Adsorption of Selected Ions on the Anatase TiO2 (101) Surface: A Density Functional Study
Jacek Piechota, Marta Kinga Bruska, Konrad Szacilowski

To cite this version:

HAL Id: hal-00515072
https://hal.archives-ouvertes.fr/hal-00515072
Submitted on 4 Sep 2010

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Adsorption of Selected Ions on the Anatase TiO2 (101) Surface: A Density Functional Study

<table>
<thead>
<tr>
<th>Journal:</th>
<th>Molecular Simulation/Journal of Experimental Nanoscience</th>
</tr>
</thead>
<tbody>
<tr>
<td>Manuscript ID:</td>
<td>GMOS-2008-0220.R1</td>
</tr>
<tr>
<td>Journal:</td>
<td>Molecular Simulation</td>
</tr>
<tr>
<td>Date Submitted by the Author:</td>
<td>26-Nov-2008</td>
</tr>
<tr>
<td>Complete List of Authors:</td>
<td>Piechota, Jacek; University of Warsaw, ICMM  Bruska, Marta; Jagiellonian University, Department of Chemistry  Szaciłowski, Konrad; Jagiellonian University, Department of Chemistry</td>
</tr>
<tr>
<td>Keywords:</td>
<td>titanium dioxide, adsorption, electronic structure, density functional theory</td>
</tr>
</tbody>
</table>

Note: The following files were submitted by the author for peer review, but cannot be converted to PDF. You must view these files (e.g. movies) online.

Bruska_Szacilowski_Piekota_TiO2_surface_figures.tar.gz
RESEARCH NOTE

Adsorption of Selected Ions on the Anatase TiO$_2$ (101) Surface: A Density Functional Study

Density functional calculations of adsorption of simple molecules (F$^-$ and OH$^-$ ions) on the TiO$_2$ anatase (101) surface have been performed. Changes to the electronic properties prior and after adsorption have been investigated. The most profound change in the electronic structure of the anatase surface after adsorption is the diminishing of the band gap of the system. While for the pure (without adsorbents) surface the band gap is 1.77 eV wide, for the modified surface with the F$^-$ and OH$^-$ ions the band gap widths equal to 0.35 eV and 0.39 eV, respectively. That means the excitation energy after adsorption is over four times smaller than in the case of pure system. Nevertheless, in all the cases studied the anatase surface maintains its semiconducting properties.

Keywords: titanium dioxide; adsorption; electronic structure; density functional theory

*Email:
RESEARCH NOTE

Adsorption of Selected Ions on the Anatase TiO$_2$ (101) Surface: A Density Functional Study

Marta Kinga Bruska $^a$, Konrad Szaciłowski $^a$, and Jacek Piechota $^b$*

$^a$Department of Chemistry, Jagiellonian University, Kraków, Poland; $^b$Interdisciplinary Centre for Materials Modelling, University of Warsaw, Warszawa, Poland

Density functional calculations of adsorption of simple molecules (F$^-$ and OH$^-$ ions) on the TiO$_2$ anatase (101) surface have been performed. Changes to the electronic properties prior and after adsorption have been investigated. The most profound change in the electronic structure of the anatase surface after adsorption is the diminishing of the band gap of the system. While for the pure (without adsorbents) surface the band gap is 1.77 eV wide, for the modified surface with the F$^-$ and OH$^-$ ions the band gap widths equal to 0.35 eV and 0.39 eV, respectively. That means the excitation energy after adsorption is over four times smaller than in the case of pure system. Nevertheless, in all the cases studied the anatase surface maintains its semiconducting properties.

Keywords: titanium dioxide; adsorption; electronic structure; density functional theory

*Email: jp@icm.edu.pl
1. Introduction

Surface-modified semiconductors have found numerous applications as (photo)catalysts, chemosensors and biomimetic light-harvesting antennae. Recently much attention has been focused on their capability of performing logic operations. The research in this field is stimulated by natural limits of classical, silicon-based electronics. Various types of electronic interactions between the surface modification and the semiconducting support control yield photocurrent generated upon visible-light irradiation and different efficiencies of the photosensitization effect.

Among many materials studied, titanium dioxide, TiO$_2$, has been a subject of extensive research both experimentally (see for instance [1-25]) and theoretically [26-36] over the last decades. The main reason for such intense interest in TiO$_2$ is the wide range of its industrial applications and the expectation that insight into properties gained on the fundamental, atomic level will help to improve materials and device performance.

