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Interaction of aerosol particles composed of protein and salts with water vapor: hygroscopic growth and microstructural rearrangement

E. Mikhailov\(^1,2\), S. Vlasenko\(^2\), R. Niessner\(^1\), and U. Pöschl\(^1\)

\(^1\)Technical University of Munich, Institute of Hydrochemistry, Marchioninistr. 17, D-81377 Munich, Germany
\(^2\)Atmospheric Physics Department, Institute of Physics, St. Petersburg State University, Ulianovskaya 1, 198904 St. Petersburg, Russia

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Abstract. The interaction of aerosol particles composed of the protein bovine serum albumin (BSA) and the inorganic salts sodium chloride and ammonium nitrate with water vapor has been investigated by hygroscopicity tandem differential mobility analyzer (H-TDMA) experiments complemented by transmission electron microscopy (TEM) and Köhler theory calculations (100–300 nm particle size range, 298 K, 960 hPa). BSA was chosen as a well-defined model substance for proteins and other macromolecular compounds, which constitute a large fraction of the water-soluble organic component of air particulate matter.

Pure BSA particles exhibited deliquescence and efflorescence transitions at \(\sim 35\%\) relative humidity (RH) and a hygroscopic diameter increase by up to \(\sim 10\%\) at 95\% RH in good agreement with model calculations based on a simple parameterisation of the osmotic coefficient. Pure NaCl particles were converted from near-cubic to near-spherical shape upon interaction with water vapor at relative humidities below the deliquescence threshold (partial surface dissolution and recrystallisation), and the diameters of pure NH\(_4\)NO\(_3\) particles decreased by up to 10\% due to chemical decomposition and evaporation.

Mixed NaCl-BSA and NH\(_4\)NO\(_3\)-BSA particles interacting with water vapor exhibited mobility equivalent diameter reductions of up to 20\%, depending on particle generation, conditioning, size, and chemical composition (BSA dry mass fraction 10–90\%). These observations can be explained by formation of porous agglomerates (envelope void fractions up to 50\%) due to ion-protein interactions and electric charge effects on the one hand, and by compaction of the agglomerate structure due to capillary condensation effects on the other. The size of NH\(_4\)NO\(_3\)-BSA particles was apparently also influenced by volatilisation of NH\(_4\)NO\(_3\), but not as much as for pure salt particles, i.e. the protein inhibited the decomposition of NH\(_4\)NO\(_3\) or the evaporation of the decomposition products NH\(_3\) and HNO\(_3\). The efflorescence threshold of NaCl-BSA particles decreased with increasing BSA dry mass fraction, i.e. the protein inhibited the formation of salt crystals and enhanced the stability of supersaturated solution droplets.

The H-TDMA and TEM results indicate that the protein was enriched at the surface of the mixed particles and formed an envelope, which inhibits the access of water vapor to the particle core and leads to kinetic limitations of hygroscopic growth, phase transitions, and microstructural rearrangement processes.

The Köhler theory calculations performed with different types of models demonstrate that the hygroscopic growth of particles composed of inorganic salts and proteins can be efficiently described with a simple volume additivity approach, provided that the correct dry solute mass equivalent diameter and composition are known. A parameterisation for the osmotic coefficient of macromolecular substances has been derived from an osmotic pressure virial equation. For its application only the density and molar mass of the substance have to be known or estimated, and it is fully compatible with traditional volume additivity models for salt mixtures.

1 Introduction

The interaction of aerosol particles with water vapor and their activation as cloud condensation nuclei (CCN) are among the central issues of current research in atmospheric and climate science. Aerosols can scatter or absorb radiation, influence the formation of clouds and precipitation, and affect
the abundance of trace gases via heterogeneous chemical reactions and other multiphase processes (e.g. Andreae and Crutzen, 1997; Baker, 1997; Ravishankara, 1997; Seinfeld and Pandis, 1998; Finlayson-Pitts and Pitts, 2000; Ramana et al., 2001; Ramaswamy et al., 2001; Austin et al., 2003; Iziomon and Lohmann, 2003; Kulmala et al., 2003; and references therein). Moreover, they are of major importance with respect to air pollution control and can cause respiratory and cardiovascular diseases when deposited in the human respiratory tract (e.g. Finlayson-Pitts and Pitts, 1997; Seinfeld and Pandis, 1998; Finlayson-Pitts and Pitts, 2000; Pöschl, 2002; and references therein).

The primary parameters which determine the optical properties, CCN activity, reactivity, and deposition of aerosol particles are their size and composition. Depending on their sources and atmospheric processing (interaction with radiation, gases, and clouds), atmospheric particles consist of a complex mixture of organic and inorganic chemical components. Water can be adsorbed on the surface or contained in the bulk of the particles in variable amounts determined by the physico-chemical properties of the other particle components (wettability, water-solubility, hygroscopicity) and ambient conditions (temperature, relative humidity). The interaction of water-soluble inorganic salts and acids with water vapor is fairly well understood and considered to have a strong influence on atmospheric aerosol properties and effects (e.g. Pruppacher and Klett, 1997; Colberg et al., 2003; Martin et al., 2004; Pszenny et al., 2004; and references therein). For example, the critical supersaturation for cloud droplet formation on ultrafine aerosol particles composed of hygroscopic salts is much lower than for insoluble materials, and the scattering cross-sections of deliquesced ammonium sulfate particles at 90% relative humidity exceed those of dry particles by a factor of five or more (Tang, 1996; Malm and Day, 2001).

The understanding of the influence of organic compounds, however, is very limited (e.g. Pruppacher and Klett, 1997; Ming and Russell, 2001; Russell et al., 2002; Tsagaridis and Kanakidou, 2003; Ciezco, 2003; Martin and Bertram, 2003; Martin et al., 2004; Kärcher, 2004; Gysel et al., 2004; and references therein). Depending on sampling location and season, organics account for up to 50% or more of the dry mass of air particulate matter, but only a few percent of the individual compounds have been identified on a molecular level (e.g. Rogge et al., 1993; Saxena and Hildemann, 1996; Facchini et al., 1999a; Jacobson et al., 2000; Turpin et al. 2000; Matta et al., 2003; Pöschl, 2003; Sciare et al., 2003; Schneider et al., 2004; and references therein). Large fractions of the water-soluble organic particulate matter (up to ~50%) have been attributed to macromolecular compounds, including proteins and humic-like substances (Mukai and Ambe, 1986; Havers et al., 1998; Zappoli et al., 1999; Dececari et al., 2001). Proteins and protein derivatives account for up to ~10% of water-soluble organic carbon in fog water and fine particulate matter (PM2.5), can act as surfactants, react with trace gases like ozone and nitrogen oxides, and affect public health as allergens (Miguel et al., 1999; Franze et al., 2001; Zhang and Anastasio, 2003; Franze et al., 2003a, 2003b). Several laboratory studies have shown that particles composed of water-soluble organic compounds can take up water vapor and act as CCN (e.g. Cruz and Pandis, 1997; Corrigan and Novakov, 1999; Prenni et al., 2001; Prenni et al., 2003; Kumar et al., 2003). Organic surfactants can decrease the surface tension of aqueous droplets, enhance hygroscopic growth, reduce the critical supersaturation for cloud droplet formation, and enhance cloud albedo (Shulman et al., 1996; Facchini et al., 1999b). On the other hand, organic surface layers can inhibit the uptake of water vapor by liquid aerosol particles and influence the wettability of solid aerosol particles (e.g. Gill et al., 1983; Niessner and Helsper, 1985; Niessner et al., 1989; Hansson et al., 1990; Hämmerli et al., 1992; Andrews and Larson, 1993; Saxena et al., 1995; Xiong et al., 1998; Kotzick and Niessner, 1999).

To our knowledge, however, only a couple of experimental studies investigating the effect of macromolecular organic compounds on the hygroscopicity of atmospheric particles have been published (Chan and Chan, 2003; Gysel et al., 2004), and these were focused on humic-like substances. No experimental data for proteins and no Köhler theory models for this type of substances have been presented up to now.

Therefore, we have set out to investigate and characterise the hygroscopic growth of aerosol particles in the 100–200 nm size range composed of the protein bovine serum albumin (BSA) and the inorganic salts sodium chloride and ammonium nitrate by laboratory experiments and model calculations. BSA was chosen as a well-defined model substance for proteins and other macromolecular organic compounds. It is a globular protein with a molecular diameter on the order of ~5 nm and a molar mass of ~66.5 kg/mol, composed of a polypeptide chain of 583 natural α-aminoacid residues (Tanford, 1961; NCBI database, www.ncbi.nlm.nih.gov, AAN17824).

The experimental investigations have been performed with a hygroscopicity tandem differential mobility analyzer (HTDMA) and complemented by transmission electron microscopy (TEM). The principles of TDMA experiments have been described a couple of decades ago (Liu et al., 1978; Rader and McMurry, 1986), and a wide range of applications and modifications of this technique have been reported since then (e.g. Cruz et al., 2000; Hämmerli et al., 2000; Krämer et al., 2000; Joutsensaari et al., 2001; Weingartner et al., 2002; Väkevä et al., 2002; Maśling et al., 2003). The instrumentation and measurement procedures applied in this study are described below. Moreover, different models for Köhler theory calculations of the hygroscopic growth of particles containing inorganic salts and proteins or comparable organic macromolecules are outlined and tested against the experimental results.
2 Experimental

Aerosols were generated by nebulisation of an aqueous solution of the investigated pure substance or substance mixture (mass fraction 0.1%). The solutions were prepared by dissolving the appropriate amounts of bovine serum albumin (BSA, fraction V, >96%, Sigma), sodium chloride, and ammonium nitrate (NaCl, NH₄NO₃, >99.5%, Merck) in 250 mL of deionised water (18.2 MΩ cm, Milli Q plus 185, Millipore). The molecular masses of the investigated compounds and their densities at 298 K are summarised in Table 1. The applied cross-flow nebuliser (glass, self-made) was operated with a nitrogen carrier gas flow of 3.0 L/min. (99.999%, Messer-Griesheim) in a 500 mL three-neck glass flask containing the aqueous solution. 1.0 L/min of the generated aerosol flow was fed into the H-TDMA setup illustrated in Fig. 1. Antistatic tubing (Tygon, Norton) was used for all aerosol and gas flows. The gas flow rates were measured with rotameters (Rota Yokogawa) calibrated with a bubble flow meter (Gillian Gilibrator 2, Sensidyne, accuracy ±1%) and adjusted with needle valves (brass/steel, self-made) and tube clips (Roth). All H-TDMA experiments were performed at ambient temperature and pressure (298±2 K, 960 hPa).

<table>
<thead>
<tr>
<th></th>
<th>H₂O</th>
<th>NaCl</th>
<th>NH₄NO₃</th>
<th>BSA</th>
</tr>
</thead>
<tbody>
<tr>
<td>M (kg mol⁻¹)</td>
<td>0.01802</td>
<td>0.05844</td>
<td>0.08004</td>
<td>66.5</td>
</tr>
<tr>
<td>ρ (kg m⁻³)</td>
<td>997.1</td>
<td>2165</td>
<td>1725</td>
<td>1362</td>
</tr>
</tbody>
</table>

Two different operation modes were applied in the process of initial aerosol drying and neutralisation.

Neutralisation mode A: Usually the aerosol flow from the nebuliser flask was directly fed into a silica gel diffusion drier (SDD, self-made: fine steel mesh tube with 50 cm length and 1 cm i.d. surrounded by dense packing of silica gel in glass jacket with 10 cm i.d.), subsequently passed through a neutraliser (¹⁸⁵Kr, 2 mCi, TSI, Model 3077), and introduced into the first differential mobility analyzer, DMA 1 (self-made, similar to TSI Model 3071). Neutralisation mode A was applied for all experiments reported below unless mentioned otherwise.
Neutralisation mode B: For some test experiments the aerosol flow from the nebuliser flask was passed through a neutraliser (\(^{85}\)Kr, 10 mCi TSI Model 3054) before entering the SDD and DMA 1. To avoid water condensation inside the neutraliser, the aerosol flow was slightly diluted by dry nitrogen (\(~0.2\) L/min). The relative humidity, \(RH\), of the diluted (excess) flow was kept at or below 85\%. The capacitive humidity sensors (\(RH_{1} \approx RH_{4}\), Ahlborn FH A646, accuracy \(\pm 2\%RH\), precision \(\pm 0.5\%\)) were also used to measure the temperature (accuracy \(\pm 0.1\) K) of gas and aerosol flows in the H-TDMA system (Fig. 1).

