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Martian oxygen density at the exobase deduced from O I 130.4-nm observations by Spectroscopy for the Investigation of the Characteristics of the Atmosphere of Mars on Mars Express

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Several observations of the O I 130.4-nm triplet have been analyzed to determine the oxygen density in the Martian upper atmosphere using a three-dimensional Monte Carlo radiative transfer model describing each line of the triplet. Solar resonant scattering is the dominant source of excitation of the O I 130.4-nm triplet in the upper atmosphere of Mars. The atomic oxygen density at the exobase is found to be $1.2^{+1.2}_{-0.5} \times 10^{7}$ cm$^{-3}$ for solar zenith angles between 20° and 55° and to decrease by a factor of 2 for solar zenith angles between 55° and 90°. Although the major contribution to the observed brightness is produced above the exobase, it is possible to extrapolate the density profile below the exobase and to estimate the [O]/[CO$_2$] mixing ratio as 0.6–1.2% at 135 km. The major source of uncertainty comes from the uncertainty in the absolute calibration, as expected for an optically thick emission, and also, to a lesser degree, from the temperature at the exobase. The profiles are better reproduced by a large exospheric temperature (>300 K), which may suggest the presence of a hot oxygen population.

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1. Introduction

The 130.4-nm oxygen triplet is a common UV airglow emission of the terrestrial planets. It was observed for the first time in Earth’s upper atmosphere through rocket measurements [Chubb et al., 1958] but was also seen in the Venunean upper atmosphere [Moos and Rottman, 1971; Broadfoot et al., 1974; Bertaux et al., 1981] and in the Martian upper atmosphere [Barth et al., 1971; Feldman et al., 2000]. The first analyses of the Martian O I 130.4-nm triplet observed by the Mariner missions during high solar activity concluded that two mechanisms contribute to this emission: resonant scattering of solar photons and photoelectron impact excitation of atmospheric oxygen atoms [Strickland et al., 1972, 1973; Fox and Dalgarno, 1979]. The resonant scattering of the solar photons was shown to be the major source of excitation. Twenty years later a reanalysis of this emission was done [Stewart et al., 1992] using a more accurate radiative transfer model [Meier and Lee, 1982]. The photoelectron impact frequency was revised using the updated cross sections from Zipf and Erdman [1985] as well as an analytical relation between the $F_{10.7}$ solar activity index and the solar flux at 130.4 nm. Two thermospheric models were used in the study by Stewart et al. [1992]: an empirical thermospheric model [Stewart, 1987] and a Mars Thermospheric General Circulation Model (MTGCM) [Bougher et al., 1990]. The first model was used to reproduce the intensity by fitting the oxygen density, and the second model was used in order to reproduce the latitude and local time distribution. A mixing ratio [O]/[CO$_2$] of 0.7% at the 1.2-nbar level was found to provide the best fit of the measured intensity profile, while a ratio equal to 0.2% was found to provide the best fit of the latitude and local time variations. These ratios were slightly smaller than the earlier estimate of 1% by Strickland et al. [1972, 1973]. Another estimate of this ratio was made using Viking descent probe data obtained at low solar activity. Using a simple photochemical model, Hanson et al. [1977] calculated the best oxygen density profile able to reproduce the ion profiles measured by Viking and deduced a ratio [O]/[CO$_2$] equal to 1.25% at 130 km. The [O]/[CO$_2$] ratio is an important element in the global heat budget of the thermosphere. Indeed, atomic oxygen collisions with CO$_2$ molecules are known to be effective in exciting the CO$_2$ ($v_2$) vibrational state, resulting in an enhanced CO$_2$ 15-$\mu$m emission, which, in turn, leads to an enhanced cooling rate in the thermosphere [Bougher et al., 1994, 1999, 2000]. For example, a higher [O]/[CO$_2$] mixing ratio was suggested by Keating et al. [1998] in order to explain the discrepancy between the temperature deduced from Mars Global Surveyor (MGS) aerobraking data and the temperature calculated by the MTGCM model of Bougher et al. [1997] (120 K versus 150 K at 130 km).

In this paper we present an analysis of the 130.4-nm triplet measured by the Spectroscopy for the Investigation of the Characteristics of the Atmosphere of Mars–ultraviolet spectrometer (SPICAM-UVS) instrument [Bertaux et al.,...
Figure 1. Example of average spectrum below 150 km obtained by Spectroscopy for the Investigation of the Characteristics of the Atmosphere of Mars—ultraviolet spectrometer (SPICAM-UVS). A stray light is observed centered near 132 and 143 nm. The origin of this stray is still unknown. The dashed arrow indicates the expected position of the 130.4-nm lines. The oxygen 130.4 nm lines could correspond to the little bump on the left side of the stray light centered at 132 nm. SZA, solar zenith angle.

Table 1. Groups of Orbits Analyzed in This Study*

<table>
<thead>
<tr>
<th>Group</th>
<th>Date</th>
<th>Altitude (MEX, km)</th>
<th>SZA (MEX)</th>
<th>Range of Altitude (MNP, km)</th>
<th>Range of SZA (MNP, deg)</th>
<th>( F_{10.7} )</th>
<th>( F_{13.4} )</th>
<th>( L_s )</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>First part (1075, 1077, 1079, 1080)</td>
<td>19–21 Nov 2004</td>
<td>340–540</td>
<td>24–39</td>
<td>150–400</td>
<td>54–56</td>
<td>41.3</td>
<td>4.0</td>
</tr>
<tr>
<td>3</td>
<td>First part (1267, 1271, 1285)</td>
<td>12–17 Jan 2005</td>
<td>360–540</td>
<td>14–16</td>
<td>150–400</td>
<td>25–45</td>
<td>36.6</td>
<td>4.2</td>
</tr>
<tr>
<td></td>
<td>Second part (1267, 1271, 1285)</td>
<td>12–17 Jan 2005</td>
<td>360–570</td>
<td>59–63</td>
<td>150–400</td>
<td>55–72</td>
<td>36.6</td>
<td>4.2</td>
</tr>
<tr>
<td>4</td>
<td>First part (1349, 1350, 1357, 1374)</td>
<td>4–14 Feb 2005</td>
<td>720–1140</td>
<td>4–9</td>
<td>150–400</td>
<td>22–32</td>
<td>37.7</td>
<td>4.3</td>
</tr>
<tr>
<td>5</td>
<td>First part (1413, 1414)</td>
<td>22 Feb 2005</td>
<td>360–560</td>
<td>30–49</td>
<td>150–400</td>
<td>20–45</td>
<td>54.2</td>
<td>4.8</td>
</tr>
<tr>
<td></td>
<td>Second part (1413, 1414)</td>
<td>22 Feb 2005</td>
<td>370–560</td>
<td>79–97</td>
<td>150–400</td>
<td>77–100</td>
<td>54.2</td>
<td>4.8</td>
</tr>
</tbody>
</table>

*Mars nearest point (MNP) is the tangent point of the line of sight. The solar index \( F_{10.7} \) is calculated from the daily average from the National Geophysics Data Center. The solar flux at 130.4 nm \( (10^2 \text{ W m}^{-2} \text{ Hz}^{-1}) \) is calculated from the daily average Solar Radiation and Climate Experiment (SORCE) data. These calculations take into account the relative positions of Mars, Earth, and the Sun, the Sun rotation, and the Sun-Mars distance. \( L_s \) is the solar longitude. MEX, Mars Express; SZA, solar zenith angle.
does not change. On the contrary, less intense O I 130.4-nm and H I Lyman-α emissions are observed with increasing solar zenith angle (SZA) (when comparing Figures 2a and 2b or Figures 2c and 2d). Figure 3 displays an example of intensity profile showing how the O emission scale height changes with respect to the solar zenith angle.

