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Florent Morel, Jean-Marie Rétif, Xuefang Lin-Shi, Bruno Allard, Pascal Bevilacqua

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Florent Morel, Jean-Marie Réatif, Xuefang Lin-Shi, Bruno Allard, Pascal Bevilacqua
AMPERE — INSA de Lyon
Bâtiment Léonard de Vinci
21 avenue Jean Capelle
69 621 Villeurbanne Cedex
France
Email: florent.morel@insa-lyon.fr
Telephone: +33 4 72 43 82 38 — Fax: +33 4 72 43 85 30

Abstract—Many research efforts have been dedicated to matrix converters for several years. As major technological issues are now solved, this structure will widespread in industrial applications, in particular with AC motors. Current control is a key issue for AC motor drives, so many control schemes have been proposed. Some of them proposed at first for inverters, were applied to matrix converters. Among algorithms used with inverters, predictive control shows very good performances. In this paper a new control scheme is proposed for a matrix converter-fed permanent magnet synchronous machine. Literature about matrix converter technology and control and about predictive control for inverter-fed AC machines is reviewed. The proposed predictive control principle, the model of the whole machine-converter and the cost-function are detailed. The method offers a trade-off between the quality of motor currents and input power factor. Finally experimental results are reported. The feasibility and the effectiveness of the proposed method is assessed.

I. INTRODUCTION

A matrix converter is a set of bidirectional switches that directly connects a \( m \)-phase voltage source to a \( n \)-phase current source [1]. Generally \( m = n = 3 \), the voltage source is the supply and the current source is an AC machine. In this case, a matrix converter is an array of nine bidirectional switches arranged in a way that any input phase (phase of the voltage source) can be connected to any output phase (phase of the AC machine) (Fig. 1).

This structure is still not common in industry applications but it presents some attractive features. Firstly output voltage amplitude and frequency can be controlled and the input power factor can be set. Secondly it is bidirectional in power.

Back-to-back converters present equivalent features but matrix converters are all-silicon converters. So it achieves AC-AC conversion without any energy storage i.e. without a bulky and unreliable capacitor for DC energy storage. As a consequence matrix converters are a solution for applications with size [2] or reliability [3] constraints. Furthermore it has been shown [3] that the input filter that must be included has smaller inductances with a matrix converter than with a back-to-back converter.

Maximum fundamental output voltage without low frequency distortion is limited to 86% of the maximum input voltage. This is a drawback compared to back-to-back converters but it is not a crucial issue if the designer can choose the load and the converter structure at the same time.

As a bidirectional controlled-switch does not exist it has to be made with discrete components. Classically it is done with two diodes and two IGBT but it can change in the near future. Indeed, new devices like reverse blocking IGBT [4] and silicon carbide JFET [5] are (or will be soon) available and their use in matrix converters is promising. Some studies are performed for module integration [6, 7]. It shows the industrial interest for matrix converters and the bidirectional switch realisation will be no more an issue when these modules will be largely distributed.

As two input phases should never be short-circuited and any output phase should ever be opened, at any time, one and only one switch connected to an output phase must be closed. Due to its structure there is no free-wheeling path in a matrix converter. So commutation is an issue that can not be solved by dead times like with conventional inverters. Many semi-soft commutation sequences [8, 9] and control circuits [10] where proposed to solve this problem.

Two main technological issues of matrix converters (commutation and bidirectional controlled-switch realisation) are
now solved so matrix converters can be considered as serious competitors to conventional converters in the near future. But there is still a peripheral problem to solve in order to prove the matrix structure superiority: when an inappropriate commutation sequence happens (due to current sign detection error for example) or in case of a hard shutdown, an over-voltage that can be dangerous for semi-conductor devices can happen. So an over-voltage protection system must be added. A diode-clamp protection circuit with a capacitor is often used [11] but this solution is expensive and bulky. Some solutions have been proposed to address this issue including varistors [12], active clamping [13] or shutdown commutation sequences [14]. Although it seems that none of these solution is widely used.

Research efforts about matrix converters does not deal only with power electronics: control is widely studied. Like for conventional motor drives, different control schemes applied to matrix converter-fed AC machines are reported in the literature. Most of them are adapted from control schemes originally designed for conventional motor drives. Vector control is such an example; it is widely used. This control needs a special algorithm to convert voltage references to power switch duty-ratio values. There are several kinds of such algorithms.

