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Antoine Lambert, Romain Bourqui, David Auber

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HAL Id: hal-00495279
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Submitted on 25 Jun 2010

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Winding Roads: Routing edges into bundles

A. Lambert and R. Bourqui and D. Auber
CNRS UMR5800 LaBRI, INRIA Bordeaux - Sud Ouest, France

Abstract

Visualizing graphs containing many nodes and edges efficiently is quite challenging. Drawings of such graphs generally suffer from visual clutter induced by the large amount of edges and their crossings. Consequently, it is difficult to read the relationships between nodes and the high-level edge patterns that may exist in standard node-link diagram representations. Edge bundling techniques have been proposed to help solve this issue, which rely on high quality edge rerouting. In this paper, we introduce an intuitive edge bundling technique which efficiently reduces edge clutter in graphs drawings. Our method is based on the use of a grid built using the original graph to compute the edge rerouting. In comparison with previously proposed edge bundling methods, our technique improves both the level of clutter reduction and the computation performance. The second contribution of this paper is a GPU-based rendering method which helps users perceive bundles densities while preserving edge color.

Categories and Subject Descriptors (according to ACM CCS): I.3.3 [Computer Graphics]: Picture/Image Generation—Line and curve generation

1. Introduction

Graphs play an important role in many research areas, such as biology, microelectronics, social sciences, data mining, and computer science. Improvements in data acquisition techniques drive the need for visualization, as the size and the complexity of acquired graphs prohibit manual drawing. The graph drawing and information visualization communities focus on designing effective visualizations of such large graphs. For particular classes of graphs, such as trees, planar graphs or directed acyclic graphs, effective solutions have been found that give very good results; not only in terms of time and space complexity but also in terms of aesthetic criteria. However, real-world graphs from application domains usually do not belong to these classes. To find an algorithm that gives good results (in terms of computation time, aesthetic criteria and information emphasized) for arbitrary graphs is a difficult problem. As it produces visually pleasant and structurally significant results, the most popular approaches to draw such graphs are the force-directed approaches (e.g., [FLM94, HJ04]).

However, due to data complexity, we cannot expect force-directed approaches to give readable representations of all graphs. To the best of our knowledge, there exists for instance no drawing algorithm that offers a satisfying layout of a scale-free network (i.e. a graph whose degree distribution follows a power law). Furthermore, in some application domains, such as geography, nodes positions cannot be changed as they bring information. In such cases, information discovery becomes difficult as edge crossings and node-edge overlaps clutter the representation. Reducing the clutter in a graph representation is therefore of utmost importance to identify relationships and high-level edge patterns.

In the past, clutter reduction had been achieved using two main techniques: compound visualization and edge bundling. In a compound visualization (e.g. [vv04, AvK06, AMA07]), an abstraction of the original network is built by collapsing clusters into metanodes and the result is then displayed on the screen. This technique reduces the cluttering of the representation as inter-cluster edges are merged into metaedges. However, complex interactions for collapsing/expanding metanodes are necessary to retrieve the information. Furthermore, the compound visualization is not suitable when nodes positions cannot be changed as clusters may overlap.
Recently, edge bundling techniques [PXY*05, Hol06, CZQ*08, Hv09] are of increasing interest in the graph visualization community. Put under the spotlight by Holten [Hol06], this technique routes edges into bundles in order to uncover high-level edge patterns and to emphasize relationships in relational data.

In this paper, we focus on a novel approach to generate edge-bundled representations of graphs. We introduce an intuitive edge bundling algorithm which efficiently reduces edge clutter in graphs drawings. Our method discretizes the plane into regions. Boundaries of these regions are used as roads to route edges. The main contribution of this paper is therefore a new edge bundling technique that improves computation times when compared to existing methods but also avoids node-edge overlaps. The second contribution of this paper is a GPU-based rendering method which enables users to perceive bundle densities while preserving edge color. Our algorithm and rendering technique have been implemented as two plugins for the Tulip graph visualization software [Aub03].

The remainder of this paper is structured as follows. Section 2 reviews related work on edge clutter reduction methods and techniques to enhance edge bundles visualization. In section 3 and 4, we present the main steps of our method and several implementation issues. We next explain a way to parametrize the level of clutter reduction in section 5. Section 6 refers to rendering techniques necessitated by edge bundling visualization. Finally, we draw a conclusion and give directions for future work in section 7.

