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Dynamic modelling for a submerged freeze microgripper using thermal networks

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Abstract. The growing interest for micromanipulation systems requires efficient, reliable and flexible handling strategies. Recent studies have demonstrated that performing manipulations and assembly in liquid surroundings is more advantageous than in dry conditions, especially when objects are under 100 µm in size. The thermally actuated ice microgripper proposed and analysed in this paper is designed to operate in a completely submerged manner in an aqueous medium. The handling principle which benefits from adhesive properties of ice, its thermal control principle based on Peltier effect, some features of the prototype, and the first micromanipulation tests are summarized. This paper is focused on the modelling of the thermal microhandling system using electrical analogy. The submerged microgripper is split into different subsystems which are studied in order to identify their thermal network. Then they are interconnected to build the whole thermal network of the submerged microgripper. This model is validated by comparison with experimental measurements. Controlling the temperatures involved in our device will be the purpose of further works.

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Thermal networks for a microgripper

1. Introduction

A trend grows since several years towards the automation of manipulation and assembly processes in the micro scale, i.e. typically between one micrometer and one millimeter. Their main applications are microrobotics, biological manipulations, optical, mechanical, or electrical microcomponents assembly. One of the common problems is the development of reliable and high accuracy handling strategies [1], particularly during the release phase. Without properly releasing strategies, this process can be very tedious and time-costly [2,3]. When the dimension of the object is under 100 µm, the release phase is strongly disturbed by the surrounding medium [3–6]. A comparative modelling of micromanipulation conditions in dry and liquid media, considering surface forces, contact force and hydrodynamic force, shows that manipulating in submerged conditions is more favorable than in dry conditions [7–9]. Firstly, capillary force is completely cancelled in submerged conditions. Secondly, contact force (pull-off force) and surface forces (van der Waals force, electrostatic force) reduce significantly in liquid medium. Thirdly, hydrodynamic force increases in submerged environment. These phenomena have two important consequences: they reduce drastically electrostatic and adhesion perturbations, and they limit the maximal velocity of the micro-objects and thus reduce their loss rate.

We developed a novel thermally controlled phase changing (liquid-solid) microgripper able to work in an aqueous medium. Its principle is detailed in [10] and summarized below. Current ice grippers act in air and its miniaturization is usually limited by the capillary force [11–16]. The dimensions of gripped objects are typically bigger than 200 µm and the main applications are optical, mechanical, or electrical microcomponents assembly [13]. Their thermal principle is based either on Peltier effect, or Joule-Thompson effect. As they work in air, water must be provided by an external device. Capillary force appears during the release because water does not evaporate completely. Then, they have to be combined with other release strategies to detach manipulated objects. In addition, they must work with particular environmental conditions like low temperature and low humidity [11,17].

Features of capillary grippers [18–21] and droplet based microgrippers [22, 23] are similar to cryogenic grippers. These strategies are conceived as non-destructive manipulation methods, causing no mechanical damage to the object. Many external release techniques have been tested to facilitate object release [21]. In addition, numbers of efforts are done searching for controlling the contact angle between the liquid bridge and the gripper surface, and the liquid bridge and the substrate, including regulating the liquid volume [24,25], controlling the gripper surface [18,20], and electrowetting [21,26]. None of them is general or versatile enough being necessary deep analysis and new strategies. Miniaturization is also limited because of the adhesion perturbations during the release phase.

The handling abilities of the cryogenic grippers are almost independent of the object shape. They provide high holding forces (≈ 0.1 N-100 N [11,27,28]) but local stresses
can also be very high, damaging delicate micro-objects. It is recommended that the manipulated microcomponent can withstand low temperatures and should not be liable to rust. Inserting it into the water container, recuperating it, and drying it will be analyzed. In addition, the water temperature must be relatively close to the fusion temperature ($< 283$ K).