The Venturini method [15] corresponds to a mathematical approach of this problem. It gives an analytical expression of duty-ratio values as functions of input voltages and desired output voltages. This method has two major limitations. First the knowledge of the load power factor is required to achieve the input power factor control at a value different of 1. Second the maximum input-output voltage ratio decreases severely when input and output power factors differ.

Space Vector Modulation (SVM) is another way to compute duty-cycle values [16]. The output voltage frame is divided into six sectors. The sector including the desired output voltage vector is determined. The same determination is performed within the input current frame. Knowing desired input current sector and output voltage sector, a table gives four converter configurations to use. The computation time is reduced compared to Venturini method one [17] and it leads to an input power factor control independent from the load power factor. The maximum input-output voltage ratio is the same whatever the load power factor.

Direct Torque Control (DTC) is another control scheme designed for conventional motor drives which has been applied to matrix converters [18, 19]. Torque and flux are controlled like with conventional DTC and the input power factor control is added. Experimental results are scarcely presented.

Some other control schemes use a virtual DC bus as an artifice [20, 21]. It allows to separate the control issue into two independent control schemes (one for the input, the second for the output).

Recently predictive control was successively applied to conventional motor drives [22, 23]. Superior performances compared to vector control or DTC are reported [24]. During transient operation, rise times with predictive control are smaller than with vector control and equivalent than with DTC. During steady state operation oscillation currents are significantly reduced compared to DTC. These results lead to port it to other converter structures. In this paper a new predictive control is applied to a matrix converter-fed Permanent Magnet Synchronous Machine (PMSM).

Firstly, used models for the PMSM, the matrix converter and the whole system are described. Then the cost function is explained and the control scheme steps are given. An experimental study is conducted in order to evaluate the influence of a tuning parameter in the cost function and in order to show the usefulness of matrix converter configurations that are not used by classical control schemes. Finally conclusions are given.

II. PROPOSED CONTROL SCHEME

In this paper, the presented predictive control consists in using a model of the whole converter - machine to predict the system behaviour after a computation period for each possible converter configuration. Then a cost function is used to determine the configuration that will be applied during the next computing period.

A. Permanent Magnet Synchronous Machine Model

The PMSM is classically modeled with state space equations in the dq rotor frame (1) where \( I_d \), \( I_q \) and \( V_d \), \( V_q \) are stator currents and voltages expressed in the \( dq \) frame, \( R \) and \( L \) are the stator winding resistor and inductance, \( \omega \) is the rotor angular speed and \( \phi \) is the flux produced by permanent magnets [25].

\[
\begin{bmatrix}
\dot{I}_d(t) \\
\dot{I}_q(t)
\end{bmatrix}
= \begin{bmatrix}
-\frac{R}{T} & \omega(t) \\
-\omega(t) & -\frac{R}{T}
\end{bmatrix}
\begin{bmatrix}
I_d(t) \\
I_q(t)
\end{bmatrix}
+ \begin{bmatrix}
\frac{T}{T} & 0 \\
0 & \frac{T}{T}
\end{bmatrix}
\begin{bmatrix}
0 \\
\omega(t)
\end{bmatrix}
\begin{bmatrix}
V_d(t) \\
V_q(t)
\end{bmatrix}
\phi(t)^T
\] (1)

Model parameters \( (R, L \) and \( \phi \) can be considered as constant and rotor electrical speed \( \omega \) variations can be neglected for a short sampling period \( T \) of the algorithm. Then the following model can be found with a first order Euler integration.

\[
\begin{bmatrix}
I_d(k+1) \\
I_q(k+1)
\end{bmatrix}
= \begin{bmatrix}
1 - \frac{RT}{T} & T\omega(k) \\
-T\omega(k) & 1 - \frac{RT}{T}
\end{bmatrix}
\begin{bmatrix}
I_d(k) \\
I_q(k)
\end{bmatrix}
+ \begin{bmatrix}
\frac{T}{T} & 0 \\
0 & \frac{T}{T}
\end{bmatrix}
\begin{bmatrix}
V_d(k) \\
V_q(k)
\end{bmatrix}
+ \begin{bmatrix}
0 \\
-\frac{T}{T}\omega(k)
\end{bmatrix}
\] (2)

This can be expressed as

\[
X(k+1) = A(k) \cdot X(k) + B \cdot V(k) + \Phi(k)
\] (3)

where \( X(k) = [I_d(k) \quad I_q(k)]^T \), \( A \) and \( \Phi \) depend on rotation speed.