Most of the traditional applications of TiO$_2$ exploit its very large dielectric constant and refractive index. TiO$_2$ is commonly used as a dielectric in electronic devices [37,38] and as an optical coating: anti-reflection films, interference filters or optical wave-guides [39,40]. It is widely used as non-toxic, white pigment in paints and cosmetic products [41], as corrosion-protective coatings and as a gas sensor [42-45]. It is also important in earth sciences, plays a role in the biocompatibility of bone implants [46] and in pure form it is used as a food additive [47]. Novel applications of TiO$_2$ are based on its surface and catalytic properties. Titanium dioxide is used in heterogeneous catalysis, electrochromic devices, as a photocatalyst, in solar cells for the production of hydrogen and electric energy [48]. The photoelectric and photochemical properties are especially interesting fields of research on TiO$_2$. Since about 1972 when Fujishima and Honda published their work on the photolysis of water on TiO$_2$ electrodes without any external bias [11], titanium dioxide has continued to hold a dominant position in photocatalysis [49-53]. The latest research investigates titania usage for photo-assisted degradation of organic molecules due to its semiconducting properties. Applications of this process range from purification of wastewaters [49], desinfection [54], self-cleaning coatings [55] or protective coatings against environmental damage [56] to therapy against tumour cells [57-59]. Semiconducting metal oxides may change their photocatalytic properties upon adsorption of chemical compounds. The TiO$_2$ modified surfaces are another focus of active research [16-20]. The nanocrystallite structures, quantum dots as well as nanorods and nanotubes made from titanium dioxide [21-25] can significantly improve catalytic properties of this material and give another topic to study around TiO$_2$. The newest possible application of TiO$_2$ is connected with miniaturization of electronics devices. Ultrathin titanium oxide films might be the gate material for replacing SiO$_2$ in MOSFET devices [60]. TiO$_2$ films doped with Co become ferromagnetic at room temperature. As they are optically transparent and semiconducting they may find application in spintronics [61]. It would be hard to find any other material with so many industrial applications and promising properties, especially photocatalytic ones, as TiO$_2$. It seems that science of TiO$_2$ surface will play key role in the future of high-tech industry. A comprehensive review of the properties of titanium dioxide surface has been given in [62].

Titanium dioxide occurs in nature as the well-known naturally occurring minerals rutile, anatase and brookite, of which the first two are used commercially. The most common form is rutile, which is also the most stable form [63]. Anatase and brookite both convert to rutile upon heating [63]. Rutile, anatase and brookite all contain six coordinate titanium. However, some recent ab initio calculations show that anatase is more stable than rutile at 0 K [31-32]. Furthermore, anatase is more efficient than rutile for several applications, including
photocatalysis [53], catalysis [64] and, especially, dye-sensitized solar cells [65,66]. In all these applications, surface properties are of major importance. However, while the surfaces of rutile have been extensively investigated [53,67] due to the limited availability of sufficiently large anatase single crystals the fundamental surface properties of this polymorph are still largely unexplored. Only very recently, thanks to improved sample preparation techniques, have experimental studies of well defined anatase surfaces started to appear [68,69].

Motivated by these advances we have carried out an extensive first-principles investigation of the structure and energetics of the TiO$_2$ (101) anatase surface prior and after adsorption of simple molecules, namely the F$^-$ and OH$^-$ ions. The (101) surface is the most thermodynamically stable and the one mainly exposed in the TiO$_2$ anatase crystals [70]. It constitutes more than 94% of the crystal surface. To our best knowledge this is the first report on the properties of the TiO$_2$ (101) anatase surface modified with the F$^-$ and OH$^-$ ions. However, the present work constitutes continuation of our earlier interest in *ab initio* modelling of oxide compounds [71-75].

The rest of the paper is organized as follows. Computational details are reported in Section 2. In Section 3 the geometrical considerations are presented and band structures with densities of states are analyzed. In Section 4 the main points of this work are summarized and perspectives for future research are outlined.

2. Computational details

2.1. General settings

The calculations performed in this study were done using the VASP package [76] as implemented in MedeA environment [77]. VASP evaluates the total energy of periodically repeated geometries, on the basis of density functional theory (DFT) and the pseudopotential approximation. The electron-ion interaction is described by projected augmented waves [78,79]. Periodic boundary conditions are used, with the one-electron pseudo-orbitals expanded over a plane-wave basis set. The expansion includes all plane-waves whose kinetic energy is defined as $\hbar^2k^2/2m < E_{\text{cut}}$, where $k$ is the wave vector, $m$ the electronic mass, and $E_{\text{cut}}$ the chosen cut-off energy. Calculations were performed using spin-unrestricted generalized gradient approximation (GGA) density functional theory, which used PBE exchange correlation functional [80]. All energies are extrapolated to a temperature of $T = 0$ K.

2.1. Settings for bulk TiO$_2$

Several tests have been initially performed to verify the accuracy of the method when applied to bulk TiO$_2$, as well as to clarify different technical aspects of the calculations, such as the optimum pseudopotentials and sampling of the Brillouin zone.

For bulk rutile and anatase phases, using the energy cut-off of 550 eV and the k-spacing of 0.3 Å (corresponding to k-meshes of 8x8x8 and 5x5x8 for anatase and rutile, respectively) we have tested for convergence, using different sets of pseudopotentials and sampling schemes of the Brillouin zone. Calculations were performed with standard set of pseudopotentials [76], but additional run was done with semi-core states pseudopotentials which treat 3s titanium states and higher ones as valence states, as well as with hard pseudopotentials for oxygen. Sampling of the Brillouin zone was performed using the Monkhorst-Pack scheme [81]. To minimize the errors in
the Hellmann-Feynman forces due to the entropic contribution of the electronic free energy we have used as the integration scheme the Methfessel-Paxton technique [82] with a smearing of $\sigma = 0.2$ eV, as well as in another calculation tetrahedron with Blöchl correction technique [83]. In all cases the total energy was converged to $10^{-5}$ eV. The changes in the accuracy of the final results were negligible, indicating that the convergence with respect to the basis set and k-spacing is ensured.