DMA 1 was operated with a dry nitrogen sheath gas flow of 10 L/min, and by electrostatic classification a dry monodisperse aerosol with a geometric standard deviation of \(\sigma_{g}<1.1\) was selected. 0.3 L/min of the monodisperse aerosol flow was passed through a conditioner tube (length, 170 cm, i.d. 0.25 cm) to adjust the relative humidity (\(RH_{2}\)) by exchange of water vapor with a humidified nitrogen gas flow through a semi-permeable membrane (Nafion, Ansyco). The residence time of the aerosol flow in the conditioner and in the subsequent line leading to DMA 2 was 11 s (conditioning time).

The size distribution of the conditioned particles was measured with a scanning mobility particle sizer SMPS (DMA 2, TSI Model 3071; CPC TSI 3025; TSI AIM 4.3 software; aerosol inflow 0.3 L/min; pre-impactor nozzle 0.0508 cm; size range 14.8–487 nm; upscan time 120 s; retrace time 15 s; delay time 10 s; CPC flow 0.3 L/min and count time 0.1 s). DMA 2 was operated with a nitrogen sheath gas flow of 3.0 L/min with adjustable relative humidity (\(RH_{3}\)), which was controlled by mixing of dry nitrogen with a nitrogen gas flow saturated with water vapor. Two independent humidifier units were used for the sheath gas flow of DMA 2 and for the conditioner flow. The residence time of the aerosol flow in DMA 2 was 7.5 s.

The experimental setup allowed to run the combination of conditioner tube and DMA 2 in three different H-TDMA operation modes and to investigate three different processes:

- **H-TDMA mode 1 ("hydration")**: In this mode \(RH_{2}\) was varied from 0 to \(~95\%) with \(RH_{2}\sim 0.98 RH_{3}\). Keeping \(RH_{2}\) lower than \(RH_{3}\) allowed to study the hygroscopic growth, restructuring, and deliquescence of dry particles without hysteresis effects.

- **H-TDMA mode 2 ("dehydration")**: In this mode \(RH_{2}\) was varied from 0 to \(~95\%) with \(RH_{2}\sim 85\%\) for \(RH_{3}\sim 85\%\) and \(RH_{2}\sim RH_{3}\) for \(RH_{3}\sim 85\%\). Keeping \(RH_{2}\) above the deliquescence threshold allowed to study the hysteresis effect and efflorescence of deliquesced droplets.

- **H-TDMA mode 3 ("hydration & dehydration")**: In this mode \(RH_{2}\) was varied from 0 to \(~95\%) with \(RH_{2}\sim 0\) and \(RH_{2}\sim 10\%). Keeping \(RH_{2}\sim 0\) and \(RH_{2}\sim 10\%\) allows to study and compare the restructuring effects of humidification in the conditioner and drying in DMA 2 without droplet formation (\(RH_{2}\sim RH_{4}\)) or with intermediate droplet formation involving a full hysteresis cycle of deliquescence and efflorescence (\(RH_{2}\sim RH_{4}\)).

The applicability of DMA 2 for both particle drying and sizing in the reported hydration & dehydration experiments (H-TDMA mode 3) has been confirmed by test experiments in which the aerosol flow was dried to \(RH_{2}<5\%) before entering DMA 2. These experiments yielded essentially the same results and indicate near-instantaneous evaporation and efflorescence of solution droplets entering the DMA drift zone for electrostatic sizing in H-TDMA mode 3. Further investigations of phase transition kinetics and a detailed discussion of particle drying and sizing inside a DMA will be presented in a separate publication. This follow-up publication will also include analyses of size distribution standard deviations and broadening effects, which go beyond and are not required to support the conclusions of the present manuscript (Mikhailov et al., 2003).

Up to \(RH\sim 90\%) the relative humidity of the sheath flow (\(RH_{2}\)) and exhaust of DMA 2 (\(RH_{4}\)) agreed to within 2\%. For \(RH_{1}\sim 90\%, RH_{4}\) was lower by up to 4\% due to small temperature gradients in the system (differences up to 0.5 K). \(RH_{4}\) is considered to be most representative for the effective overall relative humidity in DMA 2 was thus used for all plots and calculations involving \(RH\) unless mentioned otherwise. The modal diameters (local maxima) of the particle size number distributions measured with the SMPS system have been used for plots and calculations involving the particle mobility equivalent diameter \(D_{b}\). They were determined from B-Spline fits to the SMPS measurement data (Origin 7.0 software, CPC raw counts vs. mobility equivalent diameter, 64 channels per decade; Mikhailov et al., 2003). The mobility equivalent particle growth factor, \(g_{b}\), was calculated as the ratio of the mobility equivalent diameter measured after conditioning (hydration, dehydration, or hydration & dehydration) to the initial mobility equivalent diameter of the particles selected by DMA 1, \(D_{b1}(g_{b}=D_{b1}/D_{b0})\). \(D_{b1}\) was measured at \(RH_{2}\sim RH_{3}\sim RH_{4}\sim 0\). The precision of particle diameter measurements was generally better than \(\pm 1\%\) (relative standard deviation of repeated measurements). The accuracy of particle sizing is estimated to be \(\pm 2\%\), which is confirmed by the good agreement of the measurement results for pure NaCl particles with literature data and model calculations.

In addition to the H-TDMA experiments with suspended particles, the morphology of deposited particles has been studied by transmission electron microscopy (TEM, EMMA-100). The TEM samples were prepared in a system analogous to the setup described above, but instead of sizing with a DMA the aerosol particles were deposited with a thermophoretic precipitator (self-made) on 3 mm nickel grids covered with formvar film. The particles were sampled either at the output of the SDD with \(RH\approx 35\%\), or after passing through a glass conditioner tube (residence time \(~20\) s) with \(RH\approx 70\%) and a second SDD. Immediately after deposition the particles were transferred into a silica gel desiccator, and
kept under dry conditions for 10 min before transfer into the TEM high vacuum system. The relative humidity of the ambient air to which the particles were exposed in the course of the sampling and TEM analysis procedures was kept below 32%.

3 Theory and models

3.1 Köhler theory and models of hygroscopic particle growth

According to Köhler theory, the relation between relative humidity and the size and composition of a spherical aqueous solution droplet suspended in a gas under equilibrium conditions can be described by (Pruppacher and Klett, 1997):

\[ S_w = a_w \exp\left(\frac{4 \sigma M_w}{\rho R T D_m}\right). \] (1)

The water vapor saturation ratio \( S_w \) is defined as the ratio of the actual partial pressure of water vapor to the equilibrium water vapor pressure over a flat surface of pure water at the given temperature. The relative humidity \( RH \) is identical to \( S_w \) expressed in percent. The activity of water in the solution droplet, \( a_w \), is defined as the ratio of equilibrium water vapor pressures over flat surfaces of the aqueous solution and of pure water. The exponential term of Eq. (1) is the so-called Kelvin or curvature term, which describes the increase of equilibrium water vapor pressure over a spherical droplet with the surface tension and the inverse of the droplet diameter \( D_m \) (geometric = mass equivalent diameter). \( M_w \) is the molar mass of \( \text{H}_2\text{O} \). \( R \) is the ideal gas constant, and \( T \) is the absolute temperature. \( \sigma \) and \( \rho \) are the surface tension and density of the aqueous solution, respectively.

The ratio of the droplet diameter, \( D_m \), to the mass equivalent diameter of a particle consisting of the dry solute (dissolved substance), \( D_{m,s} \), is defined as the mass equivalent growth factor of the dry solute particle, \( g_{m,s} \):

\[ g_{m,s} = \frac{D_m}{D_{m,s}} = \left(\frac{\rho_s}{x_s \rho}\right)^{1/3}. \] (2)

\( x_s \) is the mass fraction of the solute in the droplet, and \( \rho_s \) is the density of the dry solute. Equations (1) and (2) can be used to describe the hygroscopic growth of aerosol particles (\( D_m \) as a function of \( D_{m,s} \) and \( RH \)), if \( a_w, \rho, \) and \( \sigma \) are known as a function of droplet composition which is usually described by the mass fraction or molality of the solute. Solute molality, \( \mu_s \), mass fraction, \( x_s \), and molar mass, \( M_s \), are related by:

\[ \mu_s = \frac{x_s}{M_s (1 - x_s)} = \left(1 - \frac{1}{x_s}\right) M_s. \] (3)

3.1.1 Full parameterisation (FP) models

3.1.1.1 Empirical parameterisations of \( a_w, \rho, \) and \( \sigma \)

For some inorganic salts experimental data of the density and water activity of aqueous solution droplets have been determined with single-particle levitation techniques (Tang, 2000, and references therein). Tang (1996) presented experimental values of \( a_w \) and \( \rho \) as polynomial fit functions of solute mass fraction \( x_s \):

\[ a_w = 1 + \sum q c_q x_s^q, \] (4)

\[ \rho = \rho_w + \sum q d_q x_s^q. \] (5)

\( \rho_w \) is the density of pure water (997.1 kg m\(^{-3}\) at 298 K). The polynomial coefficients \( c_q \) and \( d_q \) for NaCl and NH\(_4\)NO\(_3\) at 298 K are listed in Table 2. These polynomial fit functions are valid up to high salt supersaturations (\( x_{\text{NaCl}}=48\% \) and \( x_{\text{NH}_4\text{NO}_3}=90\% \), respectively). The increase of the surface tension of aqueous solution droplets with increasing concentration of inorganic salts can be described with the formula proposed by Hänel (1976). Test calculations, however, have shown that the Kelvin term in Eq. (1) can be approximated with \( \rho = \rho_w \) and \( \sigma = \sigma_w = 0.072 \text{N m}^{-1} \) under the experimental conditions of this study (298 K, \( D_m \geq 100 \text{nm} \)). For pure NaCl particles the relative errors introduced by this simplifying assumption in the calculation of \( RH \) from Eq. (1) were less than 0.1%. Moreover, the increase of surface tension by inorganic salts is counteracted by surfactants such as proteins. In the FP model calculations which are based on the above empirical parameterisations and presented below for aqueous NaCl and NH\(_4\)NO\(_3\) solution droplets, \( x_s \) was taken as the primary variable to calculate \( a_w \) and \( \rho \) from Eqs. (4) and (5). \( \rho, \rho_s, M_s, x_s, \) and \( D_m,s \) were inserted into Eq. (2) to obtain \( D_m \), and finally \( D_{m,s}, a_w, \rho, M_s, \sigma = \sigma_w, \) and \( \rho = \rho_w \) were inserted in Eq. (1) to calculate the corresponding equilibrium value of \( RH \).
3.1.1.2 Ion-interaction parameterisations of \( \alpha_w \)

According to Robinson and Stokes (1970) the water activity of aqueous solutions of ionic compounds can be described by:

\[
\alpha_w = \exp(-v_\mu \Phi_s M_w). 
\]  

(6)

\( v_\mu \) is the stoichiometric dissociation number of the solute, i.e. the number of ions per formula unit (\( v_{\text{NaCl}}=v_{\text{NH}_4\text{NO}_3}=2 \)). \( \Phi_s \) is the molal or practical osmotic coefficient of the solute in aqueous solution. It describes the non-ideality of the solution, i.e. ion interactions and other effects leading to deviations from Raoult’s law (\( \Phi_{s,\text{ideal}}=1 \)). Based on an ion-interaction approach, Pitzer (1973) derived semiempirical parameterisations, which describe \( \Phi_s \) as a function of solute molality \( \mu_s \).

