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Identification of Lamination Stack Properties: Application to High-Speed Induction Motors

Guillaume Mogenier, Régis Dufour, Guy Ferraris-Besso, Lionel Durantay, and Nicolas Barras

Abstract—In order to predict the lateral rotordynamics of a high-speed induction motor, an optimization procedure is used for identifying the dynamic behavior of the magnetic core made of a lamination stack, tie rods, and short-circuit rods. Modal parameters predicted by a finite-element model based on beam elements and measured on induction motors are included in modal error functions contained in a functional. The minimization of this functional by using the Levenberg–Marquardt algorithm permits extracting the equivalent constitutive properties of the lamination stack for several rotors of different sizes. Finally, the size effect on the constitutive properties identified is discussed.

Index Terms—Finite-element (FE) methods, parameter identification, squirrel-cage motors, vibrations.

I. INTRODUCTION

THIS PAPER focuses on the squirrel-cage induction motor known as the Moteur Grande Vitesse (MGV) in the 3 to 30 MW range from 6000 to 18 000 r/min, used for critical applications, particularly motocompressors, in the oil and gas industry. This paper continues from an International Conference on Electronic Materials 2008 conference paper dealing with other experiments performed on several MGVs to evaluate a possible relation between identified parameters and rotor sizes, i.e., magnetic core length L_{fer} (Fig. 1) and diameter D_{fer} (Fig. 2). As shown in Fig. 1, an MGV is mainly composed of two steel shaft ends and full-depth laminations held together by steel tie rods. The squirrel cage consists of copper short-circuit rods distributed at the periphery of the core (Fig. 2) and linked to two bronze alloy rings placed at both ends of the stack. The stack and the rings are tightened by the tie rods, also distributed at the periphery of the core and screwed into the shaft ends. This configuration is proposed as full-depth laminations considerably reduce the eddy-current circulation along the longitudinal axis in the core of the magnetic part and thus eliminate flux saturation. Consequently, the MGV is more

Fig. 1. Diagram of a squirrel-cage induction motor.

Fig. 2. Cross section of the magnetic core of a squirrel-cage induction motor.

compact and efficient than widely used solid rotors with shrink fitted laminations. It also prevents problems such as electrical loss, heat dissipation, and loss of adhesion between the components although it is difficult to predict its dynamic behavior. The problem of modeling the magnetic core and the stacks of full-depth laminations has been given little attention in scientific papers. References [1] and [2] suggested homogenized bending rigidity for the entire magnetic core cross section by adding the bending rigidity of each cross section component. McClurg [3] deals with a stiff shaft design for a squirrel-cage rotor, but the bending rigidity of the magnetic core is not described. However, many authors have attempted to predict the dynamic behavior of induction machine rotors with a laminated core mounted on a solid shaft, i.e., laminations around central hole. The stiffening effects of the laminated core are not easy to assess and often require identification via modal testing. Ede *et al.* [4] assess the influence of leading design parameters, such as stack length, on the natural frequencies of a high-speed permanent magnet brushless machine by using a 3-D finite-element (FE) model. Garvey *et al.* [5] present the advantages of a branched model for a laminated rotor. The laminations

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are considered as several annular ring subsets linked together by elastic connections. Moreover, the subsets are elastically connected to the shaft. Chen *et al.* [6] consider an equivalent Young modulus for the stack and use a branched beam model for the magnetic core. The authors of many papers have dealt with a coefficient known as stacking factor that modifies the value of the mass of the lamination stack. In addition, its weak Young modulus is due to resin or varnish layers on the interfaces between consecutive laminations. Garvey *et al.* [5] consider the lamination stack as an orthotropic material whose elastic strain–stress relation takes into account the lamination material and the mean flexibilities (shear and compressive) of the lamination interfaces. Kim and Kim [7] show that the lamination pressure has considerable influence on the lateral natural frequencies of a rotor. An equivalent diameter and lumped masses are considered for modeling the entire magnetic core.

In identification procedures, an optimization algorithm is used so that the optimization parameters of an FE model make predicted data tend toward target values, i.e., measured data. Such algorithms can use modal data for updating and then identifying the FE model parameters. Modal error functions are defined to quantify the difference between predicted and measured natural frequencies and mode shapes. Lee and Kam [8] use a common modal error function based on natural frequencies in order to identify the properties of laminated composite plates. Cugnoni [9] proposes two original modal error functions based on the diagonal and extra-diagonal terms of the modal assurance criterion matrix. Feng *et al.* [10] use a more classical modal error function, based on the difference between the components of predicted and measured mode shapes, to identify the material parameters of concrete dams. These functions are combined in a functional whose minimization requires its derivatives, with respect to the optimization parameters, that depend on eigenelement derivatives. Eigenvalue derivatives are obtained from the relation given by [11] whereas eigenvector derivatives can be computed by using approximate or exact methods [12]. Min *et al.* [13] compare different algorithms designed to achieve this.