2.2. Settings for the TiO$_2$ (101) anatase surface

The TiO$_2$ (101) anatase surface is represented by a slab model with periodic boundary conditions applied in all three directions. Because the supercell (slab) representing the surface is much larger than the unit cell of bulk TiO$_2$, for the purpose of the present study the surface was modelled with less computationally demanding input parameters than those used in the calculations of the bulk. All the calculations were performed with standard set of pseudopotentials with a plane-wave basis cut-off energy of 400 eV. Sampling of the Brillouin zone was performed using a Monkhorst-Pack scheme [81] with the k-mesh of $2 \times 2 \times 1$; the k-mesh was centred at the $\Gamma$-point of the Brillouin zone. The first order Methfessel-Paxton smearing with a width of 0.2 eV was used as the integration scheme [82].

The slab used in computations contained 24 atoms which build the first layer of the (101) anatase surface - see Figure 1(a) - with 10 Å of vacuum above the surface. Two different titanium sites with fivefold Ti(5) and sixfold Ti(6) coordinated titanium as well as twofold O(2) and threefold O(3) coordinated oxygen can be distinguished at this surface. As electrophilic Ti(5) centres are easy accessible for adsorbents, they were preferably covered in the course of calculations. For the modified structures two of F$^-$ (or respectively OH$^-$) ions were placed 2 Å above the Ti(5) centres and one oxygen vacancy was made to keep the system neutral in charge – see Figure 1(b) for the F$^-$ adsorption and Figure 1(c) for the OH$^-$ adsorption, respectively.

All the calculations have been performed for the non-relaxed cleaved crystal structure with the same bond distances as obtained in bulk calculations. One may claim that the slab used in computations is only a rough approximation to realistic description of the true system. However, the discrepancies introduced by insufficient size of the supercell are systematic, so that main trends in properties of modified surfaces can still be traced. The size reduction of the system under investigation was necessary to complete all the calculations in a reasonable time.

In order to report calculated results in a way consistent with other reports we have applied following definitions and formulae. The surface energy is defined as:

$$E_{\text{surface}} = \frac{1}{2} \left( E_{\text{slab}} - N \cdot E_{\text{bulk}} \right)/A_{\text{surface}},$$  \hspace{1cm} (1)

where $E_{\text{slab}}$ is the total energy of the slab, $N$ is the total number of TiO$_2$ units in the slab, $E_{\text{bulk}}$ is the total energy of the TiO$_2$ unit in the bulk anatase phase, and $A_{\text{surface}}$ is the total exposed area of the slab.

3. Results and discussion

3.1. Bulk TiO$_2$

Calculated lattice parameters of the rutile and anatase structures in comparison to results of neutron diffraction at the temperature of 15K as listed in Ref. [6] are presented in Table 1. The
calculated lattice parameters are in good agreement with experimental values. The discrepancies are not higher than 1.6% over the experimental values for rutile and 1.0% for anatase, what is within the typical error of DFT in calculating the lattice constants of bulk materials. Note that these computed lattice parameters are generally overestimated with respect to experimental values, what is typical for the GGA approximation.

3.2. Non-modified TiO$_2$ (101) anatase surface

As mentioned above, the (101) anatase surface is the most thermodynamically stable and the one mainly exposed in the TiO$_2$ anatase crystals [70]. The distance between two adjoining fivefold coordinated titanium Ti(5) centres is 3.82 Å and the range between the neighbouring Ti(6) centres is 5.55 Å – see Figure 1. The calculated surface energy (Eq. 1) is 1.02 J/m$^2$, which is close to the energy of the unrelaxed anatase (101) surface of 1.28 J/m$^2$ computed by Lazzeri et al. [84].

Calculated band structure along the symmetry lines of the first Brillouin zone for anatase (101) surface is plotted in Figure 2(a), together with corresponding density of states (DOS) – see Figure 2(b). Partial densities of states (PDOS) are shown in Figures 2(c)-(e). Zero in the energy scale corresponds to the Fermi level. The Fermi level is situated at the top of the valence band. This indicates the non-metallic properties of the material. The band gap is indirect, with the bottom of the conduction band at the Γ-point and the top of the valence band at the B-point. The width of this band gap equals to 1.77 eV. However, the energy of the valence band at the Γ-point is only 0.25 eV lower than the top of the valence band. Thus one can still think about the material as a direct band gap semiconductor. Similarly to previously reported bulk calculations [30,31], the band gap is underestimated. The DFT approaches often fail to describe experimental band gap for insulators and semiconductors. Another unphysical result from the calculation is slightly negative DOS values for oxygen orbitals. This error can be attributed to the insufficient k-point sampling in the course of the computation. It can be considered as numerical artefact and does not perturb general trends in the obtained results.

The valence electrons are distributed over two bands. The lower valence band lying just below -15.00 eV is 2.71 eV wide and contains mainly O 2s functions. The upper valence band is composed of O 2p orbitals mixed with some contribution from Ti 3d functions and is 5.12 eV wide. The conduction band originates mainly from the Ti 3d orbitals, but one can find a small O 2p character as well. The hybridization between O 2p and Ti 3d in both the conduction and upper valence bands indicates strong interactions between Ti and O atoms. As the result the excitation across the band gap involves both O 2p and Ti 3d states.

Integration of the total DOS up to the Fermi level gives the total number of electrons in Ti 3d, Ti 4s, O 2p and O 2s orbitals in the supercell. As there are 8 TiO$_2$ units in the supercell, the total number of electrons is equal to 128 as depicted in Figure 2(f).