The general form for strong electrolytes dissociating into two types of ions is

\[
\Phi_s = 1 - |z_1 z_2| \left( A_\Phi \frac{\sqrt{T}}{1 + b_{\text{pit}} \sqrt{T}} \right) 
\]

\[
+ \frac{\mu_s}{v_s} \frac{2 v_1 v_2}{v_s} \left( \beta_0 + \beta_1 e^{-\alpha \sqrt{T}} \right) 
\]

\[
+ \mu_s^2 \frac{2 (v_1 v_2)^{3/2}}{v_s} C_\Phi. 
\]  

(7)

\( v_1 \) and \( v_2 \) are the numbers of positive and negative ions produced upon dissociation per formula unit of the solute (\( v_{\text{NaCl}}=v_{\text{NH}_4\text{NO}_3}=2 \)); \( z_1 \) and \( z_2 \) are the numbers of elementary charges carried by the ions. At 298 K the parameters \( \alpha \) and \( b_{\text{pit}} \) are 2 (kg/mol)^{1/2} and 1.2 (kg/mol)^{1/2}, respectively (Pitzer, 1973). The molal ionic strength is given by \( I=0.5 (\mu_1 z_1^2 + \mu_2 z_2^2) \). \( A_\Phi \) is the Debye-Hückel coefficient which equals 0.392 (kg/mol)^{1/2} for water at 298 K (Pitzer and Mayorga, 1973). The coefficients \( \beta_0, \beta_1 \) and \( C_\Phi \) depend on the chemical composition of the solute and have been tabulated by Pitzer and Mayorga (1973) for over 200 compounds (1:1, 1:2, and 2:1 electrolytes). For NaCl and some other inorganic salts of atmospheric relevance the above coefficients and their temperature dependence have been summarised by Gysel et al. (2002). For NaCl in H2O at 298 K the parameters are \( v_1=v_2=z_1=z_2=1, \beta_0=0.1017 \text{ kg mol}^{-1}, \beta_1=0.2769 \text{ kg mol}^{-1}, \text{ and } C_\Phi=-0.003227 \text{ kg}^2 \text{ mol}^{-2} \) (Mokbel et al., 1997).

The FP model calculations for aqueous NaCl solution droplets based on the semi-empirical parameterisation of \( \Phi_{\text{NaCl}} \) by Eq. (7) and presented below were performed in analogy to the FP model calculations based on the empirical parameterisations described above (Sect. 3.1.1.1). Only \( \alpha_w \) was calculated in a different way, namely by inserting \( v_{\text{NaCl}}=v_{\text{NH}_4\text{NO}_3}=2 \) and \( v_{\text{NaCl}}=v_{\text{NH}_4\text{NO}_3} \) in Eq. (3), \( \mu_{\text{NaCl}} \) in Eq. (7), and \( \mu_{\text{NaCl}}, \Phi_{\text{NaCl}} \) and \( v_{\text{NaCl}} \) in Eq. (6).

Figure 2a shows \( \Phi_{\text{NaCl}} \) calculated with Eq. (7) and plotted against \( \mu_{\text{NaCl}} \) in comparison to the values which can be obtained from the empirical parameterisation of \( \alpha_w \) using Eqs. (3), (4), and (6). The relative deviation exceeds 5% at very low and very high molalities (<0.1 mol kg\(^{-1}\), >8 mol kg\(^{-1}\)).

Clegg, Pitzer and co-workers have extended the semi-empirical parameterisations and developed a series of ion-interaction models for the calculation of the thermodynamic properties of highly concentrated aqueous solutions of inorganic salts relevant for the atmosphere (Aerosol Inorganics Model, AIM; Clegg and Pitzer, 1992; Wexler and Clegg, 2002) which are publicly available on the internet: http://www.hpc1.uea.ac.uk/~e770/aim/aim.htm. In the FP model calculations presented below for aqueous NH4NO3 droplets, the current online version of AIM II (Clegg et al., 1998) has been used to obtain \( M_{\text{NH}_4\text{NO}_3}, M_{\text{NaCl}} \) for given values of \( \alpha_w \). \( M_{\text{NH}_4\text{NO}_3} \) and \( M_{\text{NaCl}} \) were inserted into Eq. (3) to determine \( x_{\text{NH}_4\text{NO}_3} \), and the other variables were calculated as described above (Sect. 3.1.1.1).

3.1.2 Volume additivity (VA) models

Under the assumption that the volume of the solution droplet is given by the sum of the volumes of the dry solute and of the water contained in the droplet (volume additivity), the molality of the solute is given by (Pruppacher and Klett, 1997):

\[
\mu_s = \frac{m_s}{M_s m_w} = \frac{\rho_s D_{m,s}}{M_s \rho_w (D_{m,s}^3 - D_{m,s}^3)} = \frac{\rho_s}{M_s \rho_w (g_{m,s}^3 - 1)}. 
\]  

(8)

\( m_s \) and \( m_w \) are the masses of solute and water contained in the droplet, respectively. Combination of Eqs. (1), (6), and (8) leads to a simplified version of the Köhler equation:

\[
S_w = \exp \left( \frac{4 \sigma M_w}{\rho R T D_m} - \frac{v_\mu S_m}{M_s \rho_w (g_{m,s}^3 - 1)} \right). 
\]  

(9)

Based on the molar volumes of dry solute and pure water, \( V_{\text{m,s}}=M_s/\rho_s \) and \( V_w=M_w/\rho_w \), respectively, the activity of water in the droplet can be approximated by

\[
\ln a_w = -\frac{v_\mu \Phi_s}{(g_{m,s}^3 - 1)} V_w. 
\]  

(10)

VA model calculations can be performed with the above equations and the parameterisations for water activity and osmotic coefficients presented in the preceding section or on simplified parameterisations, which are also based on the assumption of volume additivity.

3.1.2.1 Simplified ion-interaction parameterisation of \( \Phi_s \)

Brechtel and Kreidenweis (2000) presented a simplified ion-interaction parameterisation of \( \Phi_s \) based on H-TDMA experiments. For the experimental conditions of their H-TDMA experiments (80% < RH < 95% and \( \mu_s=1-6 \text{ mol kg}^{-1} \)), they demonstrated that the parameterisation of \( \Phi_s \) by Pitzer and Mayorga (1973), Eq. (7), can be reduced to

\[
\Phi_s = 1 - |z_1 z_2| \left( A_\Phi \frac{\sqrt{T}}{1 + b_{\text{pit}} \sqrt{T}} \right) + \frac{\mu_s}{v_s} \frac{2 v_1 v_2}{v_s} \beta_0. 
\]  

(11)
Furthermore, they defined a coefficient

\[ c = \frac{1}{\rho_w (g_{m,s}^3 - 1)}, \]  

(12)

which can be calculated from H-TDMA measurement data under the assumption that the mass equivalent growth factor equals the measured mobility equivalent growth factor \((g_{m,s} = g_{b,s})\). From Eqs. (12) and (8) follows \(\mu_s = \rho_s c / M_s\), and combination with the above expression for molal ionic strength leads to a simplified version of Eq. (7):

\[ \Phi_s = 1 - \frac{A \times c^{1/2} \times \phi_f^{1/2}}{\sqrt{2} + b_{pit} c^{1/2} \phi_f^{1/2}} + 2 c \beta_{0,f} Y_f. \]  

(13)

\(\beta_{0,f}\) and \(Y_f\) are the only two parameters in Eq. (13) which depend on chemical composition of the dry solute particle. Brechtel and Kreidenweis (2000) determined these parameters for several salts by inserting Eq. (13) in Eq. (9), and fitting to H-TDMA measurement data in the range of 80% < RH < 92%. The reported fit values are \(\beta_{0,f} = 0.018 \text{ kg mol}^{-1}\) and \(Y_f = 77.4 \times 10^{-3} \text{ mol m}^{-3}\) for NaCl, and \(\beta_{0,f} = -0.004 \text{ kg mol}^{-1}\) and \(Y_f = 44.1 \times 10^{-3} \text{ mol m}^{-3}\) for NH₄NO₃.

Brechtel and Kreidenweis (2000) have also tested the sensitivity of Köhler model calculations on the simplifying assumptions made above. For NaCl, NH₄NO₃, (NH₄)₂SO₄, and several salt mixtures (average solute model, see below), they found that for \(RH > 75\%\) the errors arising from the volume additivity assumption and simplified parameterisation of \(\Phi_s\) were hardly larger than the uncertainties of more detailed modeling approaches and the measurement uncertainties of experimental investigations.

Figure 2a illustrates that for NaCl the differences between the full semi-empirical parameterisation (Eq. (7); Mokbel et al., 1997) and the simplified semi-empirical parameterisation (Eq. (13); Brechtel and Kreidenweis, 2000) exceed 10% only at high supersaturations (\(\mu_{NaCl} > 10 \text{ mol kg}^{-1}\)).

For VA model calculations based on the simplified semi-empirical parameterisation of \(\Phi_s\), \(g_{m,s}\) was taken as the primary variable. Equations (12) and (13) were used to calculate \(\Phi_s\), and \(D_{in}\) was obtained by inserting \(g_{m,s}\) and \(D_{in,s}\) in Eq. (2). Finally \(D_{in}, \Phi_s, \nu_s, M_w, \sigma = \sigma_w, \) and \(\rho = \rho_w\) were inserted in Eq. (9) to calculate the corresponding equilibrium value of \(RH\).

3.1.2.2 Osmotic pressure parameterisation of \(\Phi_s\)

For solute molecules which can be regarded as rigid spheres, Carnahan and Starling (1969) derived the following virial equation of osmotic pressure, \(P_{os}\):

\[ P_{os} = \frac{RT}{V_s} \left( \phi_s + \phi_s^2 - \phi_s^3 \right) \frac{1}{(1 - \phi_s)^3}. \]  

(14)

\(\phi_s\) is the volume fraction of the solute in the solution. Osmotic pressure and water activity of aqueous solutions are related by the basic equation (Atkins, 1982):

\[ \ln \alpha_w = - \frac{V_w}{RT} P_{os}. \]  

(15)

Substituting Eq. (14) into (15) we obtain

\[ \ln \alpha_w = - \frac{V_w \phi_s (1 + \phi_s + \phi_s^2 - \phi_s^3)}{V_s (1 - \phi_s)^3}. \]  

(16)

From the volume additivity assumption follows \(\phi_s = g_{m,s}^{-3}\), and with \(\nu_s = 1\) Eq. (10) can be transformed into

\[ \ln \alpha_w = - \frac{\Phi_s}{(1/\Phi_s - 1) V_s}. \]  

(17)

Combination of (16) and (17) yields

\[ \Phi_s = \left( \frac{1}{\phi_s} - 1 \right) \frac{\phi_s (1 + \phi_s + \phi_s^2 - \phi_s^3)}{(1 - \phi_s)^3} = 1 + \phi_s (3 - \phi_s^2) (1 - \phi_s)^2. \]  

(18)
and by inserting \( \Phi_s = g_{m,s}^{-3} \) we obtain

\[
\Phi_s = 1 + \frac{g_{m,s}^{-3} (3 - 8 g_{m,s}^{-6})}{(1 - g_{m,s}^{-3})^2}.
\]  

(19)

Figure 2b shows the molal osmotic coefficient of BSA, \( \Phi_{BSA} \), calculated from Eq. (8) and (19) as a function of \( \mu_{BSA} \). \( \Phi_{BSA} \) increases from a lower limit of 1 at low molalities (ideal dilute solution) to values of 100 and more at \( \mu_{BSA} > 0.1 \), which reflects the high molar volume of the protein.

3.1.2.3 Average solute volume additivity (AS-VA) model for multi-component particles

In order to apply Eq. (9) for aerosol particles and aqueous droplets containing multiple solute components, the solute mixture has to be regarded as a single compound (“average solute”). This approach has been used to model the hygroscopic growth of particles composed of inorganic salt mixtures, and effective values of \( M_s, \rho_s, \) and \( v_s, \Phi_s \), have been obtained by weighted averaging of the properties of the individual solute components (Pruppacher and Klett, 1997):

\[
M_s = \sum_y x_{s,y} M_y,
\]  

(20)

\[
\rho_s = \left( \sum_y \frac{x_{s,y}}{\rho_y} \right)^{-1},
\]  

(21)

\[
v_s \Phi_s = \frac{\sum_y v_y \Phi_y \mu_y}{\sum_y \mu_y},
\]  

(22)

\( x_{s,y} \) and \( x_{s,y} \) are the mole and mass fractions of component \( y \) in the dry solute particle; \( M_y, v_y, \rho_y \) are the molar mass, stoichiometric dissociation number, and density of the pure component, respectively. \( \mu_y \) is the molality of component \( y \) in the mixed aqueous solution droplet, and \( \Phi_y \) is the osmotic coefficient of a reference aqueous solution which contains component \( y \) with the same molality as the mixed solution droplet, \( \mu_y \), but as the only solute.