Our microgripper takes particularly advantages of the cancellation of the capillary force in submerged medium. Consequently, it can be efficiently used to manipulate objects whose size is smaller than 100 $\mu$m.

A study of the thermal exchanges in the submerged ice microgripper is necessary to predict and control its performances. In this paper we propose to develop the complete model using electrical analogy. Electrical analogy has been largely used in several areas with good results [29–34].

This paper is composed of the following sections: section 2 presents the handling and thermal principles of the submerged ice microgripper and the features of the prototype; thermal modelling via electrical analogy of the Peltier modules and the MicroPelt’s heat sink is treated in section 3; ice generation is analyzed in section 4; finally, the dynamic thermal model of the whole microgripper is built and experimentally validated in section 5.

2. The submerged ice microgripper

A prototype of the submerged freeze microgripper has been developed. This section presents the handling and thermal principles, and the physical and technical features. It summarizes the detailed description proposed in [10].

2.1. Handling Principle

The handling principle of the submerged freeze microgripper uses adhesive properties of ice as shown in figure 1. First, the gripper approaches the micro-object without touching it. Secondly, an ice microvolume is generated and holds the micro-object. This latter can then be moved and positioned. Finally, the ice microvolume is thawed liberating the micro-object without any capillary force influence because ice mixes with water surroundings.

Liquid environment is thus exploited to generate the ice microvolume, and to avoid capillary force during the release.

2.2. Thermal Principle

The energy required to generate the ice microvolume of the submerged gripper is provided by two Peltier modules. When an electrical current is applied to the Peltier module, it generates heat on the hot face and absorbs heat on the cold face. The heat flux is proportional to the current. The hot face is usually associated to a heat sink in
order to dissipate the heat flux.

The submerged freeze system consists of two Peltier modules and a forced convection system as illustrated in figure 2. The first stage contains a Peltier micromodule named MicroPeltTM ($\mu P$). The ice microvolume is generated on its cold face. In order to actively decrease the temperature at the MicroPelt’s heat sink, a second Peltier element is connected. We called it MiniPeltier ($mP$). The temperature at its hot face is maintained at the ambient temperature by forced convection.

The MicroPelt is completely submerged while the MiniPeltier and the forced convection system stay in air to dissipate heat outside water.

2.3. Physical and Technical Features

Figure 3 shows the first prototype of the submerged freeze microgripper.

The dimensions of the MicroPeltTM (Infineon Technologies AG) are: $720 \times 720 \times 428$ $\mu m^3$. Its hot face is fastened to a copper heat sink (MicroPelt’s heat sink). The MiniPeltier (Melcor FC0.6-18-05), which dimensions are $6.2 \times 6.2 \times 2.4$ mm$^3$, is fixed on its cold face to the MicroPelt’s heat sink and on its hot face to the copper heat sink of the cooling liquid system.
Concerning power consumption, for optimal conditions operations, the MiniPeltier and the MicroPelt require 1.6 W and 0.1 W, respectively. The submerged freeze microgripper requires low power consumption compared to microgrippers using other common actuation methods (electrostatic, piezoelectric, shape memory alloy effect, etc.) [35].

Pick and place operations of a silicon micro-object (600 × 600 × 100 µm³) are described in [10].

Under water, the maximal lifting force can be estimated with good accuracy only by knowing the contact surface between the ice droplet and the object, and the gripping strength of ice (typically around 1 N/mm²) [11,13,28,36]. Considering the MicroPelt’s cold surface (0.52 mm²) as the contact surface, this force is around 0.52 N.

3. Thermal modelling by electrical analogy

Predict and control the temperature distribution in the submerged freeze microgripper require a complete study of the heat exchanges. Equivalent electrical models, so-called thermal networks, seem a relatively simple, but sufficiently accurate and powerful tool for simulating real thermal systems [29,32–34]. Furthermore, elementary thermal networks can easily be connected together. We use this faculty to split the submerged microgripper in different subsystems. The thermal networks of each subsystem considered is built and identified. They are then interconnected with the others, in order to build the complete thermal network of the microgripper. Classical equivalences between thermal and electrical systems are summarized in table 1.