3.3. Modified surfaces

3.3.1. F$^-$ adsorption

Calculated band structure along the symmetry lines of the first Brillouin zone for anatase (101) surface with the F$^-$ ions adsorbed is plotted in Figure 3(a), together with corresponding DOS – see Figure 3(b). Partial densities of states are shown in Figures 3(c)-(g).
In contrast to non-modified surface, for the F$^-$ adsorption the Fermi level is situated in the middle of the band gap. The predicted band gap is 0.35 eV wide. The valence electrons are distributed over three bands. The additional valence band, as compared to non-modified surface, is centred at -20.09 eV and originates from F 2s states. The subsequent band, as seen from the bottom of the band structure is 3.40 eV wide and corresponds to O 2s functions. The upper valence band is 5.90 eV wide and beside O 2p orbitals and some contribution from Ti 3d functions contains 2p orbitals from fluorine ions. The conduction band is still composed mainly of Ti 3d orbitals with a small O 2p character, but in this case the band is splitted into two subbands. The interaction with fluorine energy levels is taking place here. The hybridization between O 2p and Ti 3d is enriched with contribution coming from fluorine orbitals in both the conduction and valence bands. There are interactions between F ions and Ti and O atoms. When the fluorine ions are adsorbed on the anatase surface the excitation across the band gap involves O 2p, Ti 3d as well as F 2p states.

3.3.2. OH$^-$ adsorption

Calculated band structure along the symmetry lines of the first Brillouin zone for anatase (101) surface with the OH$^-$ ions adsorbed is plotted in Figure 4(a), together with corresponding (DOS) – see Figure 4(b). Partial densities of states are shown in Figures 4(c)-(g).

Similarly as for the F$^-$ adsorption, for the OH$^-$ adsorption the Fermi level is also situated in the middle of the band gap. The predicted band gap is 0.39 eV wide. The lowest valence band contains mainly O 2s functions. The upper valence band is composed of O 2p orbitals and small contribution from Ti 3d functions. It is characterized by the highest width from all the presented systems, as its value equals to 6.09 eV. The conduction band is splitted into two subbands like in the system with the fluorine ions, but still it is composed mainly from Ti 3d orbitals with a small contribution from O 2p functions. Similarly as for the F$^-$ adsorption one can see in this case the interaction of the TiO$_2$ slab levels with adsorbent orbitals. The hybridization between O 2p and Ti 3d after adsorption is stronger than in the case of the non-modified surface. The OH$^-$ ions enhance interactions of the O 2p and Ti 3d orbitals especially in the valence region. The excitation across the band gap involves O 2p and Ti 3d states, but the O 2p orbitals are more important than it was in the model of the non-modified surface.

4. Summary and outlook

Band structures and densities of states were computed for non-modified TiO$_2$ (101) anatase surface and for anatase surfaces with the F$^-$ and OH$^-$ ions adsorbed. From decomposition of the total DOS into partial DOS, more detailed information about the ion-surface interactions was gained.

The most important changes in the electronic structure of anatase surface after adsorption is the diminishing of the band gap. The excitation energy after adsorption is over four times lower. However, after adsorption the system still preserves its semiconducting properties. TiO$_2$ is a compound mostly ionic in character and hybridization effects are not expected to be common in this case, especially in interaction with ions. This can be easily visible in the band structures which are flat in all the three cases studied. Some mixing of O 2p and Ti 3d orbitals has occurred as well as small hybridizations of the ions and orbitals of the surface atoms (O 2p, Ti 3d, F 2p).
As the result the excitation across the band gap involves all states: O 2p, Ti 3d, and F 2p when present.

To understand better relevant photocatalytic properties of the modified anatase surfaces it is necessary to carry out more accurate computations. More precise results for DOS will allow to make a reasonable integration of the partial DOS that gives total percentage of the given orbital that is occupied at a specified energy level. This provides information about electron transfer processes that is important for photocatalysis. The crystal orbital overlap populations from more accurate band structures are expected to give detailed information about bond formation.

The results obtained indicate that the systems under investigation constitute an interesting topic for further studies.

Bibliography


[77] Information available at: http://www.materialsdesign.com/


List of Figures

Figure 1. The structure of the stoichiometric TiO$_2$ anatase (101) surface. (a) non-modified; (b) with F$^-$ adsorbents; (c) with OH$^-$ adsorbents.

Figure 2. Electronic structure of the non-modified TiO$_2$ anatase (101) surface. (a) band structure (G stands for Γ-point); (b) total DOS; (c) PDOS for Ti 3d orbitals; (d) PDOS for O 2p orbitals; (e) PDOS for O 2s orbitals; (f) Integrated total DOS.

Figure 3. Electronic structure of the TiO$_2$ anatase (101) surface with F$^-$ adsorbents. (a) band structure (G stands for Γ-point); (b) total DOS; (c) PDOS for Ti 3d orbitals; (d) PDOS for O 2p orbitals; (e) PDOS for O 2s orbitals; (f) PDOS for F 2p orbitals; (g) PDOS for F 2s orbitals.

Figure 4. Electronic structure of the TiO$_2$ anatase (101) surface with OH$^-$ adsorbents. (a) band structure (G stands for Γ-point); (b) total DOS; (c) PDOS for Ti 3d orbitals; (d) PDOS for O 2p orbitals; (e) PDOS for O 2s orbitals; (f) PDOS for O (from OH groups) 2p orbitals; (g) PDOS for O (from OH groups) 2s orbitals.
List of Tables

Table 1. Lattice parameters in [Å] of the rutile and anatase TiO$_2$ structures.
Table 1. Lattice parameters in [Å] of the rutile and anatase structures.