For model calculations it is convenient to express \( x_{s,y} \) and \( \mu_y \) in terms of \( x_{s,y} \):

\[
x_{s,y} = x_{s,y}/M_y,
\]  

(23)

\[
\mu_y = \frac{m_y}{M_y m_w} = \frac{\rho_s x_{s,y}}{\rho_s (g_{m,s}^3 - 1)},
\]  

(24)

In the AS-VA model calculations for mixed protein-salt particles presented below, \( g_{m,s} \) and \( x_{s,y} \) were taken as the primary input variables. Equations (20), (21), and (23) were applied to calculate \( M_s \) and \( \rho_s \), respectively. \( \mu_y \) and \( \Phi_y \) were calculated for every individual component based on Eq. (24) and on the parameterisations presented above for aqueous solutions of pure solutes. \( v_s \Phi_s \) was calculated from Eq. (22), and \( D_m \) was obtained by inserting \( g_{m,s} \) and \( D_m \) in Eq. (2). Finally, \( D_m, v_s \Phi_s, M_y, \rho_s, M_w, \sigma = \sigma_w, \) and \( \rho = \rho_w \) were inserted in Eq. (9) to obtain the corresponding equilibrium value of RH.

Obviously, the molalities of the individual components, \( \mu_y \), have to be inserted for \( \mu_y \) in the ion-interaction parameterisations presented above to calculate \( \Phi_y \). To calculate \( \Phi_y \), from the osmotic pressure parameterisation, an effective growth factor for the individual solute component \( g_{eff,y} \) has to be used instead of the overall mass equivalent growth factor \( g_{m,s} \) in Eq. (19). \( g_{eff,y} \) is the mass equivalent growth factor of a reference aqueous solution droplet which contains component \( y \) with the same molality as the mixed solution droplet, \( \mu_y \), but as the only solute:

\[
\mu_y = \frac{\rho_y}{M_y \rho_w (g_{eff,y}^3 - 1)^2},
\]  

(25)

\[
g_{eff,y} = \left( \frac{\rho_y}{\rho_s x_{s,y} (g_{m,s}^3 - 1)} \right)^{1/3}.
\]  

(26)

Based on the volume additivity assumption, \( g_{eff,y}^3 \) can be regarded as the volume fraction of the pure solute \( y \) in the reference solution, and thus \( g_{eff,y} \) can be inserted for \( g_{m,s} \) in Eq. (19) to calculate \( \Phi_y \).

3.1.2.4 Separate solute volume additivity (SS-VA) model for multi-component particles

Under the assumption that different solute components contained in a multi-component particle do not interact with each other (“separate solutes”), Eq. (1) can be generalised in the form

\[
S_w = \prod_y a_{w,y} \exp \left( \frac{4 \sigma M_w}{\rho RT D_m} \right).
\]  

(27)

\( a_{w,y} \) is the activity of water in an aqueous solution droplet containing only one specific solute component \( y \). Based on the volume additivity assumption and in analogy to the derivation of Eq. (9) from Eq. (1), Eq. (27) can be transformed into

\[
S_w = \exp \left( \frac{4 \sigma M_w}{\rho RT D_m} - \frac{M_w}{\rho_w (g_{m,s}^3 - 1)} \sum_y v_y \Phi_y \rho_y x_{s,y} \right).
\]  

(28)

The SS-VA model calculations for mixed protein-salt particles presented below were performed in analogy to the AS-VA calculations described above (Sect. 3.1.2.3), except that the parameters describing the individual solute components \( (M_y, \rho_y, x_{s,y}, \mu_y, v_s, \Phi_y) \) were not averaged but directly inserted in Eq. (28).
3.2 Particle shape factors

The shape and microstructure of an aerosol particle can be characterised by its dynamic shape factor $\chi$, which is defined as the ratio of the drag force on the particle to the drag force on the particle’s mass equivalent sphere at the same velocity (Fuchs, 1964). $\chi$ relates the mobility equivalent diameter of a particle to its mass equivalent diameter (Brockmann and Rader, 1990; Kelly and McMurry, 1992):

$$\frac{D_m}{D_b} = \frac{1}{\chi} \cdot \frac{C(D_m)}{C(D_b)},$$  

(29)

the slip correction factors $C(D_m)$ and $C(D_b)$ can be approximated by the empirical relation

$$C(D) = 1 + \left(\frac{2\lambda}{D}\right) \left(1.142 + 0.558 \exp\left(-0.999 \frac{D}{2\lambda}\right)\right),$$  

(30)

into which the appropriate particle diameter $D$ and the mean free path of the gas molecules $\lambda$ are inserted ($\lambda \approx 70$ nm for nitrogen at 298 K and 960 hPa; Allen and Raabe, 1985; Willeke and Baron, 1993).

For compact spherical and cubic particles the dynamic shape factors are $\chi_{\text{sphere}}=1.00$ and $\chi_{\text{cube}}=1.08$, respectively. For agglomerates and irregularly shaped particles $\chi$ increases to values of 2 and more (Hinds, 1999; Brockmann and Rader, 1990; Willeke and Baron, 1993; Krämer et al., 2001). $\chi$ can be split into a component $\kappa$ which describes the shape of the particle envelope and a component $\delta$ which is related to the particle porosity and allows the calculation of the void fraction inside the particle envelope, $f$ (Brockmann and Rader, 1990):

$$\chi = \kappa \frac{C(D_m)}{C(D_b)},$$  

(31)

$$f = (1 - \delta^{-3}).$$  

(32)

4 Results and discussion

4.1 Pure sodium chloride particles

4.1.1 Hygroscopic growth

The experimental results obtained for pure NaCl particles with $D_{b,i}=99$ nm in H-TDMA modes 1 (hydration) and 2 (dehydration) are summarised in Table 3 and illustrated in Fig. 3, which shows the measured particle diameter plotted against relative humidity. Upon hydration, the deliquescence transition, i.e. the transformation of the solid salt particle into a saturated solution droplet, was observed at $RH_d=(75\pm2)$%, which is in good agreement with theoretical predictions ($RH_d=75.3$%: Tang and Munkelwitz, 1993) and experimental literature data (Tang et al., 1977; Krämer et al., 2000; Gysel et al., 2002). At $RH<RH_d$ the measured mobility equivalent diameters exhibited a slight decrease towards the deliquescence threshold, where a minimum value $D_{b,\text{hy,min}}=97$ nm was observed (average value for 60–75% $RH$; see also Fig. 4). At $RH>RH_d$ the measured diameters agree very well with Köhler theory calculations performed with the FP model based on $\Phi_{\text{NaCl}}$ from Mokbel et al. (1997), on $\rho$ from Tang (1996), and on the assumption $D_{m,s}=D_{b,\text{hy,min,blcorr}}=95$ nm, which will be discussed below.

The hysteresis branch measured upon dehydration is due to the existence of solution droplets in a metastable state of NaCl supersaturation ($RH_e<RH<RH_d$). The efflorescence transition, i.e. the formation of a salt crystal and evaporation...
Table 3. Phase transition and microstructural rearrangement parameters for pure NaCl particles and mixed NaCl-BSA particles with initial diameter $D_{b,i}=99$ nm. $RH_d$ and $RH_e$ are the relative humidities at which deliquescence and efflorescence were observed, respectively. $\Delta_{r,d}D_b$ and $\Delta_{r,e}D_b$ are the relative changes of mobility equivalent diameter upon deliquescence and efflorescence, respectively, referring to the diameters measured just before and after the phase transition. $g_{b,hy,min}$ and $g_{b,de,min}$ are the minimum mobility equivalent growth factors observed upon hydration and dehydration, respectively. The measurement precision was generally better than ±2% for $RH$ and ±1% for $D_b$.

<table>
<thead>
<tr>
<th>BSA Dry Mass Fraction (%)</th>
<th>$RH_d$ (%)</th>
<th>$RH_e$ (%)</th>
<th>$\Delta_{r,d}D_b$ (%)</th>
<th>$\Delta_{r,e}D_b$ (%)</th>
<th>$g_{b,hy,min}$</th>
<th>$g_{b,de,min}$</th>
</tr>
</thead>
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<tr>
<td>0</td>
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<td>41</td>
<td>76</td>
<td>-29</td>
<td>0.98</td>
<td>1.01</td>
</tr>
<tr>
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<td>40</td>
<td>69</td>
<td>-29</td>
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<td>0.94</td>
</tr>
<tr>
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<td>73</td>
<td>38</td>
<td>89</td>
<td>-18</td>
<td>0.86</td>
<td>0.91</td>
</tr>
<tr>
<td>50</td>
<td>74</td>
<td>37</td>
<td>36</td>
<td>-13</td>
<td>0.89</td>
<td>0.88</td>
</tr>
<tr>
<td>50*</td>
<td>74</td>
<td>37</td>
<td>34</td>
<td>-13</td>
<td>0.91</td>
<td>0.90</td>
</tr>
<tr>
<td>75</td>
<td>75</td>
<td>36</td>
<td>7</td>
<td>-6</td>
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<td>0.84</td>
</tr>
<tr>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>0.94</td>
</tr>
</tbody>
</table>

*Neutralisation mode B

Fig. 5. Mobility equivalent growth factors of NaCl particles with $D_{b,i}=99$ nm and $D_{b,i}=201$ nm observed upon hydration & dehydration (H-TDMA mode 3, RH2).

of the liquid water content, was observed at $RH_e=(41±2)$%.
This is at the lower end of the range of efflorescence relative humidities reported in the literature, 37% $< RH_e <$ 50% (Martin, 2000; Tang, 2000; Krieger and Braun, 2001; and references therein). Higher values are generally attributed to heterogeneous nucleation on impurities (Lightstone et al., 2000; Tang, 2000). After efflorescence ($RH < RH_e$), the mobility equivalent diameters measured upon dehydration were slightly larger than the initial diameter.

Figure 4 displays the mobility equivalent growth factors, $g_{b}=D_b/D_{b,i}$, calculated from the diameter measurement data displayed in Fig. 3 for the non-deliquesced particles upon hydration ($RH < RH_d$) and dehydration ($RH < RH_e$). Their deviations from unity exceed the usual scatter related to diameter measurement precision (±1%) and can be attributed to microstructural rearrangement processes, as detailed below.

4.1.2 Microstructural rearrangement

Figure 5 illustrates the results obtained for pure NaCl particles with $D_{b,i}=99$ nm and $D_{b,i}=201$ nm in H-TDMA mode 3 (hydration & dehydration), where the relative humidity was varied only in the conditioner tube ($RH_2$) whereas DMA 2 was used not only as a particle sizer but also as a dryer ($RH_3=0$, $RH_4<10$%). At $RH_2 < RH_d$ the particles with $D_{b,i}=99$ nm exhibited essentially the same small mobility equivalent diameter reduction as observed in operation mode 1, and the mobility equivalent growth factor, $g_{b}=D_b/D_{b,i}$, decreased towards the deliquescence threshold, where an average minimum value of $g_{b,min}=0.99$ was observed (average value in the $RH$ range of 60–73%). At the deliquescence threshold ($RH_d=75$%), $g_{b}=D_b/D_{b,i}$ showed a step-wise increase to a near-constant value of 1.02, i.e. a reproducible 3% increase of the dry particle mobility equivalent diameter occurred after deliquescence in the conditioner tube and efflorescence in DMA 2 ($RH_2 - RH_d$). Similar but more pronounced effects were observed for the larger particles with $D_{b,i}=201$ nm. For these particles $g_{b}=D_b/D_{b,i}$ was near unity up to $RH_2=30\%$ and exhibited a near-linear decrease in the humidity range of 30–55% and an average minimum value of $g_{b,min}=0.96$ at 55% $< RH_2 < RH_d$. After a stepwise increase by 4% the growth factor observed at $RH_2 - RH_d$ was close to unity again.

The different morphologies and microstructures reported for NaCl aerosol particles range from solid spheres or cubes to fractal agglomerates, depending on the aerosol generation method and conditioning or physical aging of the
investigated aerosol (Krämer et al., 2000; and references therein). Assuming that the mass equivalent diameter $D_m$ is practically constant for NaCl salt particles at $RH < RH_e$, Eq. (29) can be rewritten as

$$\frac{D_{b,j}}{D_{b,k}} = \frac{\chi_j C(D_{b,j})}{\chi_k C(D_{b,k})} = \frac{g_{b,j}}{g_{b,k}},$$

where $D_{b,j}$, $D_{b,k}$, $g_{b,j}$, and $g_{b,k}$ stand for the mobility equivalent diameters and growth factors of the investigated particles observed in two arbitrary microstructural states $j$ and $k$, respectively. Inserting the experimental data in Eq. (29) and (30) yields $\chi_{h&d,e}/\chi_{h&d,min}=1.06$ for $D_{b,i}=99\text{ nm}$ and $\chi_{h&d,e}/\chi_{h&d,min}=1.07$ for $D_{b,i}=201\text{ nm}$, which is close to the theoretical value of $\chi_{cube}/\chi_{sphere}=1.08$. $\chi_i$, $\chi_{h&d,min}$ and $\chi_{h&d,e}$ are the shape factors of the initially selected particles, the minimum diameter particles, and the effloresced particles observed in H-TDMA mode 3 (hydration & dehydration, $RH_2 > RH_d$), respectively.