In this paper, an FE model of an induction rotor is presented with particular attention given to modeling the magnetic core. It is based on the structural dynamics theory described in [14] and therefore uses beam FE in order to limit the degrees of freedom (DOF). Under certain assumptions, tie and short-circuit rods can also be modeled with beam FE. Even if a beam-based model is used, the constitutive properties of the stack are defined such that the shear and the Young moduli are independent in order to take into account its orthotropic properties [5]. The lateral dynamic behavior of the stack is then identified by performing experimental modal analyses on several rotors of different sizes. The identification strategy presented in [15] consists in minimizing the difference between the measured and the predicted modal data provided by the FE model, by using the Levenberg–Marquardt algorithm [16], [17]. Identification results are discussed to evaluate a possible relation between the equivalent constitutive properties of the lamination stack and the magnetic core length and diameter.

Fig. 3. Short-circuit rod in bending—kinematic assumption.

II. FE MODEL

The predicted modal data emanate from the eigenvalue equation of the undamped FE model based on the structural dynamic theory, described in [14], for each mode $k = 1, \dots, m$

$$(K - \tilde{\omega}_k^2 M) \tilde{\varphi}_k = 0, \quad \text{with } K = K_S + K_P \quad (1)$$

where $\tilde{\omega}_k$, $\tilde{\varphi}_k$ are the k th angular frequency and associated mode shape, respectively. K_S is the structural stiffness matrix, K_P is the stress stiffening matrix if a possible axial prestressing force acts on the beam FE [18]. M is the mass matrix due to the translation and rotatory inertia, the latter being classically neglected for slender structures. Shear strain and rotatory inertia are taken into account in the Timoshenko in-plane beam FE containing 2 DOF per node: one translation and one rotation. Thus, a shear correction factor dependent on the shape of the cross section is used as in [19].

Free–free boundary conditions are taken into account by adding low-stiffness springs (10 N/m) at each boundary node. Disks and landing rings are considered as lumped masses. To identify the stiffness parameters of the lamination stack, specific assumptions must be considered to model the tie and the short-circuit rods. The latter can be modeled as beams of diameter D_{CC} (Fig. 2) whose neutral axes coincide with the neutral axis of the magnetic core. These rods are fastened at middle of the magnetic core by screws and their ends can slide in the short-circuit rings, as shown in Fig. 3. Thus, each FE of the discretized magnetic core is connected to two consecutive nodes its elementary matrices being the sum of those of the short-circuit rods and the lamination stack. Furthermore, the tie rods are modeled as a one FE equivalent hollow cylinder clamped at nodes A_0 and B_0 (see Fig. 2). Let D_{Out}^{TI} and D_{In}^{TI} be its outer and inner diameters, respectively, and simply calculated by considering surface S_{TI} and second moment of area I_{TI} of the tie rods

$$D_{Out}^{TI} = \left(\frac{8I_{TI}}{S_{TI}} + \frac{2S_{TI}}{\pi} \right)^{\frac{1}{2}}, \quad D_{In}^{TI} = \left(\frac{8I_{TI}}{S_{TI}} - \frac{2S_{TI}}{\pi} \right)^{\frac{1}{2}}. \quad (2)$$

The screwing torque ensures the stress stiffening in the tie rods and the prestressing in the lamination stack. The stress stiffening effect is taken into account by the K_P matrix (1) only for the hollow cylinder. The measurement is performed

on the assembled structure; therefore, the identified parameters implicitly take into account the prestressing which is of the same magnitude for each rotor presented in Section III. Since the short-circuit rings, the lamination stack and the shaft ends connected to each ring are drilled at their periphery for the short-circuit rods and tie rods, (2) is also used to model the cross section of these elements.