\( V_d \), \( V_q \) must be expressed as functions of converter switching states in order to obtain a model of the whole converter - machine.

B. Matrix Converter Model

In the one hand \( V_d \), \( V_q \) can be expressed as functions of output voltages \( V_d \), \( V_q \), \( V_c \) using a rotation matrix

\[
R(\theta(k)) = \begin{bmatrix}
\cos(\theta(k)) & \sin(\theta(k)) \\
-\sin(\theta(k)) & \cos(\theta(k))
\end{bmatrix}
\] (4).

\[
\begin{bmatrix}
V_d(k) \\
V_q(k) \\
V_c(k)
\end{bmatrix}
= R(\theta(k)) \cdot \sqrt{\frac{3}{2}} \cdot \begin{bmatrix}
\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\
\frac{-1}{\sqrt{2}} & \frac{-1}{\sqrt{2}} & 0 \\
0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
V_d(k) \\
V_q(k) \\
V_c(k)
\end{bmatrix}
\] (4)

In the other hand output voltage can be expressed as function of input voltages with the following reasoning.
Let define $\lambda \kappa$ ($\lambda = A, B, C$ and $\kappa = a, b, c$) as the switch between phases $\lambda$ and $\kappa$. Let define $u_{\lambda \kappa}$ as an integer that represent the switch state with the following convention: if $u_{\lambda \kappa} = 0$ then the switch $\lambda \kappa$ is open; if $u_{\lambda \kappa} = 1$ then the switch $\lambda \kappa$ is closed.

In a matrix converter, among the three switches connected to an output phase, one and only one switch can be closed. Indeed if more than one switch is closed, there is a short-circuit of the voltage supply and if none is closed, there is no path for the output phase current. For example, for the phase $a$, this lead to

$$u_{Aa} + u_{Ba} + u_{Ca} = 1$$

and

$$u_{Aa} = 1 \Rightarrow V_a = V_A$$
$$u_{Ba} = 1 \Rightarrow V_a = V_B$$
$$u_{Ca} = 1 \Rightarrow V_a = V_C$$

then

$$V_a = u_{Aa}V_A + u_{Ba}V_B + u_{Ca}V_C$$

As a result output voltages can be expressed as function of input voltages with (8).

$$\begin{bmatrix} V_a(k) \\ V_b(k) \\ V_c(k) \end{bmatrix} = \begin{bmatrix} u_{Aa}(k) & u_{Ba}(k) & u_{Ca}(k) \\ u_{Ab}(k) & u_{Bb}(k) & u_{Cb}(k) \\ u_{Ac}(k) & u_{Bc}(k) & u_{Cc}(k) \end{bmatrix} \cdot \begin{bmatrix} V_A(k) \\ V_B(k) \\ V_C(k) \end{bmatrix}$$

Eq.5 can be written for phase $b$ and $c$; as a result there are 27 admissible switching configurations for a three-phase to three-phase matrix converter. These converter configurations can be divided into three groups.

In the first one, each output phase is connected to a different input phase (e.g. $u_{Aa} = u_{Ab} = u_{Ac} = 1$). The corresponding output voltage vectors have a constant amplitude and a variable direction. There is six configurations in this group.

In the second group, each output phase is connected to the same input phase (e.g. $u_{Aa} = u_{Ab} = u_{Ac} = 1$). There is three configurations in this group. They lead to a null output voltage vector.

Finally the eighteen other configurations are in the third group. Two outputs are connected to the same input (e.g. $u_{Aa} = u_{Ab} = u_{Bc} = 1$). The corresponding output voltage vectors have a constant amplitude and a variable direction.

It is worth to note that, for each paper cited in reference, the six configurations from the first group are not considered. Predictive control can use these configurations.