<table>
<thead>
<tr>
<th>Structure</th>
<th>Lattice parameter</th>
<th>Present work</th>
<th>Experiment$^a$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rutile</td>
<td>a 4.661</td>
<td>4.587</td>
<td></td>
</tr>
<tr>
<td></td>
<td>c 2.969</td>
<td>2.954</td>
<td></td>
</tr>
<tr>
<td></td>
<td>c/a 0.637</td>
<td>0.644</td>
<td></td>
</tr>
<tr>
<td>Anatase</td>
<td>a 3.822</td>
<td>3.782</td>
<td></td>
</tr>
<tr>
<td></td>
<td>c 9.690</td>
<td>9.502</td>
<td></td>
</tr>
<tr>
<td></td>
<td>c/a 2.535</td>
<td>2.535</td>
<td></td>
</tr>
</tbody>
</table>

$^a$ Ref. [6]
Density functional calculations of adsorption of the F\(^-\) and OH\(^-\) ions on the TiO\(_2\) anatase (101) surface have been performed. Changes to the electronic properties prior and after adsorption have been investigated. The most profound change in the electronic structure of the anatase surface after adsorption is the diminishing of the band gap of the system. While for the pure (without adsorbents) surface the band gap is 1.77 eV wide, for the modified surface with the F\(^-\) and OH\(^-\) ions the band gap widths equal to 0.35 eV and 0.39 eV, respectively. That means the excitation energy after adsorption is over four times smaller than in the case of pure system. Nevertheless, in all the cases studied the anatase surface maintains its semiconducting properties.

**Keywords:** titanium dioxide; adsorption; electronic structure; density functional theory

*Email:*
Density functional calculations of adsorption of the \( \text{F}^- \) and \( \text{OH}^- \) ions on the \( \text{TiO}_2 \) anatase (101) surface have been performed. Changes to the electronic properties prior and after adsorption have been investigated. The most profound change in the electronic structure of the anatase surface after adsorption is the diminishing of the band gap of the system. While for the pure (without adsorbents) surface the band gap is 1.77 eV wide, for the modified surface with the \( \text{F}^- \) and \( \text{OH}^- \) ions the band gap widths equal to 0.35 eV and 0.39 eV, respectively. That means the excitation energy after adsorption is over four times smaller than in the case of pure system. Nevertheless, in all the cases studied the anatase surface maintains its semiconducting properties.

**Keywords:** titanium dioxide; adsorption; electronic structure; density functional theory

*Email: jp@icm.edu.pl*
1. Introduction

Surface-modified semiconductors have found numerous applications as (photo)catalysts, chemosensors and biomimetic light-harvesting antennae. Recently much attention has been focused on their capability of performing logic operations. The research in this field is stimulated by natural limits of classical, silicon-based electronics. Various types of electronic interactions between the surface modification and the semiconducting support control yield photocurrent generated upon visible-light irradiation and different efficiencies of the photosensitization effect.

Among many materials studied, titanium dioxide, TiO$_2$, has been a subject of extensive research both experimentally (see for instance [1-25]) and theoretically [26-36] over the last decades. The main reason for such intense interest in TiO$_2$ is the wide range of its industrial applications and the expectation that insight into properties gained on the fundamental, atomic level will help to improve materials and device performance.

Most of the traditional applications of TiO$_2$ exploit its very large dielectric constant and refractive index. TiO$_2$ is commonly used as a dielectric in electronic devices [37,38] and as an optical coating: anti-reflection films, interference filters or optical wave-guides [39,40]. It is widely used as non-toxic, white pigment in paints and cosmetic products [41], as corrosion-protective coatings and as a gas sensor [42-45]. It is also important in earth sciences, plays a role in the biocompatibility of bone implants [46] and in pure form it is used as a food additive [47]. Novel applications of TiO$_2$ are based on its surface and catalytic properties. Titanium dioxide is used in heterogeneous catalysis, electrochromic devices, as a photocatalyst, in solar cells for the production of hydrogen and electric energy [48]. The photoelectric and photochemical properties are especially interesting fields of research on TiO$_2$. Since about 1972 when Fujishima and Honda published their work on the photolysis of water on TiO$_2$ electrodes without any external bias [11], titanium dioxide has continued to hold a dominant position in photocatalysis [49-53]. The latest research investigates titania usage for photo-assisted degradation of organic molecules due to its semiconductor properties. Applications of this process range from purification of wastewaters [49], disinfection [54], self-cleaning coatings [55] or protective coatings against environmental damage [56] to therapy against tumour cells [57-59]. Semiconducting metal oxides may change their photocatalytic properties upon adsorption of chemical compounds. The TiO$_2$ modified surfaces are another focus of active research [16-20]. The nanocrystallite structures, quantum dots as well as nanorods and nanotubes made from titanium dioxide [21-25] can significantly improve catalytic properties of this material and give another topic to study around TiO$_2$. The newest possible application of TiO$_2$ is connected with miniaturization of electronics devices. Ultrathin titanium oxide films might be the gate material for replacing SiO$_2$ in MOSFET devices [60]. TiO$_2$ films doped with Co become ferromagnetic at room temperature. As they are optically transparent and semiconducting they may find application in spintronics [61]. It would be hard to find any other material with so many industrial applications and promising properties, especially photocatalytic ones, as TiO$_2$. It seems that science of TiO$_2$ surface will play key role in the future of high-tech industry. A comprehensive review of the properties of titanium dioxide surface has been given in [62].