The simplest possible explanation for the above results is that the NaCl particles with $D_{b,i}=99\text{ nm}$ selected by DMA 1 had an irregular shape ($\chi_{sphere} < \chi_{cube}$), underwent transformation to near-spherical shape upon interaction with water vapor up to the deliquescence threshold ($RH_2 < RH_d$), and recrystallisation to near-spherical shape after efflorescence in DMA 2 ($RH_2 > RH_d$). The particles with $D_{b,i}=201\text{ nm}$, on the other hand, seem to have undergone a transformation from near-cubic or irregular to near-spherical shape ($60% < RH_2 < RH_d$) and back to near-cubic shape upon efflorescence in DMA 2 ($RH_2 > RH_d$).

The irregular initial shape of the aerosol particles with $D_{b,i}=99\text{ nm}$, the near-cubic initial shape of the aerosol particles with $D_{b,i}=201\text{ nm}$, and their transformation from near-cubic to near-spherical shape upon interaction with water vapor at $RH < RH_d$ were confirmed by transmission electron microscopy (TEM) of deposited particles, which have been prepared as described in Sect. 2. Figure 6 (A1) shows NaCl particles sampled at the output of the SDD with $RH \approx 35%$. The larger particles with diameters near 200 nm exhibit near-cubic shape, whereas the smaller particles with diameters near 100 nm exhibit irregular shapes. Figure 6A2 shows NaCl particles after humidification ($RH \approx 70%$, 20 s). In this case only a large particle with a diameter of $\approx 500\text{ nm}$ exhibits near-cubic shape with rounded corners, but all smaller particles exhibit near-spherical shape.

Overall, the observations can be interpreted by the following hypotheses:

1. NaCl aerosol particles in the 100–200 nm size range freshly formed by efflorescence of aqueous NaCl solution droplets are of (near-)cubic shape.

2. Upon interaction with water vapor at $RH < RH_d$, surface adsorbed water partially dissolves the salt surface – preferentially at the corners and edges of the crystals – and thus transforms the near-cubic into near-spherical particles.

3. The microstructural rearrangement by partial dissolution of the crystal surface upon interaction with water vapor is kinetically limited (interaction time and relative humidity).

Hypothesis 1 explains why the hydration & dehydration experiments indicate near-cubic shape for both the particles with $D_{b,i}=99\text{ nm}$ and those with $D_{b,i}=201\text{ nm}$ after efflorescence in DMA 2, regardless of their microstructural before deliquescence in the conditioner tube. Hypothesis 2 explains the transformation from near-cubic or irregular to near-spherical shape at $RH < RH_d$. Hypothesis 3 explains the observed differences between 100 nm and 200 nm particles and between particle drying in the SDD and in DMA 2 operated in H-TDMA modes 2 and 3.

In the SDD (residence time $\approx 10\text{ s}$) the relative humidity of the freshly generated aerosol flow was decreased from $\approx 100\%$ in the nebuliser to $\approx 38\%$, i.e. just below the experimental value of $RH_e$. Thus the solid particles formed upon efflorescence could interact with water vapor at $RH \approx 38\%$ in the tubing and neutralizer between the SDD and DMA 1 (residence time $\approx 10\text{ s}$), before they were further dried by the dry nitrogen sheath gas and size selected. Apparently this relative humidity and interaction time were sufficient to convert the 100 nm salt particles to near-spherical shape. For the 200 nm salt particles, however, higher relative humidities were required to reach near-spherical shape: $RH > 55\%$ in the conditioner tube (residence time $\approx 11\text{ s}$).

In DMA 2 operated in H-TDMA mode 3, particle drying proceeded much faster and more efficient than in the SDD. By addition of the dry nitrogen sheath gas the relative humidity was effectively decreased by a factor of ten within a couple of seconds (flow channel width between outer steel cylinder and central electrode of DMA 2: 1.07 cm; root mean square distance of diffusion of H$_2$O in air within 1 s at standard temperature and pressure: $\approx 0.6$ cm) (Atkins, 1982). The resulting relative humidities of $< 10\%$ experienced by the particles after efflorescence in DMA 2 (residence time 7.5 s) were apparently too low to transform them from near-cubic to near-spherical shape.

These humidity differences and the postulated kinetic limitation can explain why the particles with $D_{b,i}=99\text{ nm}$ exhibited a stronger increase of mobility equivalent diameter after efflorescence in H-TDMA mode 3 (Fig. 5; $g_{b,h&d,e}=1.02; RH_2 > RH_d, RH_3=0; RH_4 < 10\%$) than after efflorescence in H-TDMA mode 2 (Fig. 4; $g_{b,h&d,e}=1.01, RH_2 > RH_d, RH_3> RH_d < RH_4$). The fact that the hydration & dehydration experiments indicate a gradual transformation of the particles with $D_{b,i}=201\text{ nm}$ from near-cubic to near-spherical shape upon interaction with water vapor at $30% < RH < RH_d$ in the conditioner tube (interaction time $\approx 11\text{ s}$) but not in DMA 2 (decrease of $RH$ from $> RH_d$ to $\approx 10\%$ within $\approx 1\text{ s}$) also supports a kinetic limitation of the microstructural rearrangement process.
Fig. 6. TEM micrographs of deposited aerosol particles composed of sodium chloride (NaCl, high contrast) and bovine serum albumin (BSA, low contrast): pure NaCl particles before conditioning (A1) and after conditioning at RH=70% (A2); mixed BSA-NaCl particles with BSA dry solute mass fractions of 25% (B1) and 50% (B2, B3); pure BSA particles (C1).

Moreover, the postulated kinetic limitation is in agreement with the results of Weis and Ewing (1999), who investigated the interaction of water vapor with NaCl aerosol particles with a median diameter of 0.4 µm by optical spectroscopy. They found that equilibration at RH=12–44% was reached after 3–6 s, i.e. the same timescale of the H-TDMA experiments.

On the other hand, the apparent kinetic limitation does not exclude additional thermodynamic limitations, which might govern the maximum extent of conversion from near-cubic to near-spherical shape that can be reached at a given relative humidity. Additional experiments with varying interaction times will be required to find out whether the intermediate stages of restructuring observed for the particles with $D_{b,i}=201$ nm at $RH_2<RH_d$ in H-TDMA mode 3 are thermodynamically stable, or if all particles would be converted to near-spherical shape after sufficiently long interaction times.

Another aspect to be investigated in further experiments is the potential influence of electric charges on the involved processes (Pruppacher and Klett, 1997; Brodskaya et al., 2002). In this study all experiments reported for pure NaCl particles were performed in neutralisation mode A, i.e. the drying process in the SDD took place before the particles were neutralised and size selected. Thus the particles which carried one elementary charge upon size-selection in DMA 1 and determined the initial mobility equivalent diameter $D_{b,i}$ might have carried more than just one elementary charge upon efflorescence and crystallisation in the SDD. The particles measured after hydration and dehydration in H-TDMA mode 3, however, can be assumed to have carried only one elementary charge upon efflorescence and crystallisation in DMA 2. Consequently different states of electrical charging may have contributed to the observed differences between particle drying in the SDD and in DMA 2. On the other hand,
electrical charge effects are neither required to explain the observations, nor do they appear to be sufficient to replace one of the effects and processes postulated in hypotheses 1–3. Therefore we suppose that charging effects might limit or modify but hardly overthrow hypotheses 1–3.

Microstructural rearrangements of NaCl aerosol particles in H-TDMA experiments at $RH < RH_d$ have been reported in a couple of earlier studies. Krämer et al. (2000) found that the mobility equivalent diameter of dry NaCl high-temperature condensation aerosol particles in the 20–100 nm size range decreased by up to 50% upon interaction with water vapor at $RH < RH_d$, which they attributed to a transformation of sparse branched-chain to more compact but still porous agglomerates. For NaCl aerosol particles generated by nebulisation and drying of salt solution droplets Krämer et al. (2000) observed no significant restructuring effects; the results implied a non-porous compact particle structure but allowed no conclusive distinction between near-cubic and near-spherical envelope shape. Gysel et al. (2002), on the other hand, found that the mobility equivalent diameter of NaCl aerosol particles generated by nebulisation and drying of salt solution droplets decreased by up to 9% when $RH$ was increased from 20% to $RH_d$. They attributed these changes to the elimination of initial particle shape irregularities but provided no detailed structural interpretation of their observations.

4.1.3 Model calculations

For accurate model calculations of hygroscopic growth, the mass equivalent diameter of the dry solute particles, $D_{m,s}$, has to be known. The H-TDMA results and TEM pictures described above indicate near-spherical shape for the particles conditioned at relative humidities of 70–75%, which implies that the minimum mobility equivalent diameter values observed under these conditions, $D_{b,min}$, should be near-identical to the mass equivalent diameter of the investigated particles. On the other hand, the observed microstructural rearrangements indicate that significant amounts of water can be adsorbed on the particle surface (“hydration layer”). Foster and Ewing (1999) have investigated the adsorption of water on the surface of NaCl (100) with infrared spectroscopy, and for $RH \sim 65\%$ (303 K) they found that the surface was covered by about 3 monolayers of water, which corresponds to a liquid-like film of about 1 nm thickness. Thus we have estimated the actual dry solute mass equivalent diameter of the particles with $D_{b,i}=99$ nm by subtraction of 2 nm from the minimum mobility equivalent diameter observed upon hydration. $D_{b,hy,min}$ (Figs. 4 and 5): $D_{m,NaCl}=D_{b,hy,min,hlcorr}=95$ nm.

In Fig. 7 the measurement data from the upper branch of the hysteresis curve in Fig. 2 (hydration, dehydration, $RH > 40\%$) are compared with calculations using different models and dry solute mass equivalent diameters. The best agreement was achieved with $D_{m,NaCl}=D_{b,hy,min,hlcorr}=95$ nm inserted in the FP models based $a_w$ and $\rho$ from Tang (1996) and $\Phi_{NaCl}$ from Mokbel et al. (1997) and $\rho$ from Tang (1996), respectively. The diameters calculated with these models generally deviated by less than ±2% from each other and from the measurement data. Above $RH_d$ also the VA model based on $\Phi_{NaCl}$ by Brechtel and Kreidenweis (2000) agreed well with the FP models. For supersaturated solution droplets, however, the VA model diameters were systematically higher by up to +7% ($RH = 40\%$), which reflects the deviations of the different parameterisations for $\Phi_{NaCl}$ at high $\Phi_{NaCl}$ (Fig. 2a). Accordingly, VA model calculations based on the assumption of near-ideal solute properties with $\Phi_{NaCl}=1$ were up to 10% lower than the FP model calculations. The influence of dry solute mass equivalent diameter is illustrated by FP model calculations ($\Phi_{NaCl}$ from Mokbel et al. (1997); $\rho$ from Tang (1996)) with $D_{m,NaCl}=D_{b,i}=99$ nm. The resulting diameters are 4% higher throughout the investigated $RH$ range, and demonstrate that deviations due to incorrect estimation of the dry solute mass equivalent diameter can easily exceed deviations due to different modeling approaches, in particular at high relative humidities.

4.2 Pure ammonium nitrate particles

4.2.1 Hygroscopic growth

The experimental results obtained for pure $\text{NH}_4\text{NO}_3$ particles with $D_{b,i}=99$ nm in HTDMA modes 1 and 2 are
No distinct deliquescence or efflorescence transitions were observed, which is most probably due to a liquid-like state of the particles selected by DMA 1. In single particle levitation experiments by Richardson and Hightower et al., 1998), they observed no efflorescence, which is consistent with earlier observations of liquid-like anhydrous NH₄NO₃ particles at RH≈0% in single particle levitation experiments by Richardson and Hightower (1987). Thus we assume that the NH₄NO₃ particles selected by DMA 1 were not solid crystals but supersaturated liquid droplets, which underwent no deliquescence or efflorescence transitions.