C. Model of the whole converter - machine

Firstly with (2), (4) and (8), if output currents, input voltages ($V_{in} = [V_A \ V_B \ V_C]$), angular position and speed are measured, it is possible to predict every possible state vector after a sampling period $X_n(k + 1)$ (1 $\leq n \leq 27$) for each possible converter configuration $U_n$ (9).

$$X_n(k + 1) = A(k) \cdot X(k) + B \cdot R(\theta(k)) \cdot C \cdot U_n(k) \cdot V_{in}(k) + \Phi(k)$$

Secondly as it is possible to achieve for currents a similar reasoning than the one used to demonstrate (8), it is also possible to predict input currents in a fixed frame $AB$ after a sampling period for each converter configuration (10).

$$\begin{bmatrix} I_{An}(k + 1) \\ I_{Bn}(k + 1) \end{bmatrix} = \frac{2}{3} \cdot \begin{bmatrix} 1 & -1 & -1 \\ 0 & -\frac{3}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix} \cdot \begin{bmatrix} V_A(k) \\ V_B(k) \end{bmatrix}$$

D. Cost Function

A cost function is used to determine which configuration must be applied. As the main goal of the control scheme is to control output currents, a first cost function that can be proposed is the sum of differences between the reference currents $I_{d,q}^\# $ and the predicted currents (11).

$$g_n = |I_d^\# - I_{dn}(k + 1)| + |I_q^\# - I_{qn}(k + 1)|$$

With this cost function, only output currents are controlled. However the matrix converter structure also allows to control input power factor. So input currents are computed with (10) in order to compute the angle between input current vector and input voltage vector if the configuration $n$ is applied ($\phi_{in}$). Then a third term is added in (11) to take into account input power factor and in order to make it as close to unity as possible (12).

$$g_n = |I_d^\# - I_{dn}(k + 1)| + |I_q^\# - I_{qn}(k + 1)| + c \cdot |\sin(\phi_{in}(k + 1))|$$

(12)

In (12) $c$ is a weighting factor. Actually the instantaneous angle between input current vector and input voltage vector is used as a way to act on input power factor.

With $c$, it is possible to obtain a trade-off between output current control and input power factor controls.

E. Control Scheme Steps

Figure 2 depicts the whole algorithm. At each sampling period input voltages, stator currents and angular position
are measured. Model components are then computed \((A(k), \Phi(k))\). State vector and input currents are predicted for the 27 appropriate converter configurations in order to compute a cost function. The converter configuration that minimize this cost function is applied for the duration of a sampling period.

III. EXPERIMENTAL STUDY

In addition to show the feasibility of the proposed scheme, experimental results are performed with the aim to show the influence of \(c\) and the usefulness of first-group configurations.

A. Hardware and Software

The test bench (Fig. 3) is composed of a laboratory-scale matrix converter including 18 IGBT. Semi-soft commutations are achieved with a board including a FPGA. Two identical PMSM (see parameters in Tab. I) are used; the first one is fed by the matrix converter, the other one is used as a load torque generator. An incremental encoder with 4096 points is used. Input voltages (400V, 50Hz) and output currents are measured.

An input filter is inserted between the matrix converter and the grid. As this filter is not included in the used model, its influence of this parameter.

The algorithm is implemented in C-language on a dSpace DS1104 controller board. This card provide a master processor: PowerPC 603e at 250MHz and and slave DSP TMS320F240 at 20MHz. The shortest sampling period that can be obtained with the proposed control scheme and this computation unit is 158\(\mu\)s. This is too large for a low power PMSM so 85mH inductances are added in series with the PMSM.

It is worth to note that these inductances emulate a higher-power machine. Actually they would be useless in the case of a high power machine (with smallest current dynamic) or if the computing duration was negligible compared to current rise time. In this regard the control scheme implementation using a FPGA [26] seems to be an interesting perspective since it could take advantage of the inherent parallelism of the algorithm (prediction of \(X_n(k+1)\) 27 times).

The ControlDesk environment is used to perform data recording and reference value tuning.

B. Experimental Conditions

A reference state vector \(X^\# = \begin{bmatrix} I_d^\# & I_q^\# \end{bmatrix}^t\) has to be determined for the proposed control scheme. For a PMSM the electromagnetic torque is proportional to \(I_q\), then the minimisation of the Joule power losses leads to fix the current \(I_d\) to zero. Consequently, reference values are \(I_d^\# = 0\)A and \(I_q^\#\) proportional to the desired torque \(T^\# = \frac{\pi \cdot \phi}{\mu \cdot d}\).

During experiments \(I_q^\#\) is is set to 5.75A in order to obtain the rated torque. Transient operations are obtained by changing the \(I_q^\#\) sign.