3. Models of the Thermospheric and Exospheric Oxygen Densities and of the 130.4-nm Emission


Figure 2. Examples of average spectra near (a, b) 150 km and (c, d) 240 km. Spectra were obtained by SPICAM-UVS at solar zenith angles between 27° and 30° for Figures 2a and 2c and at solar zenith angles between 57° and 64° for Figures 2b and 2d. Each average spectrum corresponds to ~40–60 individual integrations of SPICAM-UVS. The oxygen triplet is the line at 130 nm. The Lyman-α line is also visible at 121.6 nm. These spectra correspond to groups 3a and 3b.

The diffusion coefficient $D_O$ of O atoms through a CO$_2$ atmosphere depends on the temperature:

$$D_O(r) = \frac{AT(r)}{n(r)},$$

where $n(r)$ is the total local density (O + CO$_2$), $T(r)$ is the local temperature [from Krasnopolsky, 2002], $A$ is equal to

![Figure 3. Altitude profiles of the O 130.4-nm emission intensity at high SZA (left curve) and low SZA (right curve) for group 3 (see Table 1 for the definition and observation parameters of this group).](image-url)
4.44 × 10^{17}, and s = 0.5 when \( D_O \) is expressed in cm\(^2\) s\(^{-1}\) [Banks and Kockarts, 1973]. According to Krasnopolsky [2002], the weak escape of oxygen at the exobase does not affect the density profile, so we neglect oxygen escape when calculating our thermospheric oxygen profiles.

[s] Above the exobase at 200 km, we use a one-dimensional (1-D) Chamberlain approach (without satellite particles) to describe the oxygen exospheric density. For this model, the oxygen density above 200 km depends only on the oxygen density and temperature at 200 km [Chamberlain, 1963]. We neglect any hot exospheric O components above the exobase, and we will only describe the effect of the core of the line on the intensity. Some possible effects of an oxygen hot population are given in section 4. As a consequence, the O density profile from 80 to 1000 km is fully determined knowing the oxygen density at a given altitude. The reference altitude for the density is chosen to be 80 km. Ten densities values at 80 km are used, varying from \( 1 \times 10^9 \) to \( 1 \times 10^{12} \) cm\(^{-3}\), which encompass the range of densities \((\sim 10^{10} - 10^{11} \text{ cm}^{-3})\) estimated from current photochemical models [Krasnopolsky, 2002; Fox, 2003]. Figure 4 displays four oxygen density profiles from 80 to 300 km, corresponding to densities \( 1 \times 10^9, 1 \times 10^{10}, 1 \times 10^{11}, \) and \( 1 \times 10^{12} \) cm\(^{-3}\) at 80 km. The exobase density at 200 km varies as a consequence, from \( \sim 1.5 \times 10^8 \) to \( 1.3 \times 10^8 \text{ cm}^{-3}\). The slight deviation of the proportionality between the density range at the exobase and the density range at 80 km comes from the fact that the hydrostatic and diffusive equations are not independent, since oxygen is a major constituent. The sensitivity of the density profiles with respect to the exobase temperature and eddy diffusion is studied in section 4.2. In the following, we will use either \( n_{exo} \) (density at the exobase) or \( n_{so} \) (density at 80 km) to define the model.

3.2. Excitation of the O I 130-nm Emission

[9] The 130-nm triplet (130.217, 130.486, and 130.603 nm) emission is produced from the radiative decay of the 3s^3S state to the ground 2p^3P state [Strickland and Donahue, 1970]. In this study, the two main sources of excitation of the 3s^3S states from the ground state are considered. These two sources of excitation are the resonant scattering of solar 130-nm photons and the photoelectron impact on O [Strickland et al., 1972, 1973; Stewart et al., 1992]. The radiative transfer calculation (described in Appendixes A and B) is performed for each source separately, and the sum of the two solutions is used to estimate the total emergent intensity that should have been observed by SPICAM-UVS. The emergent intensity due to the solar photons depends on the solar flux at 130 nm in each line of the triplet (130.2, 130.4, and 130.6 nm). The total flux of the solar lines is derived from the measurement of the Solar Spectral Irradiance (SSI) provided by the Solar Radiation and Climate Experiment (SORCE) database [Rottman et al., 2006]. We have scaled this flux to the Martian position and taken into account the phase angle Earth-Sun-Mars. The SORCE database provides the brightness measured between 130 and 131 nm. We assume that all the solar brightness measured is due to the solar O 130-nm lines. The estimate of the relative solar flux in each line and of the brightness at the center of each line is done by adopting the solar line shapes derived from the Solar Maximum Mission and the Orbiting Solar Observatory 8 for the time period 1975–1985 [Gladstone, 1992]. Each solar line at Mars is then approximated by a flat “boxcar” line shape of 5 Doppler units’ width, 5 \( \Delta \mu_{\text{ex}}(T_{\text{ex}}) \), where \( T_{\text{ex}} \) is the exobase temperature.

[10] Figure 5 displays the expected shapes and relative magnitude of each solar line. The flat shapes of the efficient solar lines assumed in our model are also displayed.

[11] As in previous studies [Strickland et al., 1972, 1973; Stewart et al., 1992], we do not consider the overlapping of the oxygen triplet by the CO fourth bands. The effect of this overlapping will be the subject of a forthcoming paper and is efficient essentially below 120 km [Barthelemy et al., 2008].

[12] A spherical, 3-D Monte Carlo, resonance line radiative transfer model has been used to compute the volume emission rate due to multiple scattering. This model is derived from an approach developed for the description of the heliospheric Lyman-\( \alpha \) line [Quémerais, 2000] and has been updated to describe the oxygen triplet emissions in a planetary environment (Appendix A). The volume emission rate \( S'(\mu, z) \) due to solar photon scattering is computed on a discrete grid in solar zenith angle (\( \mu \)) and altitude (\( z \)) in a spherical model, and the multiple scattering effects are taken into account.

[13] The volume production rates due to photoelectron impact \( S_{eo} \) may be written as

\[
S_{eo} = n(z)g_{pe}[N(\mu, z)],
\]

where \( n(z) \) is the atomic oxygen density, \( g_{pe} \) is the electron impact frequency, and \( N(\mu, z) \) is the slant column density of the atmosphere in the direction of the Sun. According to Stewart et al. [1992], the details of the equilibrium photoelectron fluxes are almost fully determined by the photoionization and electron collision cross sections of CO\(_2\) and are therefore insensitive to the abundance of O. Thus, \( N(\mu, z) \) is equal to the CO\(_2\) slant column density. The variation of \( g_{pe} \) with \( N \) is based on the work of Stewart [1970] in the terrestrial case. This primary volume production rate due to electron impact excitation of O is included in the radiative transfer model. The details of this computation are described in Appendix B.
The variation of the volume emission rates due to the solar photons and photoelectron impacts as a function of the altitude at SZA = 30° is displayed in Figure 6. In Figure 6 we display the primary emission rates and the emission rates due to multiple scattering. These profiles are calculated using a model of atmosphere defined by $T_{exo} = 200$ K and $n_{exo} = 1.5 \times 10^7$ cm$^{-3}$ for the solar conditions of the group 3 observations. For this model, the effect of the multiple scattering is important below 400 km. The order of magnitude of the primary emission rate due to photoelectrons is in good agreement with the emission rate profile (SZA $= 48°$) given by Shematovich et al. [2008]. Compared to these authors, it seems that we overestimate it by a factor of 3. Because we describe the photoelectron impact in a very simple way, a sensitivity analysis of the emission intensity profiles with respect to the $g_{po}(0)$ parameter is presented in section 4.2.