The submerged freeze microgripper can be schematized as presented in figure 4, where: (a) corresponds to air; (w) corresponds to water; (1) denotes the junction between the forced convection system and the MiniPeltier’s hot face; (2) represents the junction between the MiniPeltier’s cold face and one side of the MicroPelt’s heat sink; (3) is the junction of the MicroPelt’s hot face and its heat sink; (4) is the MicroPelt’s...
Table 1. Thermal and electrical analogy

<table>
<thead>
<tr>
<th>Thermal system</th>
<th>Equivalent electrical system</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heat flux $Q$</td>
<td>Current $i$</td>
</tr>
<tr>
<td>Temperature difference $\Delta T$</td>
<td>Voltage difference $\Delta V$</td>
</tr>
</tbody>
</table>

cold face; and (5) represents the surface of the ice microvolume in contact with water. These notations will be used to identify the parameters of the thermal networks.

According to [10], the forced convection system maintains constant the temperature of the MiniPeltier’s hot face $T_1$ at the ambient temperature $T_a$. Consequently, its thermal modelling corresponds to the expression: $T_1 = T_a$.

The structure and the identification of physical parameters of both Peltier modules (MiniPeltier and MicroPelt), and the MicroPelt’s heat sink’s thermal networks are presented in the following.

3.1. Thermal network of Peltier modules

A Peltier module’s thermal network, proposed by [12], is shown in figure 5. It consists of a current source $P_S = \alpha T_c i$ representing the Peltier effect, two current sources $P_{J/2} = Ri^2/2$ for the Joule effect, and a thermal resistance $R_{TH}$ which represents the conduction. The Peltier coefficient $\alpha$, the electrical resistance $R$ and the thermal conductance $k_P$ depend on the physical features of the Peltier module. $i$ is the applied electrical current; $T_h$ and $T_c$ are the temperatures at the hot and cold faces, respectively; $Q_h$ is the heat rejected by the hot face, while $Q_c$ represents the heat absorbed by the cold face.

Classical identification methods have been used to determine the MiniPeltier’s parameters. The MicroPelt’s parameters have been calculated on the basis of technical parameters provided by the constructor (Infineon Technologies AG). These data are summarized in table 2.
Thermal networks for a microgripper

3.2. Thermal network of the MicroPelt’s heat sink

The geometry and the thermal problem of the MicroPelt’s heat sink is shown in figure 6. MicroPelt’s hot face is fixed to surface (2), while MiniPeltier’s cold face is fixed to surface (3). As the length of the heat sink is larger than all the other dimensions, we consider that the variation of the temperature between surface (2) at temperature $T_2$, and surface (3) at temperature $T_3$ is unidirectional along axis $x$. Consequently, the heat flux $Q(x, t)$ between both surfaces is also unidirectional. Moreover, heat convection $Q_h$ takes place from all others surfaces and two different surroundings, air and water (see figure 4). External temperature $T_{\text{ext}}$ involves thus both external fluids temperatures, air temperature $T_a$ and water temperature $T_w$.

This thermal problem has been solved in [37]. Here, a dynamic thermal network for the MicroPelt’s heat sink is proposed (see figure 7): $R_{c0}$ is the thermal conduction resistance, $R_{v0}$ is the thermal convection resistance, $C_{\text{th}0}$ are the thermal capacitors, $T_{\text{ext}}$ is the external temperature, and $Q_2$ and $Q_3$ are the heat flux in surface (2) and (3), respectively. The expressions of this parameters in the case of a rectangular beam are proposed in [37]. As the MicroPelt’s heat sink is partially submerged, the external temperature $T_{\text{ext}}$ in the thermal network is the average temperature between the temperature of the water and the temperature of the air. The identification of the thermal resistances $R_{c0}$ and $R_{v0}$ and the temperature $T_{\text{ext}}$ have been obtained using experimental results in steady-state conditions. Thermal capacitors $C_{\text{th}0}$, which depend on the volume of the heat sink and the specific heat, have been calculated analytically.