2. Previous Work

As mentioned above, we focus in this paper on a representation of edges whose extremities have fixed positions. In this section, we investigate existing techniques for edge clutter reduction but also techniques for enhancing edge bundles visualization. For a general overview of clutter reduction methods and not only edge clutter reduction techniques, we recommend the survey of Ellis and Dix [ED07].

2.1. Edge Clutter reduction

Edge routing: One of the first attempts to reduce clutter in graphs drawings was made by the graph drawing community. Indeed, to increase the readability of a graph drawing, one should try to bound the number of edge crossings but also to avoid node-edge overlaps (to use non-point-size nodes for instance). In [DGKN98], Dobkin et al. give a novel method using visibility graphs and shortest-path edge routing to remove node-edge overlaps. The technique was ported to tangent visibility graphs by [WMS06]. Finally, Dwyer and Nachmanison [DN10] give a fast heuristic to compute an approximation of the visibility graph to reduce the time complexity of the approach and therefore to support large graph edge routing. These approaches efficiently reduce edge clutter by avoiding node-edge overlaps, however they do not help the user to identify high level edge patterns.

Interactive techniques: Wong et al. give in [WCG03, WC05] interaction techniques to remove clutter around the user’s focii. Edges close to one of the focii are pushed away in a fisheye-like manner while preserving nodes positions. The representation is locally uncluttered around each focus, but this technique does not reduce the clutter of the entire representation.

Confluent Drawing: The graph drawing community focused on a particular representation of graph, called confluent graph drawing. In a confluent graph drawing, a non-necessarily planar graph is represented without edge crossing. In this techniques, groups of crossing edges are drawn as curved overlapping lines. For instance, Dickerson et al. [DEGM03] give an algorithm to compute a confluent graph drawing which is based on the detection of maximum cliques and bi-cliques (complete bipartite graph). Then, edges are bundled to obtain a “planar” representation of these unplanar subgraphs. Even though confluent graph drawing techniques give interesting results, they cannot be applied to all classes of graphs (see [DEGM03] for more details).

Node clustering: Phan et al. present in [PXY*05], a flow map layout technique based on geometrical node clustering. Edges are routed along the hierarchy tree branches. This idea has also been used by Holten in [Hol06] to enhance relationship in hierarchical (and relational) data. The main drawback of both methods is that edges are routed using a hierarchy tree which can be restrictive in the general case.

Edge clustering: In [GK06], Gansner and Koren give an improved circular layout algorithm where edges are routed either on the outer face of the circle or in its inner face. Edges routed inside the circle are bundled using an edge clustering algorithm that tries to optimize area utilization. Another edge clustering method is given by Cui et al. [CZQ*08]. In this paper they propose a geometric approach to create bundles of edges. The main idea is to build a control mesh based on user interaction or a Delaunay triangulation. The mesh is then used to compute regions where edges should be merged. The merging of edges is done according to a clustering algorithm based on the orientation of edges. A post processing step is applied to reduce the “zigzag” effect of edges. Finally, Holten and van Wijk introduced in [Hv09] a force-directed heuristic to bundle edges and therefore, to unclutter a representation of a graph where nodes positions are fixed. In this heuristic, dummy nodes are inserted to split edges into segments. A similarity measure between edges is computed to determine which of them should interact. Dummy nodes of any two interacting edges are linked by inserting dummy edges. Bundles are obtained by running a force-directed algorithm preserving positions of the original nodes.
2.2. Enhancing edge-bundled graph visualizations

Smoothing curves: The main feature common to each edge-bundled graph visualizations is the drawing of edges as curves. Indeed, rendering graph edges as curves makes the task of following them easier and gives a more visually appealing graph drawing. In [Hol06], Holten renders bundled edges piecewise with cubic B-splines. By using this type of splines, which offer local control on the curve shape, one can produce distinct and coherent bundles. In [ZYC+08], Zhou et al. use others models of splines to render bundled edges which are Bézier curves and Catmull-Rom splines. Another method used by Holten et al. [Hv09] and Weiwei et al. [CZQ+08] is to apply a smoothing technique on the edges drawn as polylines to morph them into curves.

