calculate the ratio k^{ads}/k^{gas} :

- the OH radical can be considered as in gas phase, even if the reaction takes place in the adsorbed phase. This assumption is justified by the fact that an OH radical approaching the graphene sheet could be captured such as **the oxidation reaction cannot occur**[38]. Moreover, the OH radical approaches toward the PAH only from the gas phase above the PAH plane.
- the internal vibrational modes and the electronic states are the same in the adsorbed phase and in the gas phase for the benzene molecule and for the TS, because of the weak interaction with the soot surface characterizing a physisorption process.

Using these assumptions, it turns out that the partition function ratios become

$$\frac{Q_{PAH}^{gas}}{Q_{PAH}^{ads}} = \frac{Q_{trans,z}^{gas,PAH}}{Q_{tr_z \rightarrow vibr}^{ads,PAH}} \frac{Q_{rot}^{gas,PAH}}{Q_{rot_x \rightarrow vibr}^{ads,PAH} Q_{rot_y \rightarrow vibr}^{ads,PAH} Q_{rot_z}^{ads,PAH}}, \quad (16)$$

and

$$\frac{Q_{tr_z \rightarrow vibr}^{\ddagger,ads}}{Q_{trans,z}^{\ddagger,gas}} = \frac{Q_{tr_z \rightarrow vibr}^{\ddagger,ads}}{Q_{tr_z \rightarrow vibr}^{\ddagger,gas}} \frac{Q_{rot_x \rightarrow vibr}^{\ddagger,ads}}{Q_{rot_x \rightarrow vibr}^{\ddagger,gas}} \frac{Q_{rot_y \rightarrow vibr}^{\ddagger,ads}}{Q_{rot_y \rightarrow vibr}^{\ddagger,gas}} \frac{Q_{rot_z}^{\ddagger,ads}}{Q_{rot}^{\ddagger,gas}}. \quad (17)$$

Finally, reporting the above equations into Equation 15, we arrive at the following expression of the rate constants ratio,

$$\begin{aligned} \frac{k^{ads}}{k^{gas}} &= \frac{Q_{trans,z}^{gas,PAH}}{Q_{tr_z \rightarrow vibr}^{ads,PAH}} \frac{Q_{rot}^{gas,PAH}}{Q_{rot_x \rightarrow vibr}^{ads,PAH} Q_{rot_y \rightarrow vibr}^{ads,PAH} Q_{rot_z}^{ads,PAH}} \\ &\times \frac{Q_{tr_z \rightarrow vibr}^{\ddagger,ads}}{Q_{tr_z \rightarrow vibr}^{\ddagger,gas}} \frac{Q_{rot_x \rightarrow vibr}^{\ddagger,ads}}{Q_{rot_x \rightarrow vibr}^{\ddagger,gas}} \frac{Q_{rot_y \rightarrow vibr}^{\ddagger,ads}}{Q_{rot_y \rightarrow vibr}^{\ddagger,gas}} \frac{Q_{rot_z}^{\ddagger,ads}}{Q_{rot}^{\ddagger,gas}} e^{\frac{-(E_2^{ads} - E_2^{gas})}{k_B T}}. \end{aligned} \quad (18)$$

where the following analytical expressions, valid for 1D and 3D rotations, 1D translation and 1D harmonic vibration, respectively, can be used for the calculations of the partition functions:

$$Q_{transl}^{1D} = L \sqrt{\frac{mk_B T}{2\pi \hbar^2}}, \quad (19)$$

$$Q_{vibr} = \frac{1}{1 - e^{\frac{-h\nu}{k_B T}}}, \quad (20)$$

$$Q_{rot}^{1D} = \frac{1}{\sigma} \sqrt{\frac{8\pi k_B T}{\hbar^2}} I, \quad (21)$$

$$Q_{rot}^{3D} = \frac{8\pi^2}{\sigma} \left(\frac{k_B T}{2\pi \hbar^2} \right)^{\frac{3}{2}} \sqrt{I_1 I_2 I_3}. \quad (22)$$

In the above equations $\hbar$ is the Planck constant divided by 2π , ν is the vibrational frequency, and σ is the symmetry number of the rotation. L is the finite distance (of arbitrary large extension) along which the molecule of mass m is permitted to move. I is a 1D moment of inertia associated with the rotation axis defined in Equation 21 and I_1 , I_2 , I_3 are the three moments of inertia of a 3D rotor.