III. OPTIMIZATION STRATEGY

The equivalent constitutive properties of the lamination stack are denoted $x \in \mathbb{R}^n$ so that $\{x\}_{p=1,\dots,n}$. The optimization parameters, stemming from the following doublet:

$$\{E, G\} \quad (3)$$

where E and G are the Young and the shear moduli, respectively, and they are also independent for modeling the anisotropy of the lamination stack, as described in [5]. The optimization parameter number is therefore equal to two, i.e., ($n = 2$). The identification strategy consists in minimizing the difference between the predicted and measured modal data.

A. Modal Error Functions

An optimization algorithm is used so that the optimization parameters of an FE model make the predicted data tend toward target values, i.e., measured data. Let x^i be the vector of optimization parameters x at iteration i . Let us assume that all the variables of the FE model depend on x^i . Let $\tilde{\omega}_k^i$ and ω_k be the predicted and measured natural frequencies, respectively. Let $\tilde{\varphi}_k^i$ and φ_k be their associated mode shapes projected on the same spatial basis. The first modal error function is based on the difference between measured natural frequencies ω_k and predicted natural frequencies $\tilde{\omega}_k^i$ for each mode shape k ($k = 1, 2, \dots, m$) [8]

$$F_k^\omega(x^i) = \frac{\tilde{\omega}_k^i}{\omega_k} - 1. \quad (4)$$

When performing modal tests, the MAC method is that most commonly used for estimating the correlation of measured mode shapes. It provides a matrix $M_{jl} = \text{MAC}(\tilde{\varphi}_j, \varphi_l)$ of scalar products between two sets of mode shapes φ_l ($l = 1, 2, \dots, m$) and $\tilde{\varphi}_j$ ($j = 1, 2, \dots, m$), denoted as follows:

$$\text{MAC}(\tilde{\varphi}_j, \varphi_l) = \frac{(\tilde{\varphi}_j \cdot \varphi_l)^2}{(\tilde{\varphi}_j \cdot \tilde{\varphi}_j)(\varphi_l \cdot \varphi_l)}. \quad (5)$$

Usually, two mode shapes φ_l and $\tilde{\varphi}_j$ are considered identical if M_{jl} is higher than 0.9, close together if $M_{jl} > 0.7$ or 0.8 depending on measurement accuracy. For each pair of measured and predicted modes $k = 1, 2, \dots, m$, let a second modal error function be defined as follows:

$$F_k^{\varphi D}(x^i) = 1 - \text{MAC}(\tilde{\varphi}_k^i, \varphi_k). \quad (6)$$

On the strength of the orthogonality property of the mode shapes, a perfect correlation between two sets of mode shapes

requires that all the extra-diagonal terms of the MAC matrix vanish. Thus, a third modal error function can be defined [9]

$$F_k^{\varphi \text{ED}}(x^i) = \sum_{j=1, j \neq k}^m |\text{MAC}(\tilde{\varphi}_j^i, \varphi_k) - \text{MAC}(\varphi_j, \varphi_k)|. \quad (7)$$

A fourth modal error function can be defined by estimating the difference between two sets of mode shapes by simply calculating the sum of the absolute values of differences between the modal vector components. However, it is essential that the pair of measured and predicted mode shapes are normalized equally and signed so that the larger component is equal to unity

$$F_k^{\varphi \text{EC}}(x^i) = \frac{1}{r} \sum_{j=1}^r \left| \frac{(\tilde{\varphi}_k^i)_j}{\max_l ((\tilde{\varphi}_k^i)_l)} - \frac{(\varphi_k)_j}{\max_l ((\varphi_k)_l)} \right| \quad (8)$$

where j stands for the j th vector component whereas r is the number of vector components. The identification method is then reduced to the minimization of a global error functional $f(x^i)$ with respect to optimization parameters vector x^i including n parameters. The global error functional can be expressed as a function of the previous four modal error functions

$$f(x^i) = \frac{1}{2} \|F^{\text{Tot}}(x^i)\|^2 = \frac{1}{2} \sum_{k=1}^q [F_k^{\text{Tot}}(x^i)]^2, \quad q = 4 \times m \quad (9)$$

with

$$F^{\text{Tot}}(x^i) = [\alpha^\omega F^\omega, \alpha^{\varphi D} F^{\varphi D}, \alpha^{\varphi \text{HD}} F^{\varphi \text{HD}}, \alpha^{\varphi \text{Ec}} F^{\varphi \text{Ec}}]^T. \quad (10)$$