3.2.1. Static thermal network parameters

In order to specify the static parameters $R_{c0}$, $R_{v0}$ and $T_{\text{ext}}$, the MicroPelt’s heat sink has been connected only to the MiniPeltier.
Thermal networks for a microgripper

(a) Geometry.

(b) Thermal problem.

Figure 6. MicroPelt’s heat sink.

Figure 7. Thermal network of the MicroPelt’s heat sink [37].

Identification method is based on the measurement of $T_3$ in function of the current in the MiniPeltier, $i_{mP}$.

As the MicroPelt is not fixed on its heat sink, surface (3) presents a convection heat transfer condition. Heat flux $Q_3$ is thus:

$$Q_3 = h_w S_3 (T_3 - T_w),$$

where $h_w = 1500 \text{ W/m}^2\text{K}$ is the convection coefficient in water and $S_3 = 4.9 \text{ mm}^2$ is surface (3).

According to the figure 7, temperatures $T_2$ and $T_3$ in steady-state can be written as:
Thermal networks for a microgripper

\[ T_2 - T_{\text{ext}} = \frac{R_{c0}((R_{c0} + R_{v0})Q_2 - R_{a0}Q_3)}{R_{c0} + 2R_{v0}} \]  
\[ T_3 - T_{\text{ext}} = \frac{R_{c0}(R_{c0}Q_2 - (R_{c0} + R_{v0})Q_3)}{R_{c0} + 2R_{v0}} \]  

(2)  
(3)

Introducing (1) in (3), \( Q_2 \) can be expressed as a function of \( R_{c0}, R_{v0}, T_{\text{ext}}, T_3 \) and \( T_w \):

\[ Q_2(T_3) = \frac{R_{c0} + 2R_{v0}}{R_{c0}}(T_3 - T_{\text{ext}}) + \frac{R_{c0} + R_{v0}}{R_{v0}}h_wS_3(T_3 - T_w) \]  
(4)

Inserting (1) and (4) in (2), \( T_2 \) is defined as a function of \( R_{c0}, R_{v0}, T_{\text{ext}}, T_3 \) and \( T_w \):

\[ T_2(T_3) = \frac{R_{c0}}{R_{c0} + 2R_{v0}}((R_{c0} + R_{v0})Q_2(T_3) - R_{c0}h_wS_3(T_3 - T_w)) + T_{\text{ext}} \]  
(5)

Considering the behavior of the thermal network in figure 5, \( Q_2 \) can be expressed as a function of \( T_1 = T_a \) and \( T_2 \):

\[ Q_2(T_3) = -(\alpha_{mP}i_{mP} + 1/R_{THmP})T_2(T_3) + R_{mP}i_{mP}^2/2 + T_a/R_{THmP} \]  
(6)

\( T_3 \) is the solution of (6) defined as a function of \( i_{mP}, R_{c0}, R_{v0}, T_{\text{ext}}, T_1 \) and \( T_w \). Parameters \( R_{c0}, R_{v0} \) and \( T_{\text{ext}} \) can be thus calculated from a non-linear system of equations with three different experimental couples \( (i_{mP}, T_3) \), knowing temperatures and \( T_w \) and \( T_a \), and MiniPeltier’s parameters \( \alpha_{mP}, R_{mP} \) and \( R_{THmP} \) done in table 2.