It is worth to note that the proposed control scheme is equivalent to a torque control. Indeed there is no speed loop. Generally torque controllers are used inside a speed loop. It is not the case in the presented experiments. Angular speed is not controlled, it is just an outcome of test bench mechanical parameters like inertia, frictions or load torque. During steady state operation this speed approximates 400rpm.

C. Influence of the value of \(c\)

Figures 4 to 8 illustrate the influence of \(c\). At first \(c\) is set to 0A; this is equivalent to only deal with output currents i.e. equivalent to not consider the instantaneous value of the input phase difference. The second value of \(c\) used during experiments is 1A; this quite large value is chosen to show the influence of this parameter.

When \(c\) is set to 0A, it can be seen that output phase currents (Fig. 4(a)) are very near to sinusoidal shapes but with a large value of \(c\) these currents (Fig. 4(b)) are significantly affected. Similar comments can be done when considering output currents expressed in the \(dq\) frame (Fig. 5) and output phase current spectra (Fig. 6). Indeed the larger the value of \(c\) the worst the output currents quality: current oscillations are significantly larger when \(c\) equals 1A. About transient operation it can be seen (Fig. 5) that, whatever the value of \(c\), the rise time is very short (near 2.5ms i.e. 15 sampling periods). Furthermore there is no overshoot and the static error is negligible.

During this transient operation angular speed grows from almost \(-400\)rpm to \(400\)rpm with the shape of an exponential function with a time constant close to 17ms (due to inertia, frictions… and not due to the presented control scheme). Then it can be seen that the control scheme features are independent from angular speed (Fig. 5).

Output current Spectra (Fig. 6) presents harmonics at low frequencies (at less that 500Hz) that are clearly larger when \(c\) is not null.

Advantages of a large value of \(c\) are clearly shown on figures 7 and 8. Input power factor is improved (Fig. 7) when

\[1\] Actually the instantaneous value of the cosine of the input phase difference
Fig. 4. Influence of $c$ on output voltage and output current

Fig. 5. Influence of $c$ on output currents in the $dq$ frame (transient operation)

Fig. 6. Influence of $c$ on output spectrum
the value of $c$ is large. Indeed the mean value is 0.374 when $c$ is zero and 0.914 when $c$ equals 1A.

The input filter is not considered in this study and this explains the high harmonic content of input currents (Fig. 7). It is obvious that, with a well-designed input filter\(^2\), input currents are nearly sinusoidal. When $c$ equals 1A, a fundamental component in phase with the input voltage can be seen in input current (Fig. 7(b)) while it is not the case when $c$ is zero (Fig. 7(a)). Thus the larger the value of $c$ the easier the input current filtering. This is confirmed by input current spectrum (Fig. 8). When the value of $c$ is large, low-frequency harmonics are reduced (particularly for orders 5 and 7).

D. Usefulness of first-group configurations

Similar experiments were performed without taking into account first-group configurations in order to show their usefulness (Fig. 9). It can be seen that output currents are affected: the oscillation amplitude is increased (Fig. 9(a)) and there is a significantly higher level of low frequency harmonics in output currents (Fig. 9(b)). Furthermore there almost no difference in input current spectra\(^3\) (with or without first-group configurations).

\[^2\text{This design depends on control scheme performances thus on the value of } c. \text{ This is a reason why input currents are not considered here.}\]

\[^3\text{These spectra are not shown in this paper due to the lack of space}\]

IV. CONCLUSION

A control scheme for a matrix converter-fed PMSM was presented and experimentally validated. It presents two characteristics: a weighting factor can be defined in the cost function and it can use converter configurations that are not taken into account by other control schemes.

The value of the weighting factor $c$ is very important. The larger $c$ the worst the output currents quality and the easier the input current filtering. Thus the control scheme designer must deal with this trade-off considering load and grid requirements.
The use of first-group configurations increases the amount of computations but leads to better output currents. This is an advantage over control schemes that use a pulse width modulation strategy for matrix converters - part I," IEEE Trans. Power Electron., vol. 49, no. 2, pp. 297–303, Apr. 2002.


REFERENCES


Fig. 9. Results when first-group configurations are not used (when c = 1/A)

The use of first-group configurations increases the amount of computations but leads to better output currents. This is an advantage over control schemes that use a pulse width modulation for example.

Further work will consist in including the input filter model in the model considered and to control grid currents together with output currents.