Nevertheless, the mobility equivalent diameters observed upon dehydration in the RH range of 40–80%, i.e. below and above the theoretical deliquescence threshold, were up to 10% higher than the ones observed upon hydration. Due to the above considerations, the different mobility equivalent diameters cannot be attributed to a simple hysteresis between solid particles and liquid droplets or rearrangement of solid particle microstructure (shape and porosity) as described for NaCl.

Instead, the differences have to be explained by other processes which depend on particle pre-conditioning and lead to differences in particle mass (total content of H₂O and NH₄NO₃) or chemical structure (crystalline or liquid-like modifications of the condensed phase), as will be discussed below.

4.2.2 Chemical decomposition and evaporation

Figure 9 displays the mobility equivalent growth factors, \( g_{\text{hy}} = \frac{D_{\text{h},i}}{D_{\text{h},i}} \), calculated from the diameter measurement data displayed in Fig. 8 for RH<50%, i.e. for the range of relative humidities where no hygroscopic growth but significant diameter reductions were observed. Upon hydration, \( g_{\text{hy}} \) was near unity up to RH≈10%, decreased by ~3% in the RH range of 10–20%, and exhibited a minimum value of \( g_{\text{hy},\text{min}} = 0.97 \) at RH=20–30%. In the RH range of 30–40%, \( g_{\text{hy}} \) re-increased to unity, and for RH>40% it increased further as illustrated in Fig. 8. Upon dehydration \( g_{\text{de}} \) was slightly below unity in the RH range of 20–40% with \( g_{\text{de},\text{min}} = 0.99 \).

Figure 10 illustrates the results obtained for pure NH₄NO₃ particles with \( D_{\text{b},i} = 99 \) nm and \( D_{\text{b},i} = 100 \) nm in H-TDMA mode 3 (hydration & dehydration). In analogy to modes 1 and 2 the mobility equivalent growth factor in mode 3 was near unity up to RH≈10%, but at higher relative humidity it exhibited a much more pronounced decrease by up to 10%, reaching a minimum value of \( g_{\text{h\&d},\text{min}} = 0.30 \) at RH=60–70%, followed by a re-increase to unity at RH≈95%.

Depending on temperature, pressure, humidity, and purity, ammonium nitrate can exist in several solid and liquid-like modifications with different chemical structures and densities (Clegg et al., 1998; Martin, 2000). Thus some of the effects described above could be due to transitions.
between different chemical structures of solid or liquid-like ammonium nitrate ("chemical restructuring"). On the other hand, NH$_4$NO$_3$ can also undergo chemical decomposition and evaporation in the form of NH$_3$ and HNO$_3$, leading to a loss of particle mass and reduction of dry solute mass equivalent diameter.

Lightstone et al. (2000) reported a significant loss of particle mass after a cycle of hydration and dehydration in their single particle levitation experiments with micrometer-sized NH$_4$NO$_3$ particles. They found that the volatilisation of NH$_4$NO$_3$ proceeded most efficiently in supersaturated droplets at RH $\leq$ 40%. Richardson and Hightower (1987) reported that the rate of decomposition and evaporation of NH$_4$NO$_3$ in liquid-like particles was about 20 times higher than for solid particles.

Our H-TDMA measurement results do not allow an unambiguous discrimination between the potential contributions of possible chemical restructuring or decomposition and evaporation to the mobility equivalent diameter decrease observed upon interaction of the investigated ammonium nitrate particles with water vapor. They demonstrate, however, that substantial effects and changes can occur on the multi-second time-scale of the H-TDMA experiments.

The fact that near-unity growth factors at very low and very high relative humidity with a pronounced minimum in between were observed in H-TDMA mode 3 (Fig. 10), which comprises a complete cycle of hydration and dehydration, clearly indicates that the restructuring or volatilisation was kinetically limited and most efficient at medium relative humidities. The most probable explanation for the results of H-TDMA mode 3 is chemical decomposition and evaporation of NH$_4$NO$_3$ with a maximum rate in supersaturated aqueous droplets (medium RH) and much lower rates in anhydrous NH$_4$NO$_3$ (low RH) and dilute aqueous solution droplets (high RH). This explanation is also consistent with the larger diameters observed in H-TDMA mode 2 relative to mode 1 at 40–80% RH (Fig. 8), since the particles in mode 2 are mostly kept at high RH (RH$_2$ $\geq$ 85%) and experience medium RH values only in DMA 2.

4.2.3 Model calculations

In Fig. 8 the measurement data obtained for NH$_4$NO$_3$ particles with $D_{b,i}$=99 nm in H-TDMA modes 1 and 2 are compared to model calculations based on the dry solute mass equivalent diameter $D_{m,\text{NH}_4\text{NO}_3}=D_{\text{b,h&d, min}}$=89 nm obtained in mode 3 (Fig. 10).

The FP model calculations based on $a_w$ and $\rho$ from Tang (1996) and on $a_w$ from Clegg et al. (1998) and $\rho$ from Tang (1996) agreed fairly well with each other (diameter deviations $\leq$ 2%) and with the measurement data observed upon dehydration (diameter deviations $\leq$ 5%), respectively. The agreement reflects the consistency of our H-TDMA results with the single particle levitation results of Tang (1996) and of Chan et al. (1992). The latter were used in the semi-empirical ion-interaction model of Clegg et al. (1998).

The VA model calculations based on $\Phi_{\text{NH}_4\text{NO}_3}$ from Brechtel and Kreidenweis (2000) are in good agreement with the FP model results for RH $>$ 85%. At lower RH the calculated diameters were just slightly lower than our hydration measurement data but up to $\sim$ 10% lower than our dehydration measurement data and the FP model results. These findings indicate that the H-TDMA experiments from which Brechtel and Kreidenweis (2000) derived the coefficients $\beta_{0,1}$ and $Y_1$ for their semi-empirical parameterisation of $\Phi_{\text{NH}_4\text{NO}_3}$ may have been affected by similar volatilisation or restructuring effects as our hydration measurements.

VA model calculations based on $a_w$ from Clegg et al. (1998) confirm that the errors introduced by the assumption of volume additivity are small for dilute solutions and high relative humidities (RH $>$ 85%). For highly supersaturated droplets at RH $\approx$ 30%, however, the VA model diameters were $\sim$ 6% lower than the FP model which was based on the same water activity values but more realistic solution density values. On the other hand, VA model calculations based on the assumption of near-ideal solute properties with $\Phi_{\text{NH}_4\text{NO}_3}$=1 were up to 10% higher than the FP model calculations.

4.3 Pure bovine serum albumin particles

4.3.1 Hygroscopic growth and microstructure

The experimental results obtained for pure BSA particles with $D_{b,i}$=98 nm in H-TDMA modes 1 and 2 are illustrated in Fig. 11. No significant differences between the diameters measured upon hydration and dehydration were observed, and the hygroscopic growth was much less pronounced than for inorganic salts. $D_b$ was near constant at RH $< 30\%$
and exhibited a stepwise increase by \( \sim 3\% \) at \( RH=30-45\% \), which seems to indicate a sort of deliquescence transition, i.e. the transformation of the dry protein particle into a saturated aqueous solution or gel-like droplet. The further hygroscopic growth at \( RH>45\% \) was in good agreement with model calculations discussed below and led to a maximum increase of \( D_b \) by \( \sim 10\% \) at \( RH=95\% \). The mobility equivalent growth factors observed for BSA particles with \( D_{b,i}=100 \text{ nm} \) in H-TDMA mode 3 and the V A model based on osmotic pressure parameterisation: Kelvin term with \( \sigma=\sigma_w \), black solid; Kelvin term with \( \sigma=0 \), dashed green.

4.3.2 Model calculations

The Köhler theory calculations illustrated in Fig. 11 were performed with a V A model based on the osmotic pressure parameterisation of \( v_i \Phi_i \), which has been derived from the osmotic pressure virial equation by Carnahan and Starling (1969) and is illustrated in Fig. 2b.

At \( RH>45\% \), i.e. above the apparent deliquescence transition, the deviations between modeled and measured diameters were less than 1%. Proteins act as surfactants and reduce the surface tension of aqueous solutions, but we could not find a suitable parameterisation of \( \sigma \) for concentrated solutions of BSA. To test the effect of surfactant activity, the Kelvin term in Eq. (9) has been neglected in one set of model calculations. This corresponds to the assumption of \( \sigma=0 \) and led to a decrease of the calculated equilibrium \( RH \) values by about 2%, which seems to improve the agreement between modeled and measured diameters at high \( RH \). The differences are, however, smaller than the measurement uncertainty.

4.4 Mixed NaCl-BSA and NH₄NO₃-BSA particles

4.4.1 Hygroscopic growth of NaCl-BSA particles

The experimental results obtained for mixed NaCl-BSA particles with \( D_{b,i}=99 \text{ nm} \) in H-TDMA modes 1 and 2 are illustrated in Fig. 13.

Upon hydration of the particles with 10–75% BSA mass fraction in the dry solute mixture, \( x_{\text{BSA}} \), the measured mobility equivalent diameter exhibited a significant decrease as the relative humidity approached the deliquescence threshold, \( RH_d \). The most pronounced diameter reduction upon hydration was observed for the particles with 25% BSA (\( \varphi_{b,\text{hy, min}}=0.86 \), Table 3), indicating substantial microstructural rearrangements as will be discussed below. The deliquescence transitions were observed at similar relative humidities as for the pure NaCl particles, \( RH_d=(75 \pm 2)\% \); again the most pronounced deviation was observed for the particles with 25% BSA (\( RH_d=73\% \)). The relative mobility equivalent diameter increase observed upon deliquescence exhibited a near-linear decrease with increasing BSA mass fraction (\( \Delta r_d D_b \), Table 3). Upon hydration of the particles with 90% BSA no sharp deliquescence transition was observed. At 20–30% and 60–70% \( RH \) small stepwise increases of \( D_b \) by 3–5% were observed, followed by a steep increase at \( RH>80\% \). At 75–90% \( RH \) the diameters measured upon hydration were up to 5% lower than the ones measured upon dehydration, indicating a kinetic limitation of the hygroscopic growth of the deliquescent particles due to the high content of BSA which inhibits the uptake and release of water vapor as will be discussed below.
Fig. 13. Mobility equivalent diameters observed upon hydration (H-TDMA mode 1) and dehydration (H-TDMA mode 2) of mixed NaCl-BSA particles with $D_{b,i} = 99$ nm and BSA dry mass fractions of 10% (a), 25% (b), 50% (c), 75% (d), and 90% (e) compared to Köhler theory calculations with different VA models ($\Phi_{\text{NaCl}}$ from Mokbel et al., 1997; $\Phi_{\text{BSA}}$ from osmotic pressure parameterisation) and dry solute mass equivalent diameters: AS-VA, green; SS-VA, black; $D_{m,s} = D_{b,\text{hy},\text{min}}$, dotted (a, b); $D_{m,s} = D_{b,\text{de},\text{min}}$, dashed (c, d, e); $D_{m,s} = D_{m,\text{hy},\text{min}}$, solid (a, b); $D_{m,s} = D_{b,\text{h&d},\text{min}}$, solid (c).}

Upon dehydration of the particles with 10–75% BSA mass fraction, efflorescence transitions were observed at relative humidities which decreased with increasing $x_s$, BSA, from $\text{RH}_{e} = 41\%$ for $x_s$, BSA = 0 to $\text{RH}_{e} = 37\%$ for $x_s$, BSA = 75% (Table 3). Apparently the protein inhibited the nucleation of salt crystals, leading to higher stability of the supersaturated salt solution. The relative mobility equivalent diameter change upon efflorescence also decreased with increasing BSA mass fraction, from $-29\%$ for $x_s$, BSA = 0 to $-6\%$ for $x_s$, BSA = 75% ($\Delta r_{e} D_{b}$, Table 3). For particles with 90% BSA no pronounced efflorescence transition was observed. Instead, both the particles with 75% and with 90% BSA exhibited several small stepwise decreases of $D_{b}$ in the RH range of 35–70% and 10–90%, respectively (Fig. 13d and e). The results of
the hydration and dehydration experiments indicate a gel-like microstructure with embedded NaCl crystallites for the particles with high BSA content at medium RH, which is consistent with the TEM micrographs of deposited particles in Fig. 6 (B2 and B3) and will be discussed below.

Figure 14 shows the particle number size distributions measured at relative humidities close to the deliquescence threshold upon hydration of pure NaCl particles and mixed NaCl-BSA particles with 10% BSA mass fraction and \( D_{b,i} = 99 \) nm.