Coloring edges: Another method of enhancing edge-bundled graph visualization is to use edge colors and opacities to encode information. In [CZQ+08], edge colors are mapped to the directions of the original links. A similar technique is used in [Hol06] but edge direction is encoded by an interpolated color gradient running from a fixed color for the source to a fixed color for the target. In [Hol06] edge opacities are mapped to their length with long curves being more transparent than short ones, preventing short curves to become obscured. In [CZQ+08], the opacity of each segment of the polyline representing an edge is mapped to the density of lines overlapping it. Another technique for estimating the quantity of edge segments merged together is proposed in [Hv09]. A GPU-based method is used to compute the amount of overlap for each pixel of the produced graph visualization. This value is then used to map pixel colors to a user-defined gradient color scale after a minimum and maximum value of overlap have been computed.

3. Routing edges for bundling

The main idea of our technique is to use edge routing to bundle edges. We first create a grid graph according to the node positions. This grid is then used to compute the shortest routes for each edge. Like highways attract more drivers than smaller roads, we use frequent paths to bundle edges.

3.1. Grid computation

To compute the shortest paths of each original edge, we create a grid graph on which we connect the original nodes. This graph is computed by discretizing the plane into cells using nodes positions. In the following paragraph, we investigate several approaches to create the grid graph.

Cui et al. [CZQ+08] use a regular grid to discretize the plane. This grid is used to aggregate edges that have the same orientation together. Using a fine regular grid would resolve in large grid graph sizes. Indeed the grid must be very precise to route edges through highly dense regions. However, using a large grid raises two major problems. First, it generates a multitude of routes and therefore reduces the bundling of long edges. Secondly, the grid graph may contain many times more than $|V|^2$ nodes, making the approach expensive in terms of shortest paths computation and memory.

To obtain a multi-resolution grid graph, one can use a quad tree [FB74]. In a quad tree, the plane is decomposed in four parts until it contains at most one element. In figure 1(a), one can see the grid graph generated on the 2000 air traffic network. Such an approach is efficient in terms of computation time since its complexity is $O(|V| \cdot \log(|V|))$. However, on one hand it generates a large grid (37,395 nodes/69,102 edges for the 2000 AT network) and on the other hand, large cells promote horizontal and vertical paths. Voronoï diagrams [Vor08] can also be used to generate the grid graph. In a voronoï diagram, cells are regions of the plane in which points of a cell are closer to the cell’s site (here original nodes) than to any other site. Figure 1(b) shows the grid graph obtained with the Voronoï approach. Using classical Voronoï diagram does not guarantee to avoid node edge overlap in case of non point size node. However that problem can be easily addressed using a constrained Voronoï diagram (taking node sizes into account). This method generates a small grid graph (4,531 nodes/13,558 edges for the 2000 AT network) and can be computed in $O(|V| \cdot \log(|V|))$ time [For86]. However, it generates large cells for sparse regions. Due to our routing method, these large cells will create large detours. In this work, we propose a hybrid algorithm based on both quad trees and Voronoï diagrams. In our algorithm, the size of quad tree cells are parameetrized to generate different levels of clutter reduction (see section 5). Voronoï diagrams are then used to construct the final grid graph. Figure 1(c) shows the grid graph obtained with this hybrid approach. Since the quad tree adds $O(|V|)$ nodes, the $O(|V| \cdot \log(|V|))$ time complexity is preserved. Therefore, the resulting grid graph is of reasonable size (10,146 nodes/30,315 edges on 2000 AT network).

3.2. Edge routing

The next step of our method consists of routing edges in the original graph onto the grid we obtained in the previous step. We can use a shortest path algorithm directly to achieve this operation. Since the grid is planar, we obtain a polyline drawing of the graph. However, this method does not guarantee that edges follow the same path and thus it creates few bundles. To augment the bundling effect, we use the metaphor of roads and highways. The idea is to transform regular roads into larger ones if they are highly used. We reproduce this effect by first computing all the shortest paths between linked nodes on the original graph. Then, according to the number of shortest paths passing through an edge of our grid, we adjust the weights of the edge. Reducing the weights of an edge is equivalent to transforming it into a highway, since using that edge enables it to go faster from one point to another. We then compute a shortest path for each edge of the original graph. This weights adjust-
A naive implementation of our approach can bundle graphs in a reasonable amount of time. In figure 2, one can see that on the US migration graph [Hv09, CZQ’08] it takes 75 seconds to bundle the graph with our approach. This execution time is faster than [Hv09] but significantly slower than [CZQ’08]. This benchmark was ran on an Intel(R) Core(TM)2 Extreme CPU Q9300 2.53GHz. To improve the efficiency of our method and make it usable on larger graphs, several optimizations must be done. In this section, we propose optimizations that reduce the overall computation time. These optimizations consist of minimizing the number of shortest paths computed and taking advantage of modern multi-core architectures. These improvements do not change the output of the algorithm when compared to the straightforward implementation. However, the execution time can be reduced by a factor of ten or more, depending on the number of CPUs and the topology of the graph.