4. Data Analysis
4.1. Estimate of the Oxygen Density at the Exobase

To retrieve the oxygen density at the exobase, we use a least squares procedure that minimizes the $\chi^2$ function defined by

$$\chi^2 = \frac{1}{n-1} \sum_{i=1}^{n} \left( \frac{I_{obs,i} - I_{mod,i}(n_{80})}{\sigma_i^2} \right)^2$$

Figure 5. Theoretical shapes of the solar lines of the oxygen 130-nm triplet, a function of the wavelength $\lambda - \lambda_0$ in angstrom, where $\lambda_0$ is the center of each line. The sum of two Gaussians is taken from the work of Gladstone [1992]. The flat lines (thick solid lines at the center of each graph) are the approximate lines used in our model. The width of the line corresponds to 5 times the Doppler width for the exospheric temperature (here equal to 300 K). $F_1$, $F_2$, and $F_3$ are the integrated flux of each line.

Figure 6. Volume emission rate profiles of oxygen excitation of the 130.4-nm lines due to solar photons (squares) and photoelectron impacts (asterisks). The dashed lines correspond to the primary emission rates, and the solid lines correspond to the multiple scattering emission rates. These profiles have been obtained for a model with an oxygen density at 80 km equal to $1 \times 10^{11}$ cm$^{-3}$ and an exobase temperature equal to 200 K (see Figure 4) and for the solar conditions of group 3.
where \( n \) is the number of points in the observed intensity profile, \( I_{\text{obs,fit}} \) is the observed intensity for the \( i \)th line of sight of the fitted profile, \( I_{\text{mod,fit}}(n_{\text{mod}}) \) is the modeled intensity for the same line of sight assuming an oxygen density \( n_{\text{exo}} \) at 80 km, and \( \sigma_i \) is the standard deviation of the individual sample (see Figure 3). Table 2 displays the density at 80 km and at the exobase, which minimizes the \( \chi^2 \) function of each group of observations. The average density of all 80-km points is \( 6.2 \times 10^{10} \text{ cm}^{-3} \), which is in good agreement with the photochemical model of Krasnopolsky [2002] and previous observations. This average density corresponds to an exobase density of \( 9.3 \times 10^6 \text{ cm}^{-3} \).

[16] The 80-km and exobase oxygen densities are systematically lower at high SZA (groups 1b, 2b, 3b, and 4b) than at low SZA (groups 1a, 2a, 3a, 4a, and 5a). The average density at the exobase is \( 1.2 \times 10^6 \text{ cm}^{-3} \) at SZA \( \sim 30^\circ \) and 2 times smaller at high SZA \( (5.7 \times 10^6 \text{ cm}^{-3}) \).

[17] Figure 7 displays an example of the fit for group 3a. The theoretical contributions of the solar photons and photoelectrons are also shown. At 200 km, the contribution from photoelectron excitation \( (\sim 80 \text{ R}) \) is \( \sim 20\% \) of the total intensity \( (430 \text{ R}) \), which is in good agreement with the values between 16 and 25\% deduced by Stewart et al. [1992] from Mariner data.

[18] The best profile displayed in Figure 7 does not fit the data very well. However, considering the assumptions (analytical description of the photoelectron impact excitation, Maxwellian velocity distribution functions in the exosphere, spherical symmetry of the density, and no hot O population) and the badly constrained parameters (exospheric temperature, electron impact excitation frequency, and eddy mixing coefficient) used in the model, the result seems reasonable. The uncertainties on the model, indicated in Figure 7 (dotted lines), are defined in section 4.2. Moreover, this result is well supported by photochemical models [Krasnopolsky, 2002]. In section 4.2, in order to estimate the uncertainties due to the model on the values of the oxygen density at the exobase, we test the sensitivity of our results to different constrained parameters.

### 4.2. Uncertainty in the Oxygen Density at the Exobase

[19] As mentioned, the derived oxygen density values of section 4.1 are dependent on poorly constrained parameters, such as eddy mixing coefficient \( K(z) \), absolute calibration (or solar flux) described by a multiplicative factor \( A \), photoelectron impact frequency parameter \( g_{pe}(0) \), and exobase temperature \( T_{\text{exo}} \). Other parameters such as Gauss/Voigt line profiles used in the Monte Carlo radiative transfer model, nonspherical symmetry of the oxygen density (i.e., variations with latitude or longitude in the vertical O density profile), or departure of the exospheric oxygen density profile from the Chamberlain’s approximation will be studied in a future work. Using a Voigt line profile should increase partly the intensity of the models at low altitudes, but the uncertainty induced by a Gauss profile with respect to a Voigt profile is expected to be smaller than other parameters listed above.

[20] In sections 4.2.1–4.2.4 the uncertainty in the oxygen density derived from the uncertainty in a given parameter is studied by varying the value of each parameter while keeping the others fixed at the values determined for them in section 4.1. The nominal values of the parameters listed above are, respectively, \( K(z) = 1.2 \times 10^{12} \times \left[ T_{\text{exo}}/n(z) \right]^{1/2} \) [Krasnopolsky, 2002], \( A = 1 \), \( g_{pe}(0) = 1.7 \times 10^{-7} \text{ s}^{-1} \times \left[ F_{10.7}/54 \right] \), and \( T_{\text{exo}} = 200 \text{ K} \). We present here the results for the observations belonging to groups 3a and 3b (low and high SZA). However, the conclusions of this analysis have been found valid for the whole set of observations presented in Table 1.

#### 4.2.1. Sensitivity to the Eddy Diffusion Coefficient

[21] In order to test the sensitivity of the intensity to the eddy mixing coefficient, we use models with the same oxygen density at (and above) the exobase \( (1.5 \times 10^7 \text{ cm}^{-3} \) at the exobase) but with different mixing diffusion coefficients (therefore different oxygen thermospheric density). The density profiles displayed in Figure 8a have been obtained using eddy mixing diffusion coefficients \( K(z) = 0.1 \times K_0(z), 1 \times K_0(z), \) and \( 10 \times K_0(z) \), where \( K_0(z) \) is the nominal eddy mixing coefficient. As expected, when this coefficient

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**Table 2. Oxygen Density at 80 and 200 km Derived From Each Group**

<table>
<thead>
<tr>
<th>Group</th>
<th>( n_{80} \times 10^{10} ) (cm(^{-3}))</th>
<th>( n_{\text{exo}} \times 10^6 ) (cm(^{-3}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>1a</td>
<td>5.8</td>
<td>8.7</td>
</tr>
<tr>
<td>1b</td>
<td>2.7</td>
<td>4.0</td>
</tr>
<tr>
<td>2a</td>
<td>7.5</td>
<td>11.3</td>
</tr>
<tr>
<td>2b</td>
<td>5.8</td>
<td>8.7</td>
</tr>
<tr>
<td>3a</td>
<td>9.2</td>
<td>13.9</td>
</tr>
<tr>
<td>3b</td>
<td>3.6</td>
<td>5.4</td>
</tr>
<tr>
<td>4a</td>
<td>9.5</td>
<td>14.2</td>
</tr>
<tr>
<td>4b</td>
<td>3.1</td>
<td>4.6</td>
</tr>
<tr>
<td>5a</td>
<td>8.6</td>
<td>13.0</td>
</tr>
</tbody>
</table>

\(^a\)The exobase altitude is 200 km.
increases, the altitude of the homopause increases. When eddy diffusion dominates, then O and CO$_2$ have the same scale heights; when molecular diffusion dominates, each species has its own scale height (Figure 8a). Figure 8b shows the intensity profiles derived from these three models for group 3 at low SZA. The calculated intensity is not very sensitive to the eddy mixing coefficient; between the two extreme models, the intensity at 150 km only varies by <10%, while the oxygen density at 80 km varies 2 orders of magnitude.