For the pure NaCl particles bimodal size distributions with a sharp stepwise transition from dry particles with \( D_{b,hy,min} \approx 98 \) nm to saturated aqueous solution droplets with \( D_{b,hy,max} \approx 176 \) nm were observed. Only at \( RH = 75.0\% \) a small particle mode was observed at an intermediate size of \( D_{b,hy} \approx 160 \) nm. The most plausible explanation for the observation of this intermediate mode is that it occurred exactly at the deliquescence threshold, and that most of the particles did not deliquesce immediately at the inlet of DMA 2 but only after having been exposed to the increased relative humidity inside DMA 2 (\( RH_3 > RH_2 \)) for a period on the order of one to a few seconds. Thus the electrostatic sizing of the particles had already proceeded to a significant extent before their diameter increased to that of a saturated salt solution droplet. As a consequence, the mobility equivalent diameter determined by the overall process of electrostatic particle sizing in DMA 2 (duration \( \sim 7.5 \) s) was a superposition of the diameters of the dry particle and of the deliquesced droplet. For pure NaCl intermediate particle modes were observed only in very few measurements at \( RH_d \) and \( RH_e \), and the obtained mobility equivalent diameters were close to the diameters of the fully deliquesced or effloresced particles, respectively (Fig. 3). This implies that the deliquescence and efflorescence transitions of pure NaCl particles in H-TDMA modes 1 and 2 generally occurred right at the entrance into the drift zone of DMA 2 and proceeded near-instantaneously, i.e. on time scale of one second or less.

In contrast to the pure NaCl particles, the mixed particles with 10% BSA mass fraction exhibited only monomodal size distributions with a gradual increase from particles with \( D_b \approx 91 \) nm to deliquesced droplets with \( D_b \approx 155 \) nm. The size distributions measured for particles with higher BSA content at \( RH_d \) and \( RH_e \) also exhibited intermediate modes in between the diameters of solid particles and deliquesced droplets, respectively (Fig. 13). These observations support that the deliquescence and efflorescence transitions of NaCl at \( RH_d \) and \( RH_e \), respectively, were kinetically limited by BSA and proceeded on a time scale of seconds. The fact that the inhibition occurred already at low mass and mole fractions of BSA (10% and 0.01%, respectively) suggests that it is a surface effect. Most probably a BSA coating limits the access of water vapor to the particle core composed of NaCl, which is consistent with the TEM micrographs of mixed NaCl-BSA particles shown in Figs. 6 (B1–B3) and discussed below.

4.4.2 Microstructural rearrangement and electric charge effects

The minimum mobility equivalent growth factors observed upon hydration and dehydration of the mixed NaCl-BSA particles (\( g_{b,hy,min} \), \( g_{b,de,min} \); Table 3) correspond to mobility equivalent diameter and volume reductions of up to 16% and 40%, respectively, which indicates highly irregular shape or high porosity of the initially selected particles and substantial microstructural rearrangement (compaction) upon interaction with water vapor.

Strong particle shrinking upon interaction with water vapor has been observed in earlier H-TDMA and microscopy...
Experiments with soot and NaCl high-temperature condensation aerosols, and it was attributed to the compaction of fractal agglomerate structures by capillary condensation effects (Weingartner et al., 1997; Mikhailov et al., 1997; Köllensperger et al., 1999; Krämer et al., 2000; Mikhailov et al., 2001). For fractal agglomerates, an enhancement of capillary restructuring is expected with increasing agglomerate size (Weingartner et al., 1997; Mikhailov et al., 1997).

Indeed NaCl-BSA particles with 50% BSA mass fraction and initial diameters of 99–201 nm exhibited a significant decrease of minimum mobility equivalent growth factors with increasing particle size ($g_{b,\text{hy, min}}$, $g_{b,\text{de, min}}$, $g_{b,\text{h&d, min}}$; Table 4). The TEM investigations showed that particles with $x_{s,\text{BSA}} \geq 50\%$ have a near-spherical envelope shape with a dendritic or fractal-like core of NaCl (Figs. 6, B2 and B3). Such dendritic or fractal-like structures are characteristic for diffusion limited growth processes (Feder, 1988). Apparently the BSA matrix inhibits the diffusion of NaCl in the efflorescent droplets and the formation of compact NaCl crystallites, which occurs upon efflorescence of droplets containing little or no BSA (Figs. A1, A2, B1).

Figure 15a illustrates the experimental results obtained for particles with 50% BSA and $D_{b,i}=99$ nm in HTDMA mode 3. Upon hydration & dehydration without droplet formation ($RH_2 < RH_d$) no significant size changes were observed up to $RH_2 \approx 30\%$. In the relative humidity range $30\% < RH_2 < RH_d$, the mobility equivalent growth factor exhibited a near-exponential decrease with $RH_2$, reaching a minimum value $g_{b,\text{h&d, min}}=0.83$ just below the deliquescence threshold. At $RH_d$ the growth factor increased from 0.83 to 0.88, i.e. a 6% increase of the dry particle mobility equivalent diameter occurred upon deliquescence in the conditioner tube and efflorescence in DMA 2. At $RH_2 < RH_d$ only small variations of $g_{b,\text{h&d, e}}$ were observed. Similar results were obtained for particles with $D_{b,i}=201$ nm (Fig. 15b). In this case the near-exponential decrease of the mobility equivalent growth factor started only at higher relative humidity ($RH_2 \approx 50\%$), was steeper, reached a lower minimum value ($g_{b,\text{h&d, min}}=0.81$), and exhibited a stronger increase at $RH_d$ (+10%).

The stepwise increase of mobility equivalent diameters and growth factors at $RH_d$ in the hydration & dehydration experiments (H-TDMA mode 3) with NaCl-BSA particles (6–10%; Fig. 15) is more pronounced but comparable to the analogous experiments with pure NaCl particles (3–5%; Fig. 5). Thus we suppose that this increase reflects a transformation of NaCl crystallites inside the mixed NaCl-BSA particles from irregular to near-cubic shape. The variations of $g_{b,\text{h&d}}$ at $RH_2 > RH_d$ are probably due to additional microstructural rearrangements of the NaCl crystallites and the BSA matrix. The differences observed between the particles with $D_{b,i}=99$ nm and $D_{b,i}=201$ nm are fully consistent with the kinetic limitation of the shape transformation of NaCl crystallites and with the fractal-like structure of the NaCl core of the particles discussed above.

Figure 13c shows that the mobility equivalent diameters of effloresced NaCl-BSA particles with 50% BSA mass fraction and $D_{b,i}=99$ nm were essentially the same in H-TDMA modes 2 and 3 ($D_{b,\text{de,e}} \approx D_{b,\text{h&d,e}} = 87$ nm). Apparently the NaCl crystallites in effloresced NaCl-BSA particles retained their near-cubic shape also in mode 2, which indicates that BSA inhibits the transformation of the crystallites from near-cubic to near-spherical shape. The higher stability of the near-cubic shape of small NaCl crystallites in mixed NaCl-BSA particles was confirmed by TEM micrographs. Figure 6 (B1) shows that 100 nm and smaller NaCl crystallites in particles generated from a NaCl-BSA solution with 25% BSA mass fraction exhibit sharper corners than those generated from a pure NaCl solution in Fig. 6 (A1).

The crystallites from the mixture appear to be covered by a BSA layer, which inhibits the transformation to near-spherical shape by interaction with water vapor (diffusion barrier). This is in agreement with the observation that BSA kinetically limits the deliquescence and efflorescence of NaCl in mixed particles as outlined above.

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**Table 4. Minimum mobility equivalent growth factors of NaCl-BSA and NH$_4$NO$_3$-BSA particles observed in H-TDMA operation modes 1–3 ($g_{b,\text{hy, min}}$, $g_{b,\text{de, min}}$, $g_{b,\text{h&d, min}}$) for different initial diameters and neutralisation modes (measurement precision ±1%).**

<table>
<thead>
<tr>
<th>Salt</th>
<th>BSA Dry Mass Fraction (%)</th>
<th>$D_{b,i}$ (nm)</th>
<th>$g_{b,\text{hy, min}}$</th>
<th>$g_{b,\text{de, min}}$</th>
<th>$g_{b,\text{h&amp;d, min}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NaCl</td>
<td>0</td>
<td>99</td>
<td>0.98</td>
<td>1.01</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>0</td>
<td>201</td>
<td>0.96</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>99</td>
<td>0.89</td>
<td>0.88</td>
<td>0.83</td>
</tr>
<tr>
<td></td>
<td>50*</td>
<td>99</td>
<td>0.91</td>
<td>0.90</td>
<td></td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>146</td>
<td>0.86</td>
<td>0.85</td>
<td></td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>201</td>
<td>0.86</td>
<td>0.83</td>
<td>0.81</td>
</tr>
<tr>
<td>NH$_4$NO$_3$</td>
<td>0</td>
<td>99</td>
<td>0.97</td>
<td>0.99</td>
<td>0.90</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>99</td>
<td>0.84</td>
<td>0.80</td>
<td></td>
</tr>
<tr>
<td></td>
<td>50*</td>
<td>99</td>
<td>0.92</td>
<td>0.87</td>
<td></td>
</tr>
</tbody>
</table>

* Neutralisation mode B
Obviously the transformation of NaCl crystallites from near-cubic to near-spherical shape (v.v.) and its kinetic limitation influence the microstructural rearrangements observed for mixed NaCl-BSA particles. These effects alone, however, are not sufficient to explain the differences between the mobility diameters of the initially selected particles and the effloresced particles, especially the large deviations observed for 25–75% BSA mass fraction ($D_{b,i} = 99$ nm (a) and $D_{b,i} = 201$ nm (b)) observed upon hydration & dehydration (H-TDMA mode 3, RH$_2$).

The most probable reason for the very different properties of the mixed NaCl-BSA particles upon size selection by DMA 1 after nebulisation and drying (efflorescence in SDD or DMA 1) and the particles analyzed by DMA 2 after conditioning (hydration and/or dehydration with or without deliquescence and efflorescence in the conditioner tube or DMA 2) are electric charge effects.

BSA and other albumins are characterised by a high content of amino acid residues with ionogenic functional groups (arginine, lysine, aspartic and glutamic acid, etc.; Brown, 1975; NCBI protein database, http://www.ncbi.nlm.nih.gov), and thus they carry a high number of elementary charges in aqueous solution. The actual number of positive and negative elementary charges and the resulting net charge of the molecule depend primarily on the pH and ionic strength of the solution. The isoelectric point, i.e. the pH value at which a protein has zero net charge, is 4.5–5.0 for BSA. Under neutral conditions (pH≈7), BSA molecules carry a negative net electric charge of about 10 elementary charges (Peters, 1985), depending on the abundance of salt ions in the solution.

Molecular interactions of globular proteins are usually described in terms of Derjaguin, Landau, Verwey, and Overbeek (DLVO) theory (Derjaguin, et al., 1987; Verwey, and Overbeek, 1948), which is based on the balancing of van der Waals attraction and electrostatic repulsion (coulomb forces). According to basic DLVO theory, electrostatic repulsion between protein molecules should decrease upon addition of salts because of charge neutralisation by cations, which has been confirmed in experiments with low salt concentrations and ion strengths. In solutions with high salt concentrations and ion strengths, however, repulsion was found to be enhanced (Paunov et al., 1996). This so-called non-DLVO behavior is characteristic for globular protein solutions, and can be attributed to hydration effects, i.e. to the repulsive interaction of hydration shells formed around salt ions adsorbed on the protein surface (Petsev et al., 2000). Moreover, repulsion can be enhanced by excess electric charges, i.e. when solution droplets and particles carry net charges due to uncompensated anions or cations. Mainelis et al. (2001) reported that aerosol particles composed of biological materials and generated by nebulisation of aqueous solutions or suspensions retained excess electric charges of the nebulised droplets upon drying. They found that bacterial cells and spores (Pseudomonas fluorescens, Bacillus subtilis var. niger) with a mean diameter 0.7 $\mu$m carried net electric charges of up to $10^4$ elementary charges or more, depending on the dispersion method. Moreover, Gu and Li (1998) have shown that the net charging of droplets generated by nebulisation of aqueous solutions is generally increased with increasing ionic strength. Thus the nebulised NaCl-BSA solution droplets may have carried high net electric charges, leading to enhanced electrostatic repulsion (Coulomb forces between the excess charges) and to a reduced packing density of protein molecules in the dried particles.