Weight coefficients α (10) permit controlling the order of each function as they are very different from each other. Thus, a weighting coefficient linked to a modal error function is defined as the inverse of the mean value of this modal error function components calculated at the first iteration, i.e., $i = 0$. We propose defining each weight coefficient α (10) as follows:

$$\alpha = 1/\overline{F(x^0)}. \quad (11)$$

To avoid numerical conditioning problems (a 10^{12} ratio between the Young modulus and the Poisson ratio), particularly for the Jacobian matrix $J(x^i)$ (12), the x^i are defined relative to reference values such as the initial values of optimization parameters x^0 . This functional is minimized by using the Levenberg–Marquardt algorithm, which is generally acknowledged as being very robust and highly efficient in a wide range of problems

$$\begin{cases} x^0, \lambda_0 \text{ given} \\ d_i = -(H_i + \lambda_i I)^{-1} \nabla f, \\ x^{i+1} = x^i + \rho_i d_i \end{cases} \quad \left| \begin{array}{l} \nabla f = J(x^i)^T F^{\text{Tot}} \\ H_i \approx J(x^i)^T J(x^i) \end{array} \right. \quad (12)$$

where I and H_i are, respectively, the identity and the approximate Hessian matrices of size $[n \times n]$. If $\lambda_i \rightarrow +\infty$, the method tends toward the steepest descent method, whereas if $\lambda_i \rightarrow 0$, the method tends toward the Gauss–Newton method. Updating damping parameter λ_i is done by calculating

a “gain factor,” i.e., the ratio of the $f(x^i)$ decrease over the F^{Tot} decrease, as vector F^{Tot} is expanded by a Taylor series. Descent step ρ_i can be obtained by a “Line Search” algorithm. The method proposed by [16] is used here by setting $\rho_i = 1$ and frequently updating λ_i . This results in smoother performance and faster convergence than that achieved by Marquardt’s updating strategy.

B. Eigenderivatives

The Jacobian matrix $J(x^i)$ (of size $[q \times n]$) of the total error vector F^{Tot} implicitly depends on eigenelements λ_k and $\tilde{\varphi}_k$ defined in (1), λ_k being equal to the square of the k th angular frequency ω_k . Assuming that the eigenvectors are normalized with respect to the mass matrix M

$$\tilde{\varphi}_k^T M \tilde{\varphi}_k = 1, \quad k = 1, \dots, m. \quad (13)$$

Taking partial derivatives of (1) and (13) with respect to an optimization parameter x_p yields the following governing equations for eigenvector derivatives [11]:

$$A_k \frac{\partial \tilde{\varphi}_k}{\partial x_p} = P_k \quad (14)$$

$$\tilde{\varphi}_k^T M \frac{\partial \tilde{\varphi}_k}{\partial x_p} = Q_k \quad \text{with} \quad Q_k = -\frac{1}{2} \tilde{\varphi}_k^T \frac{\partial M}{\partial x_p} \tilde{\varphi}_k \quad (15)$$

where

$$A_k = (K - \lambda_k M), \quad P_k = -\left(\frac{\partial K}{\partial x_p} - \frac{\partial \lambda_k}{\partial x_p} M - \lambda_k \frac{\partial M}{\partial x_p} \right) \tilde{\varphi}_k. \quad (16)$$

By premultiplying (14) by $\tilde{\varphi}_k^T$ and substituting (1) and (13), the eigenvalue derivative with respect to x_p is obtained from the relationship

$$\frac{\partial \lambda_k}{\partial x_p} = \tilde{\varphi}_k^T \left(\frac{\partial K}{\partial x_p} - \lambda_k \frac{\partial M}{\partial x_p} \right) \tilde{\varphi}_k. \quad (17)$$

The partial derivatives of global mass and stiffness matrices with respect to x_p are easily obtained by differentiating elementary mass and stiffness matrices (1). Concerning the eigenvector derivatives, the problem is that (14) is not invertible since the A_k matrix is of rank $(m - 1)$. The complete modal method assumes that the k th eigenvector derivative with respect to x_p can be expressed as follows:

$$\frac{\partial \tilde{\varphi}_k}{\partial x_p} = \sum_{j=1}^m c_j \tilde{\varphi}_j. \quad (18)$$

Substituting (18) and (14) and premultiplying by $\tilde{\varphi}_k^T$ gives

$$c_j = \frac{\tilde{\varphi}_j^T \cdot P_k}{\lambda_j - \lambda_k}, \quad j \neq k. \quad (19)$$