In order to determine the altitude range probed by SPICAM-UVS when measuring the O 130.4-nm emission, the line of sight has been divided into 50 sections of equal length ($\lambda^2$/C2$^4$70 km). Figures 9a and 9b display the contribution of each of these sections (in percent of the total intensity) with respect to its altitude (which is taken as the altitude of the center of each section). Figure 9a displays the result for the solar source, and Figure 9b displays the result for the photoelectron source. The line of sight considered in Figure 9 corresponds to a line of sight of group 3 with a tangential point near 150 km. The three models have densities at 80 km equal to $1 \times 10^9$, $1 \times 10^{11}$ cm$^{-3}$, and $1 \times 10^{12}$ cm$^{-3}$, respectively. When the simulated density increases, the optical thickness increases. As a consequence, the expected region probed by SPICAM-UVS moves toward higher altitudes. For these models, the altitude range really seen by SPICAM-UVS varies from $\sim$170 to $\sim$340 km. Therefore SPICAM-UVS probes essentially the exosphere and in a minor way the thermosphere in the cases considered in this paper.

4.2.2. Sensitivity to the Absolute Calibration

Another source of uncertainty is related to the absolute calibration of SPICAM-UVS. Such uncertainty derives from the uncertainty in the efficiency area (that is, on the calibration based on already calibrated stars), estimated as being of the order of 15% [Bertaux et al., 2006], or on the method used to retrieve the total intensity [Leblanc et al., 2006]. Another source of uncertainty, which has the same effect as the calibration uncertainty, is related to the uncertainty in the solar flux given in the SORCE database and used to calculate the oxygen emission intensity in our model. To take into account such kind of uncertainties, we introduce a factor $A$ to the intensity derived from SPICAM-UVS. The variations of the derived oxygen density at 80 km with respect to the value of this factor $A$, chosen as varying between 0.7 and 1.3, are given in Table 3.

As expected for an optically thick emission, the derived densities at 80 km are very sensitive to the calibration and vary nonlinearly with the absolute intensity. For each observation the $\chi^2$ values are decreasing when the multiplicative factor is increasing. This may suggest that the nominal calibration underestimates rather than overestimates the real intensity. An uncertainty of 20% in the absolute intensity implies an uncertainty in the oxygen density retrieved at 80 km of $\sim$70%.

4.2.3. Sensitivity to the Photoelectron Impact Frequency

A third source of uncertainty in the oxygen density may be due to the description of the photoelectron impact $g_{pe}(0)$ in the model. An overestimation of $g_{pe}(0)$ by a factor of 4 is a reasonable upper uncertainty because it corresponds to the ratio between the cross sections used by Stewart et al. [1992] and those by Strickland et al. [1973]; this overestimation also encompasses the uncertainties of the O 130-nm electron impact excitation cross section given by Barklem [2007]. In another way, we considered an underestimation by a factor of 4. The variation of the inferred density at 80 km with respect to different values of the photoelectron impact excitation frequency $g_{pe}(0)$ is given in Table 4.
The inferred density at 80 km decreases when the photoelectron frequency increases, because of the increase of the total intensity due to the excitation by the photoelectron. The lower uncertainty in the oxygen density is equal to 155% at low SZA and 100% at high SZA, and the upper uncertainty is equal to \(10^{-8}/C_2\) at low SZA and \(40\%\) at high SZA. A description of the photoelectron impact with a more accurate model describing the photoelectron transport as used by Stewart et al. [1992] is therefore highly needed to reduce the uncertainty due to this parameter.

4.2.4. Sensitivity to the Exobase Temperature

The modeled temperature is fully defined by the temperature at the exobase [Krasnopolsky, 2002]. In particular, the exosphere is assumed to be isothermal. The temperature is an important parameter because it defines the scale height of the oxygen in the thermosphere as well as in the exosphere. Moreover, it increases the width of the Doppler line in the radiative transfer model. We choose exospheric temperatures varying between 175 and 400 K in agreement with the exospheric temperatures estimated from the MTGCM model [Bougher et al., 1999]. Figure 10 displays the best fits for each exospheric temperature. Above 250 km the calculated intensity increases with increasing exobase temperature. Inversely, the oxygen density at the exobase derived from the study will decrease with increasing exobase temperature as shown in Table 5.

### Table 3. Variations of the Oxygen Density at the Exobase, 200 km, Derived From Each Group of Observations When an Uncertainty in the Absolute Calibration is Introduced

<table>
<thead>
<tr>
<th>(A)</th>
<th>(n_{exo} \times 10^6) (cm(^{-3}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low SZA</td>
<td></td>
</tr>
<tr>
<td>0.7</td>
<td>5.5</td>
</tr>
<tr>
<td>0.8</td>
<td>8.0</td>
</tr>
<tr>
<td>0.9</td>
<td>10.5</td>
</tr>
<tr>
<td>1.0</td>
<td>13.9</td>
</tr>
<tr>
<td>1.1</td>
<td>18.1</td>
</tr>
<tr>
<td>1.2</td>
<td>22.4</td>
</tr>
<tr>
<td>1.3</td>
<td>28.0</td>
</tr>
<tr>
<td>High SZA</td>
<td></td>
</tr>
<tr>
<td>0.7</td>
<td>2.1</td>
</tr>
<tr>
<td>0.8</td>
<td>3.0</td>
</tr>
<tr>
<td>0.9</td>
<td>4.0</td>
</tr>
<tr>
<td>1.0</td>
<td>5.4</td>
</tr>
<tr>
<td>1.1</td>
<td>7.1</td>
</tr>
<tr>
<td>1.2</td>
<td>9.0</td>
</tr>
<tr>
<td>1.3</td>
<td>11.0</td>
</tr>
</tbody>
</table>

*The \(A\) coefficient represents a multiplicative factor of the intensity observed by SPICAM/MEX.

### Table 4. Variations of the Oxygen Density at the Exobase, 200 km, Derived From Group 3 Observations With the Photoelectron Frequency \(g_{pe}(0)\)

<table>
<thead>
<tr>
<th>(g_{pe}(0)/g_{pe}) (Standard)</th>
<th>(n_{exo} \times 10^6) (cm(^{-3}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low SZA</td>
<td></td>
</tr>
<tr>
<td>1/4</td>
<td>23.5</td>
</tr>
<tr>
<td>1/2</td>
<td>19.0</td>
</tr>
<tr>
<td>1</td>
<td>13.9</td>
</tr>
<tr>
<td>2</td>
<td>9.3</td>
</tr>
<tr>
<td>4</td>
<td>5.8</td>
</tr>
<tr>
<td>High SZA</td>
<td></td>
</tr>
<tr>
<td>1/4</td>
<td>7.8</td>
</tr>
<tr>
<td>1/2</td>
<td>6.8</td>
</tr>
<tr>
<td>1</td>
<td>5.4</td>
</tr>
<tr>
<td>2</td>
<td>3.9</td>
</tr>
<tr>
<td>4</td>
<td>2.5</td>
</tr>
</tbody>
</table>

Figure 9. Contribution of different sections of the line of sight to the total integrated intensity with respect to the altitude of the section (taken as the altitude of the center of each section). The different lines correspond to the different models with densities at 80 km equal to \(1 \times 10^9\) cm\(^{-3}\) (diamonds), \(1 \times 10^{11}\) cm\(^{-3}\) (solid lines), and \(1 \times 10^{12}\) cm\(^{-3}\) (asterisks). (a) The results for the solar source, and (b) The results for the photoelectron impact source. The two vertical lines represent the altitude of Mars Express (MEX) and the altitude of the tangent point of the line of sight (Mars nearest point, or MNP; here near 150 km).
bands and the Np variations of the density at 80 and 200 km derived from Leblanc's Vegard-Kaplan bands below 200 km are also equal (K) cm