**First optimization** : The first optimization consists of reducing the time to compute the shortest paths. In our implementation, we use Dijkstra’s algorithm [Dij71]. The weights of the edges are modified according to the paths we want to promote. Thus, we must use the weighted shortest path algorithm, and we can not use faster Euclidian graph shortest path methods [SV86]. If we use this straightforward approach, we have to compute the shortest paths for each node of the original graph to each node of the grid. These operations can be done in \( O(|V_{\text{graph}}| \cdot |E_{\text{grid}}| \cdot \log |V_{\text{grid}}|) \) time. However, we only need the shortest path between each adjacent nodes of the original graph on the grid. With a slight modification to Dijkstra’s algorithm, we can stop the computation of paths when all candidates in the Dijkstra’s priority queue are at a distance greater than all the neighbors of our source node. In figure 2(a), 2(b) and 2(c) one can see that this modification significantly decreases running time. In figure 2(c), one can see that the running time has been reduced by a gain of factor 6.4. This call graph has been drawn with a force-directed algorithm [HJ04] which tries to lay out as close as possible connected nodes. Thus, this optimization allows us to restrict the exploration to a small part of the grid each time. This makes our algorithm efficient for graphs drawn with this kind of algorithm.

**Second optimization** : The second optimization aims to reduce the number of calls to the shortest path algorithm and also increases the efficiency of the previous one. After computing the shortest paths from one node to its neighbors, we don’t need to consider that node again during the computation. Minimizing the number of nodes to treat in order to consider each edge of the graph is the so called vertex cover problem [Hoc97]. Unfortunately this problem is NP-complete. However, it is possible to compute a minimal (but not optimal) vertex cover of a graph. Instead of using the original graph for computing the neighbors of a node in the first optimization, we can construct a copy of that graph, called vertex cover graph, in which we delete a node after it has been treated. Deleting this node in the vertex cover graph reduces the degree of its neighbors and thus it will reduce the set of nodes considered by the first optimization. In figure 2, one can see that in all cases this improvement significantly decreases the running time of our technique.

**Third optimization** : The third optimization aims to reduce the number of critical sections in the parallel implementation of our algorithm and to create tasks of equiva-

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Figure 1: Grid graphs generated on the 2000 Air Traffic (AT) network with (a) a quad tree (37395 nodes/69102 edges), (b) a Voronoi diagram (4531 nodes/13558 edges) and (c) the hybrid quad tree/Voronoi approach (10146 nodes/30315 edges).
5. Level of Clutter Reduction

As described in previous sections, our method consists of routing the original edges on the grid graph using the well-known Dijkstra’s algorithm. Weighted shortest paths allow us to define different levels of clutter reduction by either adapting edge weights or avoiding a particular path. In figure 3, one can see the different levels of clutter reduction that we propose.

5.1. Edge-edge clutter reduction

The edge-edge clutter reduction we define corresponds to the one used in [CZQ*08, Hv09], i.e. only clutter due to edge crossings is reduced. In this case bundles of edges can overlap with nodes of the original graph. For instance, figure 3.(b) shows the result obtained on the graph of figure 3.(a) using only edge-edge clutter reduction. One can see in the zoomed view that blue edges are routed through nodes of the network. To obtain this level of clutter reduction, one just has to consider each edge of the grid graph when routing the edges. In particular, a node-grid edges (i.e. edges linking original nodes to nodes of the grid graph) can be used when computing the shortest paths on the grid graph.