Equation (19) shows that the eigenvector derivative has a unique expression (Linear combination) in terms of all the system’s eigenvectors, excluding the k th one

$$\frac{\partial \tilde{\varphi}_k}{\partial x_p} = \sum_{\substack{j=1 \\ j \neq k}}^m c_j \tilde{\varphi}_j + c_k \tilde{\varphi}_k \equiv V_k + c_k \tilde{\varphi}_k. \quad (20)$$

TABLE I
SIZE AND INERTIAL CHARACTERISTICS OF THE TESTED ROTORS

Rotor	#1	#2	#3	#4	#5
Total Weight (kg)	240	830	1969	998	1704
Total Length (m)	1.15	2.02	2.61	2.03	2.24
D_{fer} (m)	0.248	0.346	0.439	0.346	0.439
L_{fer} (m)	0.375	0.610	0.910	0.850	0.750

By substituting (20) and (15), c_k can be obtained by

$$c_k = Q_k - \tilde{\varphi}_k^T M V_k. \quad (21)$$

This method is costly in terms of computation time because it requires knowing all the eigenvectors of the system. Thus, by substituting (20) in (14), [12] proposes removing the singularity of A_k by cancelling a component of V_k , (14) becomes invertible and part of the solution V_k is obtained. The complete solution is then given by (20) and (21). This method requires as many inversions of matrix A_k of size $[m \times m]$ as eigenvector derivatives needed. However, MGv rotors are considered as medium systems and the inversion of such matrices is not costly in terms of CPU time.

IV. INDUSTRIAL APPLICATIONS

Experimental modal analyses were conducted on five MGv rotors denoted as Rotor#1 through Rotor#5 whose total lengths and weights are presented in Table I. Rotor#1 is the rotor presented in [15]. Length L_{fer} and diameter D_{fer} (Figs. 1 and 2) of the core vary from rotor to rotor, as shown in Table I. The rotors were hung from a crane via a flexible sling and a swivel hoist ring to achieve free-free boundary conditions at best. The hanging rotors were radially excited along a meridian line with an impulse force hammer (KISTLER Type 9726A20000 of mass 0.5 kg), with the transmitted force being measured by a load cell. A steel impact tip was used to observe a large frequency spectrum. Meridian lines were discretized in fine experimental meshes to establish accurate mode shapes. Sets of 62, 81, 73, 68, and 89 measurement points were defined for Rotor#1 through #5, respectively. The successive accelerances obtained with a dynamic analyzer permit evaluating the measured natural frequencies. The mode shapes are plotted by exploring the imaginary part of the accelerances.

Identification procedures were performed by updating the FE models of each rotor, as described in Sections II and III. A minimum of four modes were retained to ensure sufficient measured modal data to preserve the dynamics of the rotors studied. Poisson ratio was fixed at 0.28, as in [6]. Thus, for each rotor, the optimization problem contains two unknowns $\{E, G\}$, the Young and shear moduli, respectively. Five sets of constitutive properties have been identified and are presented in Table II. The normalized values are reported and defined as follows:

$$E^* = \frac{E}{\bar{E}}, \quad G^* = \frac{G}{\bar{G}}, \quad L^* = \frac{L_{\text{fer}}}{\bar{L}_{\text{fer}}}, \quad D^* = \frac{D_{\text{fer}}}{\bar{D}_{\text{fer}}} \quad (22)$$

where $\bar{E}$ and $\bar{G}$ are the mean values of the identified Young and shear moduli, respectively. Consequently, $\bar{L}_{\text{fer}}$ and $\bar{D}_{\text{fer}}$ are

TABLE II
IDENTIFIED DIMENSIONLESS EQUIVALENT CONSTITUTIVE PROPERTIES

Rotor	#1	#2	#3	#4	#5
E^*	0.65	1.05	0.83	1.59	0.88
G^*	0.43	0.27	0.74	2.21	1.34

Fig. 4. Evolution of the β parameter versus the σ the parameter.

the mean values of the magnetic core lengths and diameters in order to obtain dimensionless variables.

To evaluate a correlation between the identified constitutive properties and the rotor sizes, the first step is achieved by using coefficient a (23) which characterized the shear effect in the FE model, as defined in [18]. It can be seen as the ratio of the bending and the shearing rigidities and tends to a low value for slender structures and to a high value for monolithic structures. Let β and σ be the numerator and the denominator, respectively, of coefficient a . They are defined as follows:

$$a = \frac{12EI}{GS_r L^2} \sim \frac{E^* D^{*2}}{G^* L^{*2}} = \frac{\beta}{\sigma} \quad (23)$$

where L , S_r , I are the characteristic length, reduced area, and second moment of inertia of the magnetic core, respectively. Fig. 4 shows the evolution of parameter β versus parameter σ . This representation shows that the identified bending rigidity of the magnetic core increases with the associated identified shear rigidity. Moreover, the identified bending rigidity seems to be very sensitive to low values of the identified shear rigidity while it tends to increase slowly for high values of the identified shear rigidity.