To perform the experimental measurements, the submerged freeze microgripper has been tested in real use conditions: the forced convection system and the MiniPeltier stay completely in air, while the MicroPelt’s heat sink is partially submerged. The MicroPelt has been removed allowing direct measurements on surface (3). For an applied current \( i_{mP} \), we measure temperature \( T_3 \) until its steady-state using a microthermocouple. Temperatures \( T_a = 295.5 \) K and \( T_w \) were also measured with a thermometer and a microthermocouple, respectively. Experimental ordered triple \( (i_{mP}, T_3, T_w) \) measured are shown in table 3.

Parameters \( R_{c0}, R_{v0} \) and \( T_{\text{ext}} \) verifying theses conditions are presented in table 4.

3.2.2. Analytical identification of the thermal capacitor  The thermal capacitor \( C_{th0} \) depends on the geometry of the heat sink and its physical properties:

\[ C_{th0} = \frac{\rho C_p V}{2} \]  
(7)
Thermal networks for a microgripper

Table 3. Experimental static values.

<table>
<thead>
<tr>
<th>(i_{mp}) (A)</th>
<th>(T_3) (K)</th>
<th>(T_w) (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>281.2</td>
<td>274.5</td>
</tr>
<tr>
<td>0.4</td>
<td>274.2</td>
<td>274.5</td>
</tr>
<tr>
<td>0.7</td>
<td>272.2</td>
<td>273.8</td>
</tr>
</tbody>
</table>

where \(\rho = 8960 \text{ kg/m}^3\) is the density of the copper heat sink, \(C_p = 385 \text{ J/(kg.K)}\) is the specific heat, and \(V = 278 \text{ mm}^3\) is the volume according to its geometry (see figure 6(a)).

The result obtained is shown in table 4.

Table 4. Parameters of the MicroPelt’s heat sink thermal network.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thermal conduction resistance (R_{c0})</td>
<td>3.3</td>
<td>K/W</td>
</tr>
<tr>
<td>Thermal convection resistance (R_{v0})</td>
<td>36.1</td>
<td>K/W</td>
</tr>
<tr>
<td>Thermal capacitor (C_{th0})</td>
<td>0.48</td>
<td>J/K</td>
</tr>
<tr>
<td>External temperature (T_{ext})</td>
<td>281.1</td>
<td>K</td>
</tr>
</tbody>
</table>

Thermal networks of the Peltier elements (MiniPeltier and MicroPelt) and the heat sink (figure 5 and figure 7) are completely defined. A model of the ice generation is proposed in the next section.

4. Thermal networks of ice generation

The thermal model of ice generation describes heat exchanges between MicroPelt’s cold face and water. On the one hand, the evolution of heat flux \(Q_4\) and temperature \(T_4\) at the MicroPelt’s cold face depend on the applied current \(i_{mp}\) and the temperature \(T_3\) at the MicroPelt’s hot face; on the other hand, the evolution of the ice thickness \(H_{ice}\) depends on \(Q_4\) and \(T_4\). Here, two cases are studied: (i) thermal problem when an ice microvolume is grown, (ii) thermal problem at the MicroPelt’s cold face without ice. Next analysis deals with the thermal network in each case, and the equations describing the corresponding phenomenon.

4.1. Thermal problem with ice

The generation of ice is done when the temperature \(T_4\) at the cold face of the MicroPelt and the melting point of water \(T_f\) have the same value \((T_4 = T_f)\). As the thickness of the ice is very small, this temperature is considered uniform at temperature \(T_f\):

\[
T_4 = T_5 = T_f
\]  (8)
Thermal networks for a microgripper

where temperature $T_5$ is the temperature of the ice in contact with water.

We consider that this surface is a circle instead a square to build an analytical model. Its diameter $d_{\mu P} = 812 \, \mu m$ is calculated in order to have the same surface $S_4$ of the experimental system.