5.2. Node-edge clutter reduction

Edge-edge clutter reduction only allows us to reduce the clutter due to edge crossings. Still, one may want to unclutter the representation by reducing clutter due to node-edge overlaps. We can forbid routing node through the original graph. For instance, in figure 3.(c), one can see that the blue edges are routed around nodes in the graph while these edges cross the nodes using edge-edge clutter reduction only. We obtain node-edge clutter removal by filtering out node-grid edges during Dijkstra’s algorithm. As these node-grid edges are not taken into account when computing the shortest paths, no original edge can be routed through a node of the original graph. Of course, path ending on original nodes are allowed.

5.3. Uncluttering highly dense zones

We can further improve clutter reduction by promoting paths to pass through sparse regions. For instance, in figure 3.(d), one can see that all blue edges have been routed around the dense subgraph (in the middle of figure 3.(d)). Our method naturally produces this effect since paths passing through dense regions are quite twisty. As the density in this part of the drawing is high, the corresponding region of the grid graph contains many cells. Therefore, the length of
an edge routed through this part of the graph is longer than the Euclidian distance between its extremities. To augment this phenomena, dummy nodes are added around the original node when applying our quadtree method (see section 3). We are able to unclutter even more dense regions by adapting the initial weights of the grid edges. Let \( l \) be the Euclidian distance between two nodes in our grid (i.e. length of an edge). We compute the new weights using the following formula

\[
    w(e) = \text{length}(e)^\alpha,
\]

the \( \alpha \) parameter can be used to increase or decrease the uncluttering of dense regions. An \( \alpha \) less than one promotes path outside dense regions. In figure 6.1(b) one can see that edges going from bottom left to the bottom right corner are bundled on the south pole. It thus reduces clutter in the center of the map.

6. Interactive rendering of edge-bundled graphs

6.1. Smoothing the edges with curves

Once the bundling process has been performed on the graph, edges become polylines due to the routing phase which adds bends to them. With respect to the size of the graph and the grid used to compute the bundles, the number of edge bends can be quite high. When rendering the edge-bundled graph layout, these bends induce a “zigzag” effect on the edges making them hard to follow. In order to smooth edges, we offer the possibility of rendering them as curves in our visualization system using edge bends as curves control points. Several kinds of parametric curves are proposed including Bézier curves and cubic B-splines. Moreover, edges going to the same region of the graph and sharing successive bends remain merged, giving a nicer impression of flows between different areas of the graph. Several kinds of parametric curves are proposed including Bézier curves and cubic B-splines. Moreover, edges going to the same region of the graph and sharing successive bends remain merged, giving a nicer impression of flows between different areas of the graph. However, even if this result is more visually appealing, one drawback of this technique is that we re-introduce edge-node clutter in the drawing. Due to the high computational cost of rendering curves with a large number of control points, especially Bézier curves, we have developed a GPU-based implementation.

It allows us to draw a large number of curves defined by an arbitrary number of control points in real time, giving us the ability to smoothly interact with the graph drawing. As an example, a comparison between the polyline and Bézier curve rendering of the graph edges is shown in figure 4.

6.2. Edge splatting

When edges have been merged into bundles, high-level edge patterns emerge on the graph drawing, giving a nice impression of flows between different regions of the graph. However, the information regarding the number of edges contained in a bundle is not easily seen in the drawing. In order to distinguish strong bundles from weak ones, we propose an edge splatting technique to visually enhance them.

Our method is inspired from the GraphSplatting technique introduced by van Liere et al. in [vd03]. In this work, the authors represent a graph as a 2D continuous scalar field and calculate a splat field. GraphSplatting provides a way to visualize continuous variations in the density of vertices which can help determine the structure of the underlying graph. Another work sharing similar features to this technique is the one by Chiricota et al. [CJM04]. They propose a technique to select points in a scatterplot representation by applying a Gaussian blur on the associated image. This blurring effect melts points forming a dense subregion of the scatterplot into a large patch that can help a user to identify and select clusters in the underlying data.

The following presents our rendering pipeline to visualize the density of edges that have been merged into bundles. It is based on a combination of common image processing and computer graphics technique and each stage entirely runs on the GPU. In a similar way than the GraphSplatting technique, the idea is to compute a splat field encoding continuous variations in the density of merged edges. This splat field can then be displayed on screen in a various ways. We explored two solutions to visually encode bundles density.

submitted to Eurographics/IEEE-VGTC Symposium on Visualization (2010)
Figure 4: Comparison between two representations of an edge-bundled graph. In (a), edges are drawn as polylines while in (b) they are drawn as Bézier curves. When edges are rendered as Bézier curves, their shapes are smooth and a nice impression of flows between different regions of the graph emerges from the drawing. However, edges can overlap nodes due to the lack of local control proper to Bézier curves.