Nagy and Cravens are also given by the convolution of the solar lines profile and the Gaussian absorption profile:

\[ g_{exc} = \sum_{j=1}^{\infty} g_{0,j} \int_{-\infty}^{+\infty} \left( \pi F_{\lambda,j} \right) \exp \left[ -\left( \lambda - \lambda_0,j \right)^2 / \Delta \lambda_{D,j}^2 \right] d\lambda, \]

(4)

where \( \sigma_{0,j} \) is the absorption cross section at the center of the \( j \)th line, \( \pi F_{\lambda,j} \) is the spectral solar flux of the line \( j \), \( \lambda_0,j \) is the wavelength at the center of the line \( j \), and \( \Delta \lambda_{D,j} \) is the Doppler width of the line \( j \). Because here we assume a uniform temperature for the hot population, \( p_0, \sigma_{0,j} \), and \( \Delta \lambda_{D,j} \) are also uniform. Using the analytical profile lines given by Gladstone [1992] and displayed in Figure 5, the calculation of equation (4) is straightforward, and we find an excitation factor \( g_{exc} \) equal to \( 1.35 \times 10^{-5} \) s\(^{-1}\).

[31] We take into account the auto-absorption when we calculate the integrated intensity along the line of sight. The integrated intensity obtained for group 3a is equal to \( \sim 11 \) R between 200 and 400 km. When we use a hot oxygen temperature of 10,000 K, the integrated intensity is equal to \( \sim 12 \) R. Therefore a hot population can partly explain the differences between the best model obtained in section 4.1.

Table 5. Variations of the Density at 80 and 200 km Derived From Group 3 Observations When the Exobase Temperature is Varied\(^a\)

<table>
<thead>
<tr>
<th>( T_{exo} ) (K)</th>
<th>( n_{ox} \times 10^{18} ) (cm(^{-3}))</th>
<th>( n_{ex} \times 10^{18} ) (cm(^{-3}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group 3a</td>
<td></td>
<td></td>
</tr>
<tr>
<td>175</td>
<td>13.4</td>
<td>16.5</td>
</tr>
<tr>
<td>200</td>
<td>9.2</td>
<td>13.9</td>
</tr>
<tr>
<td>225</td>
<td>6.5</td>
<td>11.0</td>
</tr>
<tr>
<td>250</td>
<td>4.8</td>
<td>8.9</td>
</tr>
<tr>
<td>275</td>
<td>3.7</td>
<td>7.3</td>
</tr>
<tr>
<td>300</td>
<td>3.0</td>
<td>6.0</td>
</tr>
<tr>
<td>325</td>
<td>2.4</td>
<td>4.9</td>
</tr>
<tr>
<td>350</td>
<td>2.0</td>
<td>4.2</td>
</tr>
<tr>
<td>375</td>
<td>1.7</td>
<td>3.6</td>
</tr>
<tr>
<td>400</td>
<td>1.5</td>
<td>3.1</td>
</tr>
<tr>
<td>Group 3b</td>
<td></td>
<td></td>
</tr>
<tr>
<td>175</td>
<td>5.3</td>
<td>6.6</td>
</tr>
<tr>
<td>200</td>
<td>3.6</td>
<td>5.4</td>
</tr>
<tr>
<td>225</td>
<td>2.5</td>
<td>4.3</td>
</tr>
<tr>
<td>250</td>
<td>2.0</td>
<td>3.6</td>
</tr>
<tr>
<td>275</td>
<td>1.5</td>
<td>2.9</td>
</tr>
<tr>
<td>300</td>
<td>1.2</td>
<td>2.3</td>
</tr>
<tr>
<td>325</td>
<td>1.0</td>
<td>2.0</td>
</tr>
<tr>
<td>350</td>
<td>0.8</td>
<td>1.7</td>
</tr>
<tr>
<td>375</td>
<td>0.7</td>
<td>1.5</td>
</tr>
<tr>
<td>400</td>
<td>0.6</td>
<td>1.3</td>
</tr>
</tbody>
</table>

\(^a\)For all groups of observations, the assumption of a high exospheric temperature (300 K) provides the best fit.

4.3. Effect of a Hot Population

[29] To estimate the effect of a hot population on the observed brightness, we have computed a first-order calculation. The density profile used to describe the hot population is the one computed by Chaufray et al. [2007] for minimum solar conditions, extrapolated exponentially below 550 km until 200 km. The densities of the cold and hot oxygen populations are displayed in Figure 11. The temperature of the hot population is assumed to be uniform and equal to 6000 K, which corresponds to an average energy of \( \sim 0.6 \) eV by atoms and is near the values found by Krestyanikova and Shematovich [2005] and Cipriani et al. [2007].

[30] The volume emission rates are computed assuming that the atmosphere is optically thin. In this case, the volume emission rate at the line \( i \) is proportional to the density. The volume emission rate is then equal to the density multiplied by the product of the percentage of oxygen in the ground state susceptible to absorbing the photons emitted in the line \( i \) and \( p_i \) (see Appendix A for more details) and the excitation parameter \( g_{exc} \) given by the convolution of the solar lines profile and the Gaussian absorption profile:

\[ g_{exc} = \sum_{j=1}^{\infty} p_j \sigma_{0,j} \int_{-\infty}^{+\infty} \left( \pi F_{\lambda,j} \right) \exp \left[ -\left( \lambda - \lambda_0,j \right)^2 / \Delta \lambda_{D,j}^2 \right] d\lambda, \]

where \( \sigma_{0,j} \) is the absorption cross section at the center of the \( j \)th line, \( \pi F_{\lambda,j} \) is the spectral solar flux of the line \( j \), \( \lambda_0,j \) is the wavelength at the center of the line \( j \), and \( \Delta \lambda_{D,j} \) is the Doppler width of the line \( j \). Because here we assume a uniform temperature for the hot population, \( p_0, \sigma_{0,j} \), and \( \Delta \lambda_{D,j} \) are also uniform. Using the analytical profile lines given by Gladstone [1992] and displayed in Figure 5, the calculation of equation (4) is straightforward, and we find an excitation factor \( g_{exc} \) equal to \( 1.35 \times 10^{-5} \) s\(^{-1}\).
A hot oxygen density that is denser (by a factor of \( \sim 5 \)) than that modeled by Chaufray et al. [2007] could improve the fit.

5. Discussion

5.1. Exospheric Density

[32] From the sensitivity study of section 4.2, the total uncertainty in the oxygen density as derived from the observations is equal to a factor of 2 or 3 on the nominal values given in section 4.1. Therefore the oxygen exobase density derived from our analysis is between 0.7 and 2.4 \( \times 10^7 \) cm\(^{-3} \) at low SZA and between 0.3 and 1.0 \( \times 10^7 \) cm\(^{-3} \) at high SZA. Actually, the different parameters considered in section 4.2 do not act independently, and therefore this uncertainty is probably overestimated. The ratio between the densities at low SZA and those at high SZA should be less dependent on these parameters. As an example, an uncertainty in the calibration implies the same correction to the data at low and high SZA and, as a consequence, a significantly smaller uncertainty in the divided exobase densities (Table 3).