Titanium dioxide occurs in nature as the well-known naturally occurring minerals rutile, anatase and brookite, of which the first two are used commercially. The most common form is rutile, which is also the most stable form [63]. Anatase and brookite both convert to rutile upon heating [63]. Rutile, anatase and brookite all contain six coordinate titanium. However, some recent ab initio calculations show that anatase is more stable than rutile at 0 K [31-32]. Furthermore, anatase is more efficient than rutile for several applications, including
photocatalysis [53], catalysis [64] and, especially, dye-sensitized solar cells [65,66]. In all these applications, surface properties are of major importance. However, while the surfaces of rutile have been extensively investigated [53,67] due to the limited availability of sufficiently large anatase single crystals the fundamental surface properties of this polymorph are still largely unexplored. Only very recently, thanks to improved sample preparation techniques, have experimental studies of well defined anatase surfaces started to appear [68,69].

Motivated by these advances we have carried out an extensive first-principles investigation of the structure and energetics of the TiO$_2$ (101) anatase surface prior and after adsorption of the F$^-$ and OH$^-$ ions. The (101) surface is the most thermodynamically stable and the one mainly exposed in the TiO$_2$ anatase crystals [70]. It constitutes more than 94% of the crystal surface. To our best knowledge this is the first report on the properties of the TiO$_2$ (101) anatase surface modified with the F$^-$ and OH$^-$ ions. However, the present work constitutes continuation of our earlier interest in \textit{ab initio} modelling of oxide compounds [71-75].

The rest of the paper is organized as follows. Computational details are reported in Section 2. In Section 3 the geometrical considerations are presented and band structures with densities of states are analyzed. In Section 4 the main points of this work are summarized and perspectives for future research are outlined.

2. Computational details

2.1. General settings

The calculations performed in this study were done using the VASP package [76] as implemented in MedeA environment [77]. VASP evaluates the total energy of periodically repeated geometries, on the basis of density functional theory (DFT) and the pseudopotential approximation. The electron-ion interaction is described by projected augmented waves [78,79]. Periodic boundary conditions are used, with the one-electron pseudo-orbitals expanded over a plane-wave basis set. The expansion includes all plane-waves whose kinetic energy is defined as $\hbar^2 k^2/2m < E_{\text{cut}}$, where $k$ is the wave vector, $m$ the electronic mass, and $E_{\text{cut}}$ the chosen cut-off energy. Calculations were performed using spin-unrestricted generalized gradient approximation (GGA) density functional theory, which used PBE exchange correlation functional [80]. All energies are extrapolated to a temperature of $T = 0$ K.

2.1. Settings for bulk TiO$_2$

Several tests have been initially performed to verify the accuracy of the method when applied to bulk TiO$_2$, as well as to clarify different technical aspects of the calculations, such as the optimum pseudopotentials and sampling of the Brillouin zone.

For bulk rutile and anatase phases, using the energy cut-off of 550 eV and the k-spacing of 0.3 Å$^{-1}$ (corresponding to k-meshes of 8×8×8 and 5×5×8 for anatase and rutile, respectively) we have tested for convergence, using different sets of pseudopotentials and sampling schemes of the Brillouin zone. Calculations were performed with standard set of pseudopotentials [76], but additional run was done with semi-core states pseudopotentials which treat 3s titanium states and higher ones as valence states, as well as with hard pseudopotentials for oxygen. Sampling of the Brillouin zone was performed using the Monkhorst-Pack scheme [81]. To minimize the errors in the Hellmann-Feynman forces due to the entropic contribution of the electronic free energy we
have used as the integration scheme the Methfessel-Paxton technique [82] with a smearing of \( \sigma = 0.2 \) eV, as well as in another calculation tetrahedron with Blöchl correction technique [83]. In all cases the total energy was converted to \( 10^{-5} \) eV. The changes in the accuracy of the final results were negligible, indicating that the convergence with respect to the basis set and k-spacing is ensured.

### 2.2. Settings for the TiO\(_2\) (101) anatase surface

The TiO\(_2\) (101) anatase surface is represented by a slab model with periodic boundary conditions applied in all three directions. Because the supercell (slab) representing the surface is much larger than the unit cell of bulk TiO\(_2\), for the purpose of the present study the surface was modelled with less computationally demanding input parameters than those used in the calculations of the bulk. All the calculations were performed with standard set of pseudopotentials with a plane-wave basis cut-off energy of 400 eV. Sampling of the Brillouin zone was performed using a Monkhorst-Pack scheme [81] with the k-mesh of 2\( \times \)2\( \times \)1; the k-mesh was centred at the \( \Gamma \)-point of the Brillouin zone. The first order Methfessel-Paxton smearing with a width of 0.2 eV was used as the integration scheme [82].

The slab used in computations contained 24 atoms which build the first layer of the (101) anatase surface - see Figure 1(a) - with 10 Å of vacuum above the surface. Two different titanium sites with fivefold Ti(5) and sixfold Ti(6) coordinated titanium as well as twofold O(2) and threefold O(3) coordinated oxygen can be distinguished at this surface. As electrophilic Ti(5) centres are easy accessible for adsorbents, they were preferably covered in the course of calculations. For the modified structures two of F\(^-\) (or respectively OH\(^-\)) ions were placed 2 Å above the Ti(5) centres and one oxygen vacancy was made to keep the system neutral in charge – see Figure 1(b) for the F\(^-\) adsorption and Figure 1(c) for the OH\(^-\) adsorption, respectively.