The first one simply maps density values to colors based on a user-defined color scale. The second one preserves edges colors and uses a per-pixel shading technique mapping density values to heights giving the impression than strong bundles appears higher than weak ones.

6.2.1. Computing and rendering the splat field

The first stage of our edge splatting rendering pipeline is to compute the number of edges crossing each pixel of the drawing. As in [Hv09], this operation can be done by performing an offscreen rendering of the graph edges in an accumulation buffer. Using the OpenGL graphics API, we can implement it with a render-to-texture technique using a Frame Buffer Object with a single precision floating point texture attached to it. Then, we assign the same color to each edge and activate additive blending during the rendering stage.

Next stage of the rendering pipeline is the splat field computation. The resulting texture of the previous stage is a field of discrete values encoding edges density per pixel. The goal of this stage is to transform it into a continuous scalar field. This process can be performed by convoluting the discrete density values field with a Gaussian kernel defined by a radius $r$ and a standard deviation $\sigma$. This operation can still be performed on the GPU by rendering to a texture and by writing an OpenGL fragment shader to perform the convolution. A shader program allows to modify the default behavior of some processing units in the GPU rendering pipeline. A fragment shader aims to customize the pixel processing unit of the pipeline whose role is to calculate the colors of the pixels to display. In OpenGL, shader programs can be written using a C-like language called GLSL (the OpenGL Shading Language). Shaders offer tangible benefits since they are well suited for parallel processing as most modern GPUs have multiple shader pipelines. Because a fragment shader allows reads of pixels from a texture stored in graphics memory, implementing the convolution of the discrete density values with a Gaussian kernel is an easy task. Our implementation takes advantage of the fact that a Gaussian filter is linearly separable. Therefore, we can divide the process into two passes [Smi97]. In this way, performances do not degrade as the radius of the kernel increases. The source code of this fragment shader is generated dynamically with respect to the kernel radius requested by the user. The standard deviation of the Gaussian kernel can also be modified dynamically. The larger the kernel radius and standard deviation, the more the splat field is smoothed.

In order to visualize the computed splat field, a gradient-based rendering is performed, mapping the splatting value associated to each pixel to a user-defined color scale. To achieve this task, the minimum and maximum value of the splat field are determined with a GPU texture reduce operation [KW03]. A quadrilateral with the same size as the splat field texture is then drawn to the screen and pixel coloring is performed by a dedicated fragment shader, mapping splatting values to the user-defined gradient. The result of the edge splatting technique on the US migration graph is presented in figure 5.

6.2.2. Enhancing the splatting with shading

As a way of improving the splat field representation, we propose an extra rendering stage based on a bump mapping...
technique. Bump mapping is a computer graphics technique introduced by Blinn [Bli78] allowing a rendered surface to appear more realistic without modifying geometry. It adds a per-pixel shading that makes the surface appears bumpy, by changing the surface normals. The colors and brightnesses of the pixels are then altered with respect to these normals using a lighting algorithm. The modified normal for each pixel are stored in a texture called a normal map. RGB components of the pixels colors store the X, Y and Z values of the normal vectors. This normal map is generated from a heightmap, another texture storing the height values for each pixel of the surface. Bump mapping is classified in the per-pixel displacement mapping methods. An exhaustive survey of these displacement mapping algorithms is presented by Szirmay-Kalos et al. [SKU08].

Recently, Willems et al. proposed a geographical visualization of vessel movements [Wvv09] where they used shading to highlight significant maritime areas, like highways or anchoring zones. Their visualization is based on density fields that are derived from the convolution of dynamic vessel positions with a kernel. In our case, if we map splatting values to heights, we can use bump mapping to enhance edge-bundled graph visualizations. Bundles with high density edges will appear higher than others with this rendering technique and will visually emerge from the layout. In order to achieve this task, we first need to generate a heightmap from the computed splat field. This map can be generated by mapping the splatting values to a black to white color scale: black representing minimum height and white representing maximum height. Then, we can generate the associated normal map by obtaining the heightmap gradient using for instance the Sobel or Prewitt filter [GW06]. This operation can be performed on the GPU with a fragment shader. This program compute for each pixel the heightmap derivatives in horizontal and vertical directions using the gradient operator and construct the associated normal from these.