[33] Recently, Mazarico et al. [2007] have estimated the total density of the Martian atmosphere at 400 km altitude by using radio-tracking data and precise orbit determination on the Mars Odyssey spacecraft between March 2002 and November 2005. These authors found a density between \( 10^{-15} \) and \( 10^{-14} \) kg m\(^{-3} \) and a scale height between 25 and 45 km. The main species contributing to the mass density at 400 km are O, H, H\(_2\), and He. (The extrapolations of the CO and N\(_2\) densities from Krasnopolsky [2002] show that they are minor contributors, even in terms of mass density.)

[34] The mass density \( \rho \) of the exosphere is

\[
\rho = \sum_i \rho_i, \tag{5}
\]

where \( \rho_i = n_i m_i \) is the mass density of species \( i \). The atmospheric scale height can be linked to the scale height of the different species. If we assume a simple exponential law to describe the local density profile near 400 km as used by Mazarico et al. [2007], we find

\[
\frac{1}{H_r} = \frac{1}{\rho} \left( \sum_i \frac{\rho_i}{H_i} \right), \tag{6}
\]

where \( H_r \) is the scale height of the total mass density and \( H_i \) is the scale height of species \( i \).

[35] The hydrogen density is estimated from SPICAM above the south pole [Chaufray et al., 2008], which corresponds to the observations analyzed by Mazarico et al. [2007]. The H\(_2\) and He densities are estimated by extrapolating the exobase densities given by Krasnopolsky [2002] with a simple Chamberlain approach, for an exospheric temperature equal to 200 K. This author found an exobase hydrogen density in reasonable agreement with SPICAM. We consider the oxygen density estimated in this paper at 400 km for SZA between 55\(^\circ\) and 90\(^\circ\).

[36] The densities at 400 km are therefore \( 1 \pm 1 \times 10^5 \), \( 1 \pm 1 \times 10^5 \), \( 3 \pm 3 \times 10^4 \), \( 5 \pm 3 \times 10^4 \) cm\(^{-3} \) for H, H\(_2\), He, and O, respectively. Using these values, we find a mass density \( \rho \) between 0.5 and 3.5 \( \times 10^{-15} \) kg m\(^{-3} \) in good agreement with the estimate of Mazarico et al. [2007]. Neglecting any hot populations and assuming a single temperature for all species, the mass density scale height \( H_r \) of 35 km corresponds to an exospheric temperature between 140 and 240 K, in good agreement with Leblanc et al. [2007].

[37] The presence of a hot oxygen population should not change this temperature derived from a scale height. Indeed, as shown in equation (6), the term \( \rho_{\text{hot}}/H_{\text{hot}} \) should be small with respect to the other terms. Figure 7 shows that for the best model considered here, the intensity is lower than the observed intensity at high altitudes. This effect has also been observed on Earth by the Berkeley EUV airglow rocket spectrometer (BEARS) [Cotton et al., 1993]. Cotton et al.

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Figure 11. Density profiles of CO\(_2\), O (cold), and O (hot) used to estimate the contribution of the hot oxygen component to the intensity.
[1993] suggest that this discrepancy may be due to an emission induced by photons escaping the lower thermosphere and scattered in the large wings of the velocity distribution of a hot oxygen corona component. However, the investigation of the effect of the hot population on these EUV data has been shown to be insufficient [Hubert et al., 1999]. A full radiative transfer calculation including both cold and hot oxygen components and non-Maxwellian velocity distributions would be useful to investigate further the effect of the hot population.

5.2. [O]/[CO₂] Mixing Ratio

As shown in section 4.2, the emission intensity measured above 150 km by SPICAM-UVS is essentially constrained by the oxygen exospheric density profiles. The thermospheric oxygen density profile is therefore badly constrained by SPICAM-UVS observations. Despite this limitation, it is interesting to derive the value of the [O]/[CO₂] mixing ratio using the oxygen profiles given in section 4.1. The average value of the mixing ratio [O]/[CO₂] at 135 km is equal to 0.9%. This value is slightly lower than the value (~1.25%) deduced from Viking ion profiles at SZA ~ 60° during low solar activity [Hanson et al., 1977]. Hanson et al. [1977] used a simple photochemical approach in order to reproduce the observed ion profiles. In another way, this value is slightly higher than the mixing ratio deduced by Stewart et al. [1992] from Mariner’s missions (between 0.4 and 0.7%) during high solar activity. At low SZA the average value of the mixing ratio is found to be around 1.2%, and at high SZA this value is equal to 0.6% These values are in good agreement with the MTGCM model [Bougher et al., 1999] and cannot explain the low thermospheric temperature deduced by Keating et al. [1998] from the accelerometer’s measurement of MGS. Keating et al. [1998] attributed this low thermospheric temperature to a possible higher [O]/[CO₂] mixing ratio than that predicted or to the presence of gravity waves. Because the temperatures deduced by SPICAM are lower than those predicted by the MTGCM model [Leblanc et al., 2006, 2007], an uncertainty in the collision coefficient between CO₂ and O and therefore on the cooling rate or in the solar EUV/UV heating efficiency could be another explanation of the observed discrepancy.

6. Conclusion

We present here the first detailed analysis of the oxygen 130.4-nm line observed by SPICAM-UVS aboard Mars Express. The present coverage of measurements in terms of solar zenith angle, aero-centric longitude, and local time is limited because limb-viewing observations of the dayglow imply a particular orientation of the spacecraft. The measurements presented in this paper are the first of the oxygen in the upper atmosphere since Mariner’s missions 30 years ago. Comparison between oxygen data and density models coupled to a radiative transfer approach leads to derivation of an oxygen density at the exobase equal to 1.2±0.5×10⁻⁴ cm⁻³ at SZA < 60° and equal to 0.6±0.3×10⁻² cm⁻³ at SZA > 60°. Because Mars Express is above the exobase, the observed oxygen emission is more sensitive to the exospheric oxygen than to the thermospheric oxygen. A simple diffusion model allows one to extrapolate the density below the exobase, leading to a [O]/[CO₂] mixing ratio between 0.6 and 1.2%, in good agreement with previous measurements [Hanson et al., 1977; Stewart et al., 1992]. Exospheric temperatures higher than 200 K provide the best fit to the data and could be due to the presence of a hot population produced by dissociative recombination of O₂ [Krestyanikova and Shematovich, 2005]. In order to confirm this conclusion, a model of radiative transfer needs to be developed that takes into account a hot oxygen population and describes non-Maxwellian velocity distribution. Reducing the model’s uncertainties by using a more realistic description of the photoelectron impact frequency is also needed to better constrain the oxygen density at the exobase. Such a model could also be useful to study the O 1356 A line. This line, identified on SPICAM-UVS spectra below 200 km in altitude [Leblanc et al., 2006], is an optically forbidden transition, and its intensity is weaker than the intensity of the 130.4-nm triplet. Finally, the CO fourth positive bands overlapping partly the O 130.4-nm emission could also contribute to the observed emission, in particular by redistributing part of the 130.4-nm emission intensity toward longer wavelengths [Barthelemy et al., 2008].

Appendix A: A Radiative Transfer Code for the Solar Source

Because the O 130.4-nm triplet is optically thick, we use a spherical radiative transfer model that takes into account multiple scattering in calculating the volume emission rates. The optical thickness at the center of the first line (130.217 nm) for the SPICAM/MEX observations (for the nominal model) is ~720 at 150 km, 130 at 200 km, and 5 at 300 km. Our radiative transfer model is derived from the Monte Carlo model developed by Quéméréais [2000] to describe the Lyman-α brightness of the interplanetary medium. This Monte Carlo model takes into account temperature variations with altitude and partial frequency redistribution. For each oxygen density profile, twenty million solar photons are followed into the atmosphere until they escape or they are absorbed by CO₂.