After experimental observations, we consider that the microvolume of ice has a spherical calotte geometry (figure 8). Its volume $V_{\text{ice}}$ and the surface $S_5$ in contact with water are:

$$
V_{\text{ice}} = \frac{\pi H_{\text{ice}}}{24} (3d_{\mu P}^2 + 4H_{\text{ice}}^2) \tag{9}
$$

$$
S_5 = \frac{\pi}{4} (d_{\mu P}^2 + 4H_{\text{ice}}^2) \tag{10}
$$

![Figure 8. Geometry of the ice microvolume (lateral view).](image)

The surface of the ice microvolume in contact with water has a heat convection flux $Q_5$ with the water:

$$
Q_5 = \frac{1}{Z_{\text{ice}}} (T_f - T_w) \tag{11}
$$

where $Z_{\text{ice}} = h_w S_5$ is a variable and non-linear thermal impedance which depends on height of the ice $H_{\text{ice}}$ (see(10)).

The evolution of the ice’s height is a function of the difference between $Q_5$ and $Q_4$, which is absorbed by latent heat:

$$
\rho_{\text{ice}} L_f \frac{dV_{\text{ice}}}{dt} = Q_5 - Q_4 \tag{12}
$$

where $\rho_{\text{ice}}$ is the ice density and $L_f$ is the water’s latent enthalpy of fusion.

Considering (9) and (11), the temporal variation of ice thickness $H_{\text{ice}}$ in relation with temperatures $T_f$ and $T_w$, and heat flux $Q_4$ is:

$$
\frac{dH_{\text{ice}}}{dt} = \frac{1}{\rho_{\text{ice}} L_f} \left(2h_w (T_f - T_w) - \frac{8Q_4}{\pi (d_{\mu P}^2 + 4H_{\text{ice}}^2)} \right) \tag{13}
$$

This equation allows to calculate the height of the ice $H_{\text{ice}}$ at every time $t$ and thus to determine the variable impedance $Z_{\text{ice}}$. 
4.2. Thermal problem without ice

As MicroPelt is completely submerged in water without ice \(H_{\text{ice}} = 0\), a convection heat transfer takes place between the MicroPelt’s cold face and the medium:

\[
Q_4 = \frac{1}{R_{v4}}(T_4 - T_w)
\]

(14)

where \(R_{v4} = \frac{1}{(h_wS_4)}\) is the thermal convection resistance, \(h_w\) is the convective heat transfer coefficient of water, and \(S_4 = \pi d^2/4\) is the surface of the MicroPelt’s cold face.

The thermal behavior at the MicroPelt’s cold face without ice, can be thus represented as the equivalent electrical model in figure 9.

Modelling of thermal behavior at the MicroPelt’s cold face and non-linear growing of the ice microvolume is summarized in figure 9. Parameters of these thermal networks are presented in table 5.

![Figure 9. Thermal modelling of the ice generation using electrical analogy.](image)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>(R_{v4})</td>
<td>1637</td>
<td>K/W</td>
</tr>
<tr>
<td>(\rho_{\text{ice}})</td>
<td>920</td>
<td>kg/m³</td>
</tr>
<tr>
<td>(L_f)</td>
<td>330</td>
<td>kJ/kg</td>
</tr>
<tr>
<td>(T_f)</td>
<td>273</td>
<td>K</td>
</tr>
</tbody>
</table>

5. Thermal network of whole system

One of the advantages of thermal modelling using electrical analogy is the possibility of connecting the thermal networks of different subsystems. Here, we use this advantage to construct the whole thermal network of the submerged freeze microgripper connecting
Thermal networks for a microgripper

Figure 10. Thermal network of the submerged freeze microgripper.

The equivalent electrical models of its elementary components: the forced convection cooling system, the MiniPeltier, the MicroPelt’s heat sink, the MicroPelt, and the ice microvolume. The thermal network of the submerged freeze gripper are depicted in figure 10. This thermal network let us modelling the ice generation as a function of the electrical currents $i_{\mu P}$ and $i_{mP}$ of the MicroPelt and the MiniPeltier, respectively. It is able to provide easily a linear modelling of the ice microgripper which will be use to study the automatic control of this device. Next sections deals with the simulation of the whole thermal network and the experimental validation.