To obtain the vibrational frequencies of the various hindered rotational motions we tilted the given molecule around its equilibrium position. The rotations are performed by small angles around the x and y axis parallel to the soot surface and we calculated the energy in the tilted positions (but we did not optimized it). Then, the obtained energy values were fitted by a quadratic function:

$$E_{pot} = \frac{1}{2}k(x - x_0)^2 + a, \quad (23)$$

in which x denotes the tilt angle. The force constant k was then used for determining the frequency:

$$\nu = \frac{1}{2\pi} \sqrt{\frac{k}{I}}, \quad (24)$$

where I is the corresponding moment of inertia.

A similar procedure was repeated for the vibrational motion (i.e. hindered translational motion) along the z axis, but by replacing the moment of inertia by the mass of the admolecule in Equation 24.

The moment of inertia in the adsorbed phase was calculated around an axis perpendicular to the surface and passing through the center of mass of the admolecule. Note that this axis was considered as the z axis in our calculations.

The various constants corresponding to the different type of motions are collected in Table 3, and the partition functions calculated for the benzene molecule and the corresponding TS complex are given in Table 4. By using these values in Equation 18, we calculate that $\frac{k^{ads}}{k^{gas}} = 0.69$, indicating that the oxidation reaction of a benzene molecule by OH is slightly hindered when the molecule is adsorbed on a graphene sheet.

This result is not too surprising because the adsorption of the PAH on the graphene sheet prevents from the OH attack from one side of the PAH plane. Then, we expect from this simple argument that the rate constant should be more or less divided by a factor of two with respect to the reaction in gas

phase. Although this is a reductive reasoning, it gives some confidence on the application of our SE-D model to reactivity problems. Note that our model has been built to allow also the simulation of gas-surface processes on which the surface can carry some defects like Stone-Wales defects[57], in plane and edge atom vacancies[58]. Of course, the modification of the reactivity on a defective surface is expected to be very different and non predictable a priori with respect to the perfect surface analyzed here. But, in this latter case, the conclusion is in accordance with the results of our energy optimization process, (see above) which shows that the soot particle stabilizes the OH+benzene PRC and the corresponding TS with respect to the gas phase situation.

4 Conclusions

In the present paper, we have used the AM1-D method to characterize the oxidation by OH of a PAH molecule adsorbed on a soot surface modelled by a graphene-like cluster. This method is based on an electrostatic and induction contribution calculated at the SCF AM1 level associated with a sum of two-body dispersion terms of the $C^{(6)}/R^6$ form[37]. Indeed, the AM1-D is able to properly describe the interactions between large aromatic systems, and it can be used to study systems for which full *ab initio* calculations are prohibited because of their large size. As a first application, we have detailed the oxidation mechanism for benzene, which is the simplest aromatic molecule (although not strictly a PAH molecule!). We have thus compared the characteristics of the oxidation reaction for the adsorbed benzene with those of the corresponding reaction in the gas phase. The main conclusion of the present work is a clear inhibition of the oxidation process by the adsorption of the

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benzene molecule on the soot surface. This conclusion is in qualitative agreement with previous experimental observations, concerning, however, larger PAH molecules[21]. For a better comparison with these experimental results, further investigations devoted to naphthalene, phenanthrene and anthracene molecules are under consideration. However, the corresponding calculations are much more complex due to the presence of different non-equivalent carbon sites for the OH attachment in the oxidation mechanism. Moreover, the real surface of soot is certainly not free of defects, and it would be thus also important to characterize the oxidation reactions of PAH molecules adsorbed on defective carbonaceous surfaces.

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Table 1
Selected parameters for the dispersion contribution to the SE-D potential calculated with the semi-empirical AM1 method. The parameters $C_C^{(6)}$, $C_H^{(6)}$, and $C_{OC}^{(6)}$ are given in $\text{kJ mol}^{-1} \text{ \AA}^6$; α is given in $\text{\AA}^{-1}$ and R_0 in $\text{\AA}$.

benzene	
$C_C^{(6)}$	2207.94
$C_H^{(6)}$	48.6
$C_{OC}^{(6)}$	1923.51
α	3.96
R_0	2.68
α^{OH}	64.00
R_0^{OH}	2.75

Table 2

Comparison of the energy values and O–C distances obtained using the AM1 and AM1D methods. The energies are in kJ/mol while the distances in Å.