All the calculations have been performed for the non-relaxed cleaved crystal structure with the same bond distances as obtained in bulk calculations. One may claim that the slab used in computations is only a rough approximation to realistic description of the true system. However, the discrepancies introduced by insufficient size of the supercell are systematic, so that main trends in properties of modified surfaces can still be traced. The size reduction of the system under investigation was necessary to complete all the calculations in a reasonable time.

In order to report calculated results in a way consistent with other reports we have applied following definitions and formulae. The surface energy is defined as:

\[
E_{\text{surface}} = \frac{(E_{\text{slab}} - N \cdot E_{\text{bulk}})}{A_{\text{surface}}} \tag{1}
\]

where \( E_{\text{slab}} \) is the total energy of the slab, \( N \) is the total number of TiO\(_2\) units in the slab, \( E_{\text{bulk}} \) is the total energy of the TiO\(_2\) unit in the bulk anatase phase, and \( A_{\text{surface}} \) is the total exposed area of the slab.

### 3. Results and discussion

#### 3.1. Bulk TiO\(_2\)

Calculated lattice parameters of the rutile and anatase structures in comparison to results of neutron diffraction at the temperature of 15K as listed in Ref. [6] are presented in Table 1. The calculated lattice parameters are in good agreement with experimental values. The discrepancies
are not higher than 1.6% over the experimental values for rutile and 1.0% for anatase, what is
within the typical error of DFT in calculating the lattice constants of bulk materials. Note that
these computed lattice parameters are generally overestimated with respect to experimental
values, typical for the GGA approximation.

3.2. Non-modified TiO$_2$ (101) anatase surface

As mentioned above, the (101) anatase surface is the most thermodynamically stable and the one
mainly exposed in the TiO$_2$ anatase crystals [70]. The distance between two adjoining fivefold
coordinated titanium Ti(5) centres is 3.82 Å and the range between the neighbouring Ti(6)
centres is 5.55 Å – see Figure 1. The calculated surface energy (Eq. 1) is 1.02 J/m$^2$, close to the
energy of the unrelaxed anatase (101) surface of 1.28 J/m$^2$ computed by Lazzeri et al. [84].

Calculated band structure along the symmetry lines of the first Brillouin zone for anatase
(101) surface is plotted in Figure 2(a), together with corresponding density of states (DOS) – see
Figure 2(b). Partial densities of states (PDOS) are shown in Figures 2(c)-(e). Zero in the energy
scale corresponds to the Fermi level. The Fermi level is situated at the top of the valence band.
This indicates the non-metallic properties of the material. The band gap is indirect, with the
bottom of the conduction band at the Γ-point and the top of the valence band at the B-point. The
width of this band gap equals to 1.77 eV. However, the energy of the valence band at the Γ-point
is only 0.25 eV lower than the top of the valence band. Thus one can still think about the material
as a direct band gap semiconductor. Similarly to previously reported bulk calculations [30,31],
the band gap is underestimated. The DFT approaches often fail to describe experimental band gap
for insulators and semiconductors. Another unphysical result from the calculation is slightly
negative DOS values for oxygen orbitals. This error can be attributed to the insufficient k-point
sampling in the course of the computation. It can be considered as numerical artefact and does
not perturb general trends in the obtained results.

The valence electrons are distributed over two bands. The lower valence band lying just
below -15.00 eV is 2.71 eV wide and contains mainly O 2s functions. The upper valence band is
composed of O 2p orbitals mixed with some contribution from Ti 3d functions and is 5.12 eV
wide. The conduction band originates mainly from the Ti 3d orbitals, but one can find a small
O 2p character as well. The hybridization between O 2p and Ti 3d in both the conduction and
upper valence bands indicates strong interactions between Ti and O atoms. As the result the
excitation across the band gap involves both O 2p and Ti 3d states.

Integration of the total DOS up to the Fermi level gives the total number of electrons in
Ti 3d, Ti 4s, O 2p and O 2s orbitals in the supercell. As there are 8 TiO$_2$ units in the supercell, the
total number of electrons is equal to 128 as depicted in Figure 2(f).

3.3. Modified surfaces

3.3.1. F$^-$ adsorption

Calculated band structure along the symmetry lines of the first Brillouin zone for anatase (101)
surface with the F$^-$ ions adsorbed is plotted in Figure 3(a), together with corresponding DOS – see Figure 3(b). Partial densities of states are shown in Figures 3(c)-(g).

In contrast to non-modified surface, for the F$^-$ adsorption the Fermi level is situated in the
middle of the band gap. The predicted band gap is 0.35 eV wide. The valence electrons are
distributed over three bands. The additional valence band, as compared to non-modified surface,
is centred at -20.09 eV and originates from F 2s states. The subsequent band, as seen from the bottom of the band structure is 3.40 eV wide and corresponds to O 2s functions. The upper valence band is 5.90 eV wide and beside O 2p orbitals and some contribution from Ti 3d functions contains 2p orbitals from fluorine ions. The conduction band is still composed mainly of Ti 3d orbitals with a small O 2p character, but in this case the band is splitted into two subbands. The interaction with fluorine energy levels is taking place here. The hybridization between O 2p and Ti 3d is enriched with contribution coming from fluorine orbitals in both the conduction and valence bands. There are interactions between F ions and Ti and O atoms. When the fluorine ions are adsorbed on the anatase surface the excitation across the band gap involves O 2p, Ti 3d as well as F 2p states.