5.1. Simulation model

The thermal network of the submerged freeze microgripper has been simulated with Simulink™ and Matlab™, considering an ambient temperature $T_a = 295.5$ K, and a water temperature $T_w = 274.2$ K.

Figure 11 describes an example of a simulation result of the network presented in figure 10:

(a) temperatures $T_3$ and $T_4$ of the MicroPelt’s hot face and cold face are stationary; MiniPeltier’s current $i_{mP}$ and MicroPelt’s current $i_{\mu P}$ are zero ($i_{mP} = i_{\mu P} = 0$ A); and ice thickness is zero ($H_{ice} = 0$ $\mu$m);

(b) only the MiniPeltier is activated at 0.4 A ($i_{mP} = 0.4$ A). This value is always maintained in the following steps. Temperatures $T_3$ and $T_4$ reduces, $T_4$ stay always greater than melting point $T_f$: ice thickness stays zero ($H_{ice} = 0$ $\mu$m);

(c) the MicroPelt is activated at 0.5 A ($i_{mP} = 0.4$ A, $i_{\mu P} = 0.5$ A). Temperature $T_4$ falls and reaches melting point $T_f$ ($T_4 = T_f = 273$ K) producing ice generation ($H_{ice} > 0$ $\mu$m). Temperature $T_3$ increases slightly because of the MicroPelt;

(d) the MicroPelt is switched off ($i_{\mu P} = 0$ A), ice thaws and $H_{ice}$ reduces. Temperatures $T_4$ stays at melting point $T_f$ while $H_{ice} > 0$ $\mu$m. Temperature $T_3$ reduces slightly because of the MiniPeltier;

(e) the ice microvolume is completely thawed ($H_{ice} = 0$ $\mu$m) and $T_3$ grows. Electrical currents $i_{mP}$ and $i_{\mu P}$ are maintained to their previous values ($i_{mP} = 0.4$ A, $i_{\mu P} = 0$ A).
Figure 11. Evolution of MicroPelt’s current $i_{\mu P}$, MiniPeltier’s current $i_{mP}$, temperatures $T_3$ and $T_4$ at the MicroPelt’s hot face and cold face, respectively, and ice thickness $H_{\text{ice}}$. Signals obtained simulating the thermal network of the submerged freeze gripper.

5.2. Experimental behaviour

The experimental behavior of the submerged freeze gripper (upper view) has been filmed with CDD camera. Ice thickness $H_{\text{ice}}$ is manually measured for every image taken. Figure 12 depicted the experimental dynamic evolution of the electrical currents $i_{mP}$ and $i_{\mu P}$, and temperature $T_4$ form MicroPelt activation:

(a) MiniPeltier’s and MicroPelt’s currents are zero $i_{mP} = i_{\mu P} = 0$ A, and temperatures are stationary;
(b) the MiniPeltier is activated ($i_{mP} = 0.9$ A; $i_{\mu P} = 0.5$ A) to reduce MicroPelt’s heat sink temperature. This current is strongly dependent on experimental conditions (submerged surfaces, temperature and volume of water, etc.). During this experimentation, required $i_{mP}$ is bigger than this one required during simulation.
This value is maintained during all the experimentation. MicroPelt’s current stays at zero ($i_{\mu P} = 0$ A);

(c) MicroPelt is activated ($i_{\mu P} = 0.5$ A), water is locally get cold, but a supercooling phenomenon appears. Simulation does not consider this phenomenon, which induces a crystallization delays. During simulations, ice generation begins immediately after MicroPelt’s activation and $T_f$ is at 273 K;

(c’) ice generation takes place. First crystallization appears at time $t_4$, some seconds after current $i_{\mu P}$ sets up to 0.5 A, at $t_3$. This phenomenon, caused by supercooling as explained, is not observed during following crystallizations;

(d) MicroPelt’s current is inversed ($i_{mP} = -0.5$ A), MicroPelt’s hot face warms up and ice microvolume thaws;

(e) in order to repeat ice generation and thawing, a square signal $\pm 0.5$ A is applied to $i_{\mu P}$.