The second step is carried out by plotting the normalized identified Young modulus E^* weighted by L^{*2} as a function of $D^{*2}L^*$, a classical parameter used in electromagnetic design. Fig. 5 shows that E^*/L^{*2} decreases quasi-linearly with the $D^{*2}L^*$ parameter. This behavior probably signifies an exponential decrease, since the normalized identified Young modulus E^* cannot be negative for a high value of $D^{*2}L^*$. This means that for a given parameter $D^{*2}L^*$, a Young modulus can be found for the lamination stack. Therefore, a shear modulus can be associated, by using the curve shown in Fig. 4.

The first four predicted and measured natural frequencies are given in Table III while the predicted and measured lateral

Fig. 5. Evolution of the normalized identified Young modulus weighted by L^{*2} versus the $D^{*2}L^*$ parameter.

TABLE III
FIRST FOUR PREDICTED AND MEASURED NATURAL FREQUENCIES

Rotor#1	1 st	2 nd	3 rd	4 th
Measured	856 Hz	1230 Hz	1713 Hz	2330 Hz
Predicted	844 Hz	1285 Hz	1741 Hz	2279 Hz
Error	1.4 %	4.5 %	1.6 %	2.2 %
Rotor#2	1 st	2 nd	3 rd	4 th
Measured	426 Hz	610 Hz	953 Hz	1243 Hz
Predicted	423 Hz	677 Hz	898 Hz	1216 Hz
Error	0.9 %	10.9 %	5.7 %	2.2 %
Rotor#3	1 st	2 nd	3 rd	4 th
Measured	247 Hz	440 Hz	766 Hz	1143 Hz
Predicted	242 Hz	470 Hz	749 Hz	1133 Hz
Error	1.9 %	6.7 %	2.2 %	0.9 %
Rotor#4	1 st	2 nd	3 rd	4 th
Measured	435 Hz	735 Hz	1228 Hz	1802 Hz
Predicted	421 Hz	798 Hz	1190 Hz	1783 Hz
Error	3.4 %	8.5 %	3.1 %	1.0 %
Rotor#5	1 st	2 nd	3 rd	4 th
Measured	342 Hz	676 Hz	1121 Hz	1624 Hz
Predicted	343 Hz	666 Hz	1093 Hz	1655 Hz
Error	0.2 %	1.5 %	1.6 %	1.9 %

mode shapes are shown in Figs. 6–10. The relative errors between the predicted and measured frequencies vary from 0.2% to 10% with a mean value equal to 3.1%. Figs. 6–10 show a good correlation between the predicted and measured mode shapes. Therefore, the identification method presented is more accurate than classical identification methods when considering restrictive assumptions on the mechanical behavior of a lamination stack mode of isotropic material. It shows that the FE model presented here is an efficient means of prediction the dynamics of this kind of real assembled structure.

V. CONCLUSION

The proposed optimization procedure was tested on several industrial induction motors with complex designs. An FE model

Fig. 6. First four (solid line) predicted and (dashed line) measured lateral mode shapes of the Rotor#1.

Fig. 7. First four (solid line) predicted and (dashed line) measured lateral mode shapes of the Rotor#2.

Fig. 8. First four (solid line) predicted and (dashed line) measured lateral mode shapes of the Rotor#3.

was presented taking into account that MGVS are assemblies made of different components including in particular a magnetic core. The prestressed tie rods were also modeled. It was

Fig. 9. First four (solid line) predicted and (dashed line) measured lateral mode shapes of the Rotor#4.

Fig. 10. First four (solid line) predicted and (dashed line) measured lateral mode shapes of the Rotor#5.

shown that the identified equivalent constitutive properties of the lamination stack, i.e., its stiffness, depend on the rotor sizes. This procedure is very useful for formulating an FE model mainly based on beam elements containing few DOF, which is a great advantage for rotordynamics prediction, i.e., unbalanced and transient responses. The reliability of such a procedure will allow predicting the dynamic behavior of an MGVS under development, operating at 6000 r/min in the 30-MW range. This will permit the manufacturer to increase the reliability of this range of products.

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