	PRC		TS		
	energy	d_{C-O}	energy	d_{C-O}	
AM1 gas phase ^a	-4.27	3.17	4.06	2.08	[a] AM1 calculations
AM1D gas phase	-12.1	2.81	1.26	2.09	
AM1D adsorbed phase	-13.9	2.81	-0.98	2.10	

lead to a gas phase TS energy slightly greater than zero i.e. TS lies above the reactants. The same is obtained when dispersion is included but with a much smaller magnitude. This result is proper to AM1 methodology applied to benzene molecule. Similar calculations on larger PAHs in the same conditions lead to small negative gas phase TS energies i.e. TS energy level is always below the energy of the reactants[38]. DFT and ab initio calculations on benzene and naphthalene show that the TS is also below the reactants, irrespective of the situation (gas-phase, with or without dispersion)[38,51,53]. This slight discrepancy between AM1 and more sophisticated methods in the case of benzene does not matter since benzene is considered here as a test molecule for our statistical approach explained further.

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Table 3

Molecular constants corresponding to the different type of motions

		PAH(Benzene)	TS(Benzene + OH)
Gas phase	Translation	$M = 1.29 \cdot 10^{-25} \text{ kg}$	$M = 1.58 \cdot 10^{-25} \text{ kg}$
		$I_1 = 29.5 \cdot 10^{-46} \text{ kg m}^2$	$I_1 = 41.2 \cdot 10^{-46} \text{ kg m}^2$
	Rotation	$I_2 = 14.8 \cdot 10^{-46} \text{ kg m}^2$	$I_2 = 32.1 \cdot 10^{-46} \text{ kg m}^2$
		$I_3 = 14.8 \cdot 10^{-46} \text{ kg m}^2$	$I_3 = 20.8 \cdot 10^{-46} \text{ kg m}^2$
		$\sigma = 12$	$\sigma = 1$
Adsorbed phase	Transl $\rightarrow$ Vibr	$M = 1.29 \cdot 10^{-25} \text{ kg}$	$M = 1.58 \cdot 10^{-25} \text{ kg}$
		$\nu = 1.57 \cdot 10^{12} \text{ s}^{-1}$	$\nu = 1.42 \cdot 10^{12} \text{ s}^{-1}$
	Rot _x $\rightarrow$ Vibr	$I_x = 14.8 \cdot 10^{-46} \text{ kg m}^2$	$I_x = 53.4 \cdot 10^{-46} \text{ kg m}^2$
		$\nu = 1.16 \cdot 10^{12} \text{ s}^{-1}$	$\nu = 1.44 \cdot 10^{12} \text{ s}^{-1}$
	Rot _y $\rightarrow$ Vibr	$I_y = 14.8 \cdot 10^{-46} \text{ kg m}^2$	$I_y = 26.6 \cdot 10^{-46} \text{ kg m}^2$
		$\nu = 1.17 \cdot 10^{12} \text{ s}^{-1}$	$\nu = 9.12 \cdot 10^{11} \text{ s}^{-1}$
	Rotation _z	$I_z = 29.5 \cdot 10^{-46} \text{ kg m}^2$	$I_z = 37.5 \cdot 10^{-46} \text{ kg m}^2$
		$\sigma = 6$	$\sigma = 1$

Table 4

Molecular partition functions of the different type of motions

		PAH(Benzene)	TS(Benzene + OH)
Gas phase	Translation	$8.73 \cdot 10^{10} \cdot L \text{ m}^{-1}$	$9.63 \cdot 10^{10} \cdot L \text{ m}^{-1}$
	Rotation	$7.53 \cdot 10^3$	$1.87 \cdot 10^5$
Adsorbed phase	Transl $\rightarrow$ Vibr	4.48	4.89
	Rot _x $\rightarrow$ Vibr	5.85	4.84
	Rot _y $\rightarrow$ Vibr	5.81	7.32
	Rotation _z	27.6	187

Fig. 1. Schematic representation of the oxidation reaction of PAH molecules by OH radical. The energy of the reactants (PAH + OH) is taken as the reference state for the definition of the energies. PRC and TS define the pre-reactive complex and the transition state, respectively.

Fig. 2. Side (top of the figure) and top (bottom of the figure) views of the geometry of (a) the PRC and (b) the TS obtained for the oxidation reaction by OH of an adsorbed benzene molecule, using AM1-D method. The C atoms of the benzene molecule are represented as black circles for clarity, whereas the C atoms of the graphite cluster are represented as grey circles. Dark grey and white circles represent the O and H atoms, respectively. Note that the nearest C–C distances between the benzene molecule and the surface is also indicated on the side views.

Fig. 3. Energy curves obtained upon rotating an adsorbed benzene molecule (a) around the z axis perpendicular to the surface of the $C_{80}H_{22}$ cluster and (b) around the x axis parallel to this surface. Note that the relative energy (in eV) is defined with respect to the maximum or the minimum of the energy curve. The angles are given in radian.

PAH + OH

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