Each test photon comes from a disk orthogonal to the Sun-Mars axis and whose radius is equal to 4400 km (Marsian radius plus altitude upper limit). The position on this disk is determined randomly.

In our model, the relation between the flux at the center of each line and the integrated flux of each line is deduced from the profiles of Gladstone [1992] and given by

\[
\frac{F_i(0)}{F_i} = \frac{1}{\sqrt{\pi x_{0i}}} \left\{ \exp \left[ -\left( \frac{x_{1i}}{x_{0i}} \right)^2 \right] \right\},
\]

where \(F_i(0)\) is the solar flux at the center of the line \(i\), \(F_i\) is the integrated solar flux of the line \(i\), and \(x_{0i}\) and \(x_{1i}\) are the parameters of each line estimated by Gladstone [1992]. The ratios between the integrated solar flux of the \(i\)th line and the total flux of the three lines \(f_i = F_i(F_1 + F_2 + F_3)\) used in this study are also those estimated by Gladstone [1992].

Because the temperature of the Martian atmosphere is very low compared to the temperature of formation of the solar lines, the solar line can be assumed to be flat in the spectral region studied here [−2.5Δν_D(T_exo), 2.5Δν_D(T_exo)], where Δν_D(T_exo) is the Doppler width of the line \(i\) (which is assumed independent of the line hereafter). Figure 5 displays
the profile of each line normalized by $F_1 + F_2 + F_3$ and the flat profiles used in this study for an exospheric temperature equal to 300 K. To determine the solar line of emission of each simulated solar photon, we use

$$0 < r < \frac{G_1}{G} \text{: line1}$$
$$\frac{G_1}{G} < r < \frac{G_1 + G_2}{G} \text{: line2}$$
$$\frac{G_1 + G_2}{G} < r < 1 \text{: line3}$$  \hspace{1em} (A2)

In equation (A2), $r$ is a random number between 0 and 1; $G_1$, $G_2$, and $G_3$ are the integrated fluxes over the flat shape used in this study ($G_i = 5 \times F_i(0) \times \Delta v_i$) (thick solid lines of Figure 5); and $G = G_1 + G_2 + G_3$. The ratios $G_i/G$ are independent of the integrated solar flux; therefore each model can be scaled to any of the observations. The normalized frequency of the solar photon is given by

$$x = 5r - 2.5.$$  \hspace{1em} (A3)

This implies that the frequency is given by

$$\nu = \nu_{0,i} + \Delta\nu_{D,ref}(5r - 2.5),$$  \hspace{1em} (A4)

where $\nu_{0,i}$ is the frequency at the center of the line $i$ and $\Delta\nu_{D,ref}$ is the Doppler width of the line for a reference temperature $T_{ref}$ (here the exospheric temperature).

[44] The direction of propagation of the solar photon is the Sun-Mars direction. We then determine the optical thickness that the solar photon needs to cross before its first scattering:

$$\tau_s = -\log(r).$$  \hspace{1em} (A5)

To determine the position of the scattering, we compute, step by step, the optical thickness at the frequency of the photon $\tau$ crossed by the photon:

$$\tau + d\tau = \tau + \sigma_{i,ref} \sqrt{\frac{T_{ref}}{T(r)}} \times e^{-\frac{x}{kT(r)}} \times p_i(r) \times ds(r),$$  \hspace{1em} (A6)

where $ds(r)$ is the step size (varying from 0.5 km at low altitudes to 10 km at high altitudes), the term in the exponential is the local normalized frequency, which depends on temperature through the Doppler width, $T_i$ is the temperature at the position where the photon has been emitted ($T_i = T_{ref}$ before the first scattering), $T(r)$ and $n(r)$ are the local temperature and oxygen density, respectively, $\sigma_{i,ref}$ is the cross section at the center of the line $i$ for the reference temperature $T_{ref}$ and the root square factor describes the variations of this cross section with the temperature.

[45] Value $p_i(r)$ is the percentage of oxygen in the ground state susceptible to absorbing the photons emitted in the line $i$. This percentage depends on the temperature as follows:

$$p_i(r) = \frac{g_i e^{-\frac{\Delta E_i}{kT_i}}}{\sum_k g_k e^{-\frac{\Delta E_k}{kT_k}}},$$  \hspace{1em} (A7)

where

$$\Delta E_i = \frac{hc}{\lambda_{0,i}} - \frac{hc}{\lambda_{i,i}},$$  \hspace{1em} (A8)

$h$ is the Planck’s constant, $c$ is the light velocity, $\lambda_{0,i}$ is the wavelength of the $i$th line of the triplet (130.217, 130.486, and 130.603 nm), $k$ is the Boltzmann’s constant, and $g_i$ are the relative populations for an infinite temperature [Strickland and Donahue, 1970].

[46] We also estimate the optical thickness due to the absorption of CO$_2$ by

$$\tau_{abs} + d\tau_{abs} = \tau_{abs} + \sigma_{abs,i} \times n_{CO_2}(r) \times ds(r),$$  \hspace{1em} (A9)

where $n_{CO_2}(r)$ is the CO$_2$ density and $\sigma_{abs,i}$ is the absorption cross section at the wavelength $\lambda_i$. The weight $W$ of the photons initially equal to 1 is reduced by a factor $\exp(-\tau_{abs})$ at each step.

[47] We neglect the variation of the CO$_2$ absorption cross section with temperatures. It only depends on the line. We follow the photon until $\tau = \tau_s$. If the photon crosses the limits of the described region before reaching this equality, we simulate a new solar photon; otherwise, we compute the scattering. When we have a scattering in $(r, \alpha)$, we assume that a photon is emitted at the same position. We assume an isotropic scattering, so the new direction of the photon is given by

$$\phi = 2\pi r_{\phi},$$
$$\theta = \arccos(1 - 2r_{\theta}),$$  \hspace{1em} (A10)

where $r_{\phi}$ and $r_{\theta}$ are random numbers between 0 and 1, and $\phi$ and $\theta$ are the two angles that define the new direction. The definition of these angles is given in Figure A1. Note that $\theta$ is the scattering angle. The line of the emitted photon is determined thanks to the relative population of the ground state (equation (A7)), and the accurate frequency in the line is estimated from the algorithm of Lee [1977] assuming a partial frequency redistribution. The basic method for the algorithm is the following.

[48] The only atoms that can absorb the photons are those that “see” the photons with the frequency $\nu_{0,i}$, that is, those whose velocity component $V_1$ along the direction of the incident photons follows

$$\nu_{0,i} = \left(1 - \frac{V_1}{c}\right) \times \nu.$$  \hspace{1em} (A11)

Equation (A11) can be rewritten by replacing $\nu$ with the normalized frequency:

$$x\left(\Delta\nu_{D,i}(T_i) - \frac{V_1}{c} \Delta\nu_{D,i}(T_i)\right) = \nu_{0,i} \times \frac{V_1}{c}.$$  \hspace{1em} (A12)

The second term on the left is negligible. We normalize the component of the atom velocity by

$$V_1 = V_{th}(r) \times u_1,$$  \hspace{1em} (A13)
where \( V_{th} \) is the local thermal velocity. We can write

\[
\frac{V_{th}}{\Delta \nu_D(T_i)} = \frac{c}{\sqrt{2 \pi \nu_0 \nu}} \sqrt{\frac{T_i}{T_f}} \quad \text{(A14)}
\]

where \( T(r) \) is the local temperature and \( T_i \) is the temperature at the position at which the photon incident has been emitted (exospheric temperature before the first scattering).