Figure 12. Experimental sequence of ice generation: evolution of ice thickness $H_{\text{ice}}$, MiniPeltier’s or MicroPelt’s currents $i_{mP}$ and $i_{\mu P}$, and temperature at the MicroPelt’s cold face $T_4$.

For the micromanipulation operations described in [10], the cycle time for pick up and release the micro-object is 10 s. This time could be reduced controlling the thickness of the ice droplet via, for instance, a visual control system directly acting over Peltier module’s currents. Moreover, the reduction of the size of both gripper and micro-object could enable the reduction of the thermal inertia, and thus the improvement of the time response.
5.3. Comparison between experimental and simulated ice

In order to validate the thermal network of the submerged freeze microgripper, measured and simulated ice thickness $H_{ice}$ have been compared. For this validation, temperature at the MicroPelt’s hot face $T_3$ has been fixed at 295 K at the simulator. Figure 13 shows the results of the comparison. Experimental and simulated behaviors follow the same trends. Three major differences can be identified.

First, simulation of the submerged freeze microgripper’s thermal network imposes the ice generation immediately after MicroPelt’s activation. For this reason, during the first crystallization, simulated current $i_{\mu P}$ is voluntary delayed against experimental $i_{\mu P}$ searching that measured and experimental $H_{ice}$ begin at the same time. This first crystallization is not representative of the sequential use of the gripper. During the following crystallizations, both, simulated and experimental currents have the same dynamics.

Second, thawing model does not represent the real phenomenon. During experiments, ice is detached of the MicroPelt’s cold face, contrary to simulation, where $H_{ice}$ decreases continuously.

![Figure 13. Comparison between ice thickness $H_{ice}$ and electrical current $i_{\mu P}$ obtained experimentally and simulating the thermal network of the submerged freeze microgripper.](image)
Third, it is obvious that simulated $H_{\text{ice}}$ is bigger than experimental $H_{\text{ice}}$. In fact, thermal networks of Peltier modules does not consider electrical contact resistances. These losses become bigger than Peltier effect showing that experimental heat flux provided by Peltier modules is lower than simulated heat flux: simulated ice microvolume is generated faster than experimental ice microvolume.

Fourth, the geometry of ice droplet has been modelled as a spherical calotte overcoming only MicroPelt’s cold face. Experimentally, ice volume is bigger than modelled volume. Consequently, real ice droplet takes more time to grow than simulated ice droplet.

Summarizing, the network model does not consider supercooling phenomenon, real thawing process, and contact resistances. Furthermore, simulated geometry of the ice droplet is smaller than real geometry. The two last limitations produce that simulated ice grows faster than experimental ice. In order to improve the network model, measurement concerning junction resistances and the real ice microvolume must be done.

Despite these differences, thermal network of the simulated submerged freeze microgripper lets follow ice generation in real time as a function of electrical currents of Peltier modules.

6. Conclusion

Modelling of complex thermal problems using electrical analogy presents several advantages as flexibility, precision real time calculation and easy connection of various models. We have thus developed a dynamical thermal network of the submerged freeze microgripper proposed in this article. This thermal network is based on the thermal networks of every elementary component: forced convection system, MiniPeltier, MicroPelt’s heat sink, and the MicroPelt. Identification of the thermal network’s parameters has been done by analytical calculations or based on experimentations. Thermal network of the submerged freeze microgripper is completed with an original non-linear thermal network of the ice generation. Connecting all these networks, we have built the thermal network of the whole submerged freeze microgripper. This network lets to observe real time ice generation as a function of electrical currents of both Peltier’s modules. Further work will deal with the use of this thermal network to design control strategies in order to enable automatic microgripping.

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