3.3.2. OH\(^-\) adsorption

Calculated band structure along the symmetry lines of the first Brillouin zone for anatase (101) surface with the OH\(^-\) ions adsorbed is plotted in Figure 4(a), together with corresponding (DOS) – see Figure 4(b). Partial densities of states are shown in Figures 4(c)-(g).

As for the F\(^-\) adsorption, for the OH\(^-\) adsorption the Fermi level is also situated in the middle of the band gap. The predicted band gap is 0.39 eV wide. The lowest valence band contains mainly O 2s functions. The upper valence band is composed of O 2p orbitals and small contribution from Ti 3d functions. It is characterized by the highest width from all the presented systems, as its value equals to 6.09 eV. The conduction band is splitted into two subbands like in the system with the fluorine ions, but still it is composed mainly from Ti 3d orbitals with a small contribution from O 2p functions. As for the F\(^-\) adsorption one can see in this case the interaction of the TiO\(_2\) slab levels with adsorbent orbitals. The hybridization between O 2p and Ti 3d after adsorption is stronger than in the case of the non-modified surface. The OH\(^-\) ions enhance interactions of the O 2p and Ti 3d orbitals especially in the valence region. The excitation across the band gap involves O 2p and Ti 3d states, but the O 2p orbitals are more important than they were in the model of the non-modified surface.

4. Summary and outlook

Band structures and densities of states were computed for unrelaxed non-modified TiO\(_2\) (101) anatase surface and for anatase surfaces with the F\(^-\) and OH\(^-\) ions adsorbed. From decomposition of the total DOS into partial DOS, more detailed information about the ion-surface interactions was gained. The most important changes in the electronic structure of anatase surface after adsorption is the diminishing of the band gap. The excitation energy after adsorption is over four times lower. However, after adsorption the system still preserves its semiconducting properties. TiO\(_2\) is a compound mostly ionic in character and hybridization effects are not expected to be common in this case, especially in interaction with ions. This can be easily visible in the band structures which are flat in all the three cases studied. Some mixing of O 2p and Ti 3d orbitals has occurred as well as small hybridizations of the ions and orbitals of the surface atoms (O 2p, Ti 3d, F 2p). As the result the excitation across the band gap involves all states: O 2p, Ti 3d, and F 2p when present.

To understand better relevant photocatalytic properties of the modified anatase surfaces it is necessary to carry out more accurate computations. More precise results for DOS will permit...
reasonable integration of the partial DOS that gives total percentage of the given orbital that is occupied at a specified energy level. This provides information about electron transfer processes that is important for photocatalysis. The crystal orbital overlap populations from more accurate band structures are expected to give detailed information about bond formation.

The results obtained indicate that the systems under investigation constitute an interesting topic for further studies.

Bibliography


[77] Information available at: http://www.materialsdesign.com/


List of Figures

Figure 1. The structure of the stoichiometric TiO$_2$ anatase (101) surface. (a) non-modified; (b) with F$^-$ adsorbents; (c) with OH$^-$ adsorbents.

Figure 2. Electronic structure of the non-modified TiO$_2$ anatase (101) surface. (a) band structure (G stands for Γ-point); (b) total DOS; (c) PDOS for Ti 3d orbitals; (d) PDOS for O 2p orbitals; (e) PDOS for O 2s orbitals; (f) Integrated total DOS.

Figure 3. Electronic structure of the TiO$_2$ anatase (101) surface with F$^-$ adsorbents. (a) band structure (G stands for Γ-point); (b) total DOS; (c) PDOS for Ti 3d orbitals; (d) PDOS for O 2p orbitals; (e) PDOS for O 2s orbitals; (f) PDOS for F 2p orbitals; (g) PDOS for F 2s orbitals.

Figure 4. Electronic structure of the TiO$_2$ anatase (101) surface with OH$^-$ adsorbents. (a) band structure (G stands for Γ-point); (b) total DOS; (c) PDOS for Ti 3d orbitals; (d) PDOS for O 2p orbitals; (e) PDOS for O 2s orbitals; (f) PDOS for O (from OH groups) 2p orbitals; (g) PDOS for O (from OH groups) 2s orbitals.
List of Tables

Table 1. Lattice parameters in [Å] of the rutile and anatase TiO$_2$ structures.
Table 1. Lattice parameters in [Å] of the rutile and anatase structures.

<table>
<thead>
<tr>
<th>Structure</th>
<th>Lattice parameter</th>
<th>Present work</th>
<th>Experiment$^a$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rutile</td>
<td>a</td>
<td>4.661</td>
<td>4.587</td>
</tr>
<tr>
<td></td>
<td>c</td>
<td>2.969</td>
<td>2.954</td>
</tr>
<tr>
<td></td>
<td>c/a</td>
<td>0.637</td>
<td>0.644</td>
</tr>
<tr>
<td>Anatase</td>
<td>a</td>
<td>3.822</td>
<td>3.782</td>
</tr>
<tr>
<td></td>
<td>c</td>
<td>9.690</td>
<td>9.502</td>
</tr>
<tr>
<td></td>
<td>c/a</td>
<td>2.535</td>
<td>2.535</td>
</tr>
</tbody>
</table>

$^a$ Ref. [6]