[51] Equation (A17) can be rewritten by replacing \( \nu \) with the normalized frequency to provide

\[
x' \left( \Delta \nu_{D,i}(T(r)) - \frac{u' \times V_{th}}{c} \right) = \frac{V_{th}}{c} u',
\]

which is the same equation as equation (A12), but this time the temperature defining the Doppler width is \( T(r) \). Neglecting the second term on the left, equation (A18) is reduced to

\[
x' = u' = u_1 \cos(\theta) + u_2 \sin(\theta).
\]

We note \( u_2 \) is the atom-normalized velocity component orthogonal to the direction of propagation. This velocity is determined randomly by assuming a Gaussian velocity function distribution (even in the exosphere, which is probably not the case). We compute the velocity with the Box and Muller algorithm [Box and Muller, 1958]. If we consider that the new photon is emitted in the line \( k \), the frequency of the photon in the referential frame of the atom will be \( \nu_{0,k} \).

[50] If \( u' \) is the component of the atom-normalized velocity in the direction of propagation of the emitted photon, we have

\[
u_0 = \frac{u'}{c} \times \nu.
\]

The frequency \( \nu' \) of the emitted photon in the referential frame (referential of the atmosphere) will follow the relation (A17):

\[
u_{0,k} = \left(1 - \frac{u' \times V_{th}}{c}\right) \times \nu', \quad \text{(A17)}
\]

[52] Thereafter, we can estimate the contribution of the emitted photon to the simulated primary (for the first scattering) or multiple emission volume rate at the points of the spatial and frequency grids. The new photon is followed, and the same cycle is repeated. After each scattering, we update the volume emission of multiple scattering simulated. The process is stopped when the photon crosses the boundaries of the model, or when its weight becomes lower than \( 1 \times 10^{-9} \).

The link between the real volume emission rate and the volume emission rate simulated is given by

\[
S_{\text{real}}(r,x) = S_{\text{inc}} \times G \frac{V_{\text{cell}}(r) \cdot \Delta x \cdot N_{\text{photon}} \Delta \lambda_D}{\Delta \nu_D(r)} \sum_{\text{photon}} W_{\text{sim}}(r,x),
\]

where \( S_{\text{inc}} \) is the surface area of the disk where solar photons are issued, \( V_{\text{cell}} \) is the efficiency volume around the considered spatial point [Quémerais, 2000], \( \Delta x \) is the frequency grid step, \( N_{\text{photon}} \) is the total number of photons simulated, \( \sum W_{\text{sim}}(r,x) \) is the emission volume rate simulated at the...
spatial grid point \( \mathbf{r} \) and the frequency \( x \) of the line \( i \), and \( G \) is the total solar flux in the three efficient lines.

[53] Once the emission volume rates have been calculated, we compute the intensity integrated on the line of sight for each observation for each model using the formal solution of the radiative transfer given by equation (A21). The only changes for one observation to another are the geometry of the line of sight (the direction \( \mathbf{\Omega} \) of the line of sight and the position of the spacecraft \( \mathbf{r} \)) and the value of the solar flux at 130.4 nm:

\[
I(\mathbf{r}, \mathbf{\Omega}) = \frac{1}{4\pi} \sum_{i=1}^{3} \int_{0}^{\infty} \int_{0}^{\infty} S_{i}^{\text{real}}(\mathbf{r} + s\mathbf{\Omega}, \lambda) e^{-\tau_{\lambda,i}(\mathbf{r} + s\mathbf{\Omega})} e^{-100\lambda(\mathbf{r} + s\mathbf{\Omega})} ds d\lambda. \tag{A21}
\]

Appendix B: Photoelectron Source

[54] The variation of impact frequency of the photoelectrons \( g_{pe} \) with the column density \( N \) is based on the work of Stewart [1970] in the terrestrial case and is given by

\[
g_{pe}(N; \text{cm}^{-2}) = \frac{1}{B_{0} + B_{1}(N/10^{17}) + B_{2}(N/10^{17})^{2}}. \tag{B1}
\]

\( B_{1} \) and \( B_{2} \) have been chosen to reproduce the variations given in Figure 4 of Strickland et al. [1973]. \( B_{0} \) is equal to \( 1/g(0) \). We assume a linear relation between \( g(0) \) and the solar flux \( F_{0.7} \) at Mars. The normalization factor \( g(0) \) is the value estimated by Stewart et al. [1992]: \( 1.7 \times 10^{-7} \text{s}^{-1} \) for \( F_{0.7} = 54 \).

[55] The scheme of the model for describing the multiple scattering due to photoelectron impacts is the same as that used to describe the solar source. Twenty million photons emitted by electronic impact are followed. The only difference comes from the computation of the photons before the first scattering. The position of the photons emitted (before the first scattering) is given by solving the following equation:

\[
\int_{0}^{\varphi} \int_{0}^{\mu} \int_{0}^{r} \left( \frac{S^{\text{pe}}(\mu, r)}{W} r^{2} d\mathbf{r} \right) d\mu d\varphi = \alpha \int_{0}^{1} \int_{0}^{r_{\text{max}}} \left( \frac{S^{\text{pe}}(\mu, r)}{W} r^{2} d\mathbf{r} \right) d\mu d\varphi, \tag{B2}
\]

where \( S^{\text{pe}} \) is the production volume rate, defined in equation (1), \( W \) is the weight of the photon, which means the number of real photons represented by one test particle, \( r \) is the distance from the center of Mars (assumed spherical), \( \mu = \cos(SZA) \), \( \varphi \) is the second spherical coordinate, and \( \alpha \) is a random number between \([0, 1] \). To simplify this calculation, we assume \( W = S_{i}^{\text{pe}} \times V_{\text{tot}} \), where \( V_{\text{tot}} \) is the volume between \( r_{\text{min}} \) and \( r_{\text{max}} \). Under this assumption, the position of the first photon \( (r, \mu, \varphi) \) is given by

\[
r = \sqrt{r_{\text{min}}^{2} + \alpha_{1}(r_{\text{max}}^{2} - r_{\text{min}}^{2})},
\mu = 1 - \alpha_{2},
\varphi = \alpha_{3} \times 2\pi. \tag{B3}
\]

The direction of the photon emitted is assumed to be isotropic; the line of the emitted photon is determined thanks to the relative population of the ground state at the local temperature (equation (A7)) and the frequency using the Box and Muller algorithm [Box and Muller, 1958]. The optical thickness before scattering is determined by using equation (A5).

[56] If the weight of the photon is higher than \( 10^{-9} V_{\text{tot}} \), the primary emission volume rate is updated, meaning that photons produced at a position where \( S^{\text{pe}} < 10^{-9} \text{cm}^{-3} \text{s}^{-1} \) are not taken into account. Each photon is followed until it crosses the upper limit or the lower limit or until its weight becomes lower than \( 1 \times 10^{-9} \times V_{\text{tot}} \); the scheme used for multiple scattering is the same as that for the solar source.

[57] Then the spectral production volume rates are normalized by

\[
S_{\text{real}}(\mathbf{r}, \lambda) = \frac{P_{\text{real}}}{P_{\text{sim}}} \sum_{i=1}^{3} \frac{W_{\text{photons},i}(\mathbf{r}, x)}{V_{\text{cell}}(\mathbf{r}) \times \Delta X \times \Delta Z / (\Delta r)}, \tag{B4}
\]

where \( P_{\text{real}} \) is the real total production in \( \text{s}^{-1} \) for the atmospheric model (given by the right term of equation (B2) with \( \alpha = 1 \) and \( W = 1 \)) and \( P_{\text{sim}} \) is the total production simulated, which means the sum of the weight of all the photons emitted. The sum symbol corresponds to the sum of the weight of the photons emitted at the position \( \mathbf{r} \) with a normalized frequency \( x \) in the line \( i \).

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