Once the normal map associated with the splat field has been generated, bump mapped rendering can be performed. The bump mapped is generated by a dedicated shader program reading the modified normals from the normal map texture and performing a per-pixel illumination using Blinn-Phong [Bli77]. The final colors of the pixels are computed from the lighting properties and another texture called the diffuse map. In our case, the diffuse map can correspond to the splat field color mapping or the original edge colors. To perform a global illumination, the light is set to be directional with each light ray parallel to the Z-axis. Our visualization system then lets the user configure the ambient, diffuse and specular color of the light source. Results of this rendering technique are presented in figure 6.

6.2.3. Rendering performances

In table 1, we introduce an estimation of the running time for the edge splatting rendering pipeline. The benchmarks have been ran on two different edge-bundled graphs containing at least ten thousands edges. The table provides estimation for the whole pipeline traversal but also for its three main stages : density map generation, splat field computation (includes Gaussian convolution and GPU reduction) and bump mapping rendering (includes diffuse map, heightmap and normal map generation). The introduced performances have been measured by executing one hundred times the edge splatting pipeline and by computing the average rendering times. As shown by the results, the most expensive stage is the density map generation. During that process, the rendering of the whole graph edges set is required. Bundled edges can have a high number of bends so the number of vertices sent to the GPU is much larger when compared to straight line rendering. Obviously, the Bézier curve rendering is more expensive than the polyline one due to the high computational cost of curves generation. The two remaining stages of the rendering pipeline can be executed in real time with respect to the measured framrates. Eventually, performances are acceptable with respect to the number of edges bends. For instance, the whole pipeline traversal for the US migration graph, which contains ten thousands edges with a large number of bends, takes around 0.1 seconds for the polyline rendering and around 0.5 seconds when rendering edges as Bézier curves.

Table 1: Performances of edge splatting rendering for different edge-bundled graphs. Rendering is performed in a viewport whose size in pixels is 800 x 800. Edge splatting is performed with a Gaussian kernel of radius 3. The normal map needed for bump mapping is generated with a 5 x 5 Prewitt Filter. The CPU used to perform these tests is an Intel(R) Core(TM)2 Extreme CPU X9100 @ 3.06GHZ and the graphic card is a NVidia Quadro FX 1700M.

7. Conclusion

In this paper, we have presented a novel and intuitive technique to route edges into bundles. This technique reduces the clutter of the representation and also emphasizes high-level edge patterns. Optimizations of our technique allow us to outperform the execution times of existing methods and
Figure 6: Illustrations of the bump mapping based rendering of edge splatting with the edge-bundled representations of the US migration graph and 2000 AT network. Strong bundles appear higher than other ones with this technique making them visually emerge from the graph drawing. For the US migration graph, heights are linearly mapped to the splat field and the diffuse map used for the bump mapping rendering corresponds to the splat field linear color mapping. For the AT graph, heights are logarithmically mapped to the splat field and the original edges colors are used as diffuse map.

scale to larger graphs. In addition to edge-edge clutter reduction, our method can guarantee that no node-edge overlaps occurred in the drawing. Moreover, by promoting long grid edges, we can further reduce edge cluttering in highly dense regions and preferably bundle edges in sparse ones.

Using curves when rendering edges facilitate information discovery as it eases the following of bundles. We extend the GraphSplatting technique to edge splatting in order to depict bundles densities. Finally, a bump mapping technique enhances the edge splatting and also makes it possible to preserve the color encoding of the edges. Our GPU-implementation allows fast enough rendering to support smooth interaction.

An interesting direction for future work is to explore different methods to build the grid graph such as constrained Delaunay triangulations. More specifically, a grid supporting non-uniform node sizes would allow bundles to avoid regions of the image in order to display nodes labels, captions, color scales or any other information. We also plan to adapt our method to the sphere, to surfaces having other topologies, or even 3D space.

Improving the curves smoothing technique also remains future work. On one hand, we want to constrain our curves to avoid nodes. On the other hand, we want to speed up the rendering by minimizing the number of bends, while also guarantying that no node-edge overlap is created.

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