Fig. 15. Mobility equivalent growth factors of NaCl-BSA particles with 50% BSA dry mass fraction, $D_{b,i}$=99 nm (a) and $D_{b,i}$=201 nm (b) observed upon hydration & dehydration (H-TDMA mode 3, RH$_2$).
To test the influence of electric charge effects, some experiments have been performed in aerosol neutralisation mode B (Fig. 1), in which the aerosol flow from the nebuliser was passed through a neutraliser (10 mCi $^{85}$Kr) before particle drying in the SDD. For the particles with 50% BSA mass fraction and $D_{b,i}=99$ nm, the particle diameter decrease due to microstructural rearrangement upon hydration and dehydration in neutralisation mode B was significantly less pronounced than in neutralisation mode A, where a neutraliser was applied only after particle drying in the SDD ($g_{b,hy,min}=0.91 \text{ vs. } 0.89; g_{b,de,min}=0.90 \text{ vs. } 0.88; \text{Table 3}$).

A similar but more pronounced effect of neutralisation mode B was observed for mixed NH$_4$NO$_3$-BSA particles with 50% BSA dry mass fraction and $D_{b,i}=99$ nm. As illustrated in Fig. 16, the decrease of mobility equivalent diameters with increasing $RH$ observed in H-TDMA operation modes 1 and 3 was strongly reduced in neutralisation mode B relative to mode A ($g_{b,hy,min}=0.92 \text{ vs. } 0.84; g_{b,h&d,min}=0.87 \text{ vs. } 0.80; \text{Table 4}$).

In contrast, the results of test experiments performed with pure NH$_4$NO$_3$ particles and $D_{b,i}=99$ nm in neutralisation mode B (H-TDMA modes 1 and 3) were practically identical to the results obtained in neutralisation mode A which are displayed in Figs. 9, 10, and 11. These test experiments and the results obtained with pure BSA particles, which exhibited no restructuring upon interaction with water vapor (Fig. 12), confirm that the influence of charge effects was specific for protein-salt mixtures and did not significantly affect the experiments with pure solutes. The influence of mixed solute composition on the effect of excess charge neutralisation in mode B (stronger effect for NH$_4$NO$_3$-BSA than for NaCl-BSA) may be due to different ion-interactions or to different size distributions of the droplets generated by nebulisation and passed through the neutraliser.

Based on the experimental results and considerations outlined above, we propose the following hypotheses to explain the apparent microstructural differences between the particles selected by DMA 1 after nebulisation and drying (efflorescence in SDD or DMA 1) and the particles analyzed by DMA 2 after conditioning (hydration and/or dehydration with or without deliquescence and efflorescence in the conditioner tube or DMA 2):

1. The aqueous NaCl-BSA solution droplets generated by nebulisation carried excess electric charges which enhanced electrostatic repulsion between the protein molecules and led to the formation of porous agglomerates upon efflorescence of the solution droplets in the SDD or DMA 1.

2. The electric charging of aqueous solution droplets generated by nebulisation was strongly enhanced by the interaction of salt ions and proteins (adsorption), because no significant charge effects had been observed for pure NaCl and pure BSA particles.

3. The dried particles retained their porous agglomerate structure upon neutralisation and size selection by DMA 1.

4. Upon interaction with water vapor the agglomerate structure of the single-charged particles selected by DMA 1 was efficiently compacted by capillary condensation ($RH < RH_d$) or deliquescence and efflorescence ($RH < RH_g$), involving the transformation of NaCl crystallites between near-cubic and near-spherical shape.

5. The porosity or void fraction of the agglomerates and the corresponding extent of restructuring upon interaction with water vapor were determined by the chemical composition and electric charge of the nebulised solution droplets, as will be detailed below (Table 5).

4.4.3 Model calculations for NaCl-BSA particles

Köhler theory calculations for the hygroscopic growth of mixed NaCl-BSA particles have been performed using the AS- and SS-VA models outlined in Sects. 3.1.2.3 and 3.1.2.4 with $\Phi_{NaCl}$ and $\Phi_{BSA}$ from Eqs. (7), (24), (19), and (26), respectively. In Fig. 13 the model results obtained with different values of $x_{s,BSA}$ and $D_{m,s}$ are compared to the H-TDMA measurement data.

For the particles with 10 and 25% BSA mass fraction in the dry solute mixture (Figs. 14a and b), the AS- and SS-VA models agreed to within $\leq 2\%$ (AS\textgreater SS). The diameters

---

**Fig. 16.** Mobility equivalent diameters observed in H-TDMA modes 1 and 3 and neutralisation modes A and B for mixed NH$_4$NO$_3$-BSA particles with $D_{b,i}=99$ nm and 50% BSA dry mass fraction compared to Köhler theory calculations using the SS-VA model with different parameterisations and dry solute mass equivalent diameters: $\omega_w$ from Clegg et al. (1998), black; $\Phi_{NH_4NO_3}$ from Brechtel and Kreidenweis (2000), green; $D_{m,s}=D_{b,hy,min}$, dashed; $D_{m,s}=D_{b,h&d,min}$, solid.
calculated with the minimum diameter observed upon hydration $D_{m,s}=D_{b,hy,min}$ were $\sim5\%$ higher than the measurement data ($\sim15\%$ with $D_{m,s}=D_{b,i}$). Since the TEM investigations indicated near-cubic shape for the mixed NaCl-BSA particles, we calculated an envelope shape corrected diameter $D_{m,hy,min}$ by inserting $D_{b,hy,min}$ and the dynamic shape factor for cubic particles $\chi_{cube}=1.08$ in Eq. (29). The model results obtained with the SS-VA model and $D_{m,s}=D_{m,hy,min}$ were in good agreement with the measurement data.

At $x_{s,BSA}=50\%$ the results of the AS-VA model were $\sim5\%$ higher than those of the SS-VA model (Fig. 13c). The diameters calculated with the minimum diameter observed upon dehydration $D_{m,s}=D_{b,de,min}$ were $\sim10\%$ higher than the measurement data ($\sim25\%$ with $D_{m,s}=D_{b,i}$). The results obtained with the SS-VA model and the minimum diameter observed in operation mode 3 ($D_{m,s}=D_{b,h&d,min}$) were in fair agreement with the measurement data (differences $\leq5\%$).

For the particles with higher BSA mass fractions (Fig. 14d and e), similar agreement was achieved with the SS-VA model and the minimum diameter observed upon dehydration $D_{m,s}=D_{b,de,min}$. For $x_{s,BSA}=90\%$ and $RH > 90\%$ the model results practically coincide with the measurement data. At $70\%$–$90\%$ $RH$, however, the diameters measured upon hydration were significantly lower than the calculated diameters whereas the diameters measured upon dehydration were significantly higher. These findings confirm that the protein at high concentration inhibits the uptake and release of water vapor and leads to a kinetic limitation of hydration and dehydration on the time-scale of the H-TDMA experiments.

In any case, the correct determination of $D_{m,s}$ turned out to be critical for Köhler theory calculations of the hygroscopic growth of particles with complex composition and microstructure. Moreover, the SS-VA approach appears to be fairly well suited for the modeling of particles containing organic macromolecules, whereas the AS-VA approach usually applied for inorganic salt mixtures turned out to be less suitable.

Thus the SS-VA model was used to calculate dynamic shape factors and void fractions for the characterisation of different microstructural states of the non-deliquesced NaCl-BSA particles: after size selection in DMA 1 ($D_{b,i}$) and at the minimum diameters observed in the different H-TDMA modes of operation, i.e. after exposure to water vapor without deliquescence in modes 1 ($D_{b,hy,min}$) or 3 ($D_{b,h&d,min}$), or after efflorescence in mode 2 ($D_{b,de,min}$).

To minimise statistical errors, the droplet diameters measured in the relative humidity range of 75–94\% (89–94\% for $x_{s,BSA}=0.9$) were least-squares fitted with a third-order polynome. From the given interval and polynomial fit eight data pairs of relative humidity and droplet diameter ($RH$, $D_{b}=D_{m}$) were taken to calculate the corresponding values of $g_{m,s}$ through iterative solving of Eq. (9) with $\Phi_{NaCl}$ and $\Phi_{BSA}$ given by Eqs. (24), (7), (26), and (19), respectively.

The pairs of $D_{m}$ and $g_{m,s}$ obtained from this procedure were inserted in Eq. (2), and the arithmetic mean and standard deviation of the resulting $D_{m,s}$ values are listed in Table 5. $D_{m,s}$ and the mobility equivalent diameter corresponding to the investigated microstructural state of the non-deliquesced particle ($D_{b,i}$, $D_{b,hy,min}$, $D_{b,h&d,min}$, or $D_{b,de,min}$) were inserted in Eqs. (29) and (30) to obtain the corresponding dynamic shape factor $\chi$. Finally $\chi$ and an appropriate envelope shape factor $\kappa$ (1.08 for the near-cubic particles at $x_{s,BSA}\leq25\%$; 1.00 for the near-spherical particles at $x_{s,BSA}\geq25\%$) were inserted in Eqs. (31) and (32) to calculate the envelope void fraction $f$.

The maximum void fraction calculated for the initial particles size selected by DMA 1 was almost 50\% for the particles with $x_{s,BSA}=0.5$. The initial void fraction decreased towards lower and higher BSA mass fractions, which confirms that the formation of porous agglomerate structures was due to specific ion-protein interactions.

For the particles restructured by interaction with water vapor or deliquescence and efflorescence the calculated void fraction was mostly less than 5\%, which is at the edge of measurement and modeling precision, as outlined above and confirmed by the negative value of 5\% for effloresced

<table>
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<tr>
<th>BSA Dry Mass Fraction (%)</th>
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<th>Initial Particles</th>
<th>Restructured Particles</th>
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<tr>
<td></td>
<td></td>
<td>$\chi_i$</td>
<td>$f_i$ (%)</td>
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<tr>
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<td>50</td>
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<td>75</td>
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<tr>
<td>90</td>
<td>95.4±0.8</td>
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<td>11</td>
</tr>
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</table>

<sup>a</sup> $D_{b,hy,min}$; <sup>b</sup> $D_{b,de,min}$; <sup>c</sup> $D_{b,h&d,min}$

Table 5. Dynamic shape factor ($\chi$) and envelope void fraction ($f$) of NaCl-BSA particles with initial diameter $D_{b,i}$=99 nm based on dry mass equivalent diameters ($D_{m,s}$, mean ± standard deviation of 8 data points) derived from SS-VA model calculations.
4.4.4 Hygroscopic growth, restructuring, volatilisation, and model calculations for NH₄NO₃-BSA particles

The experimental results obtained for NH₄NO₃-BSA particles with \(D_{b,i}=99\) nm and \(x_r,\text{BSA}=0.5\%\) in H-TDMA modes 1 and 3 are illustrated in Fig. 16. As for pure NH₄NO₃ particles no pronounced deliquescence transition was observed upon hydration (H-TDMA mode 1). In neutralisation mode A the measured mobility equivalent diameters were near constant up to \(RH<30\%\), followed by a pronounced decrease to a minimum at \(RH=70–75\%\) (\(g_{b,\text{hy},\text{min},A}=0.84\)), and a subsequent steep increase. In neutralisation mode B similar effects were observed, but the diameter reduction started only at \(RH<30\%\) and was less pronounced (\(g_{b,\text{hy},\text{min},B}=0.92\)). In H-TDMA mode 3 the measured diameters were almost the same as in H-TDMA mode 1 up to \(RH<65\%\). In neutralisation mode A minimum diameters were observed at \(RH=70–75\%\) (\(g_{b,\text{h&d},\text{min},A}=0.80\)), and at \(RH=95\%\) the diameter increased to the same value which was observed as a minimum in H-TDMA mode 1. Again neutralisation mode B showed similar effects but a less pronounced minimum at higher relative humidity (\(g_{b,\text{h&d},\text{min},B}=0.87, RH<85\%\)).

In view of the results described and discussed above for mixed NaCl-BSA and NH₄NO₃ particles, the most plausible explanation for the NH₄NO₃-BSA results is:

1. Porous agglomerates are formed upon particle generation by nebulisation and drying due to ion-protein interactions and electric charge effects.

2. The diameter reductions upon interaction with water vapor is due to a combination of restructuring (compaction) of the porous agglomerates and volatilisation of NH₄NO₃: The 7–8% difference between the minimum diameters observed in neutralisation modes A and B (\(g_{b,\text{hy},\text{min},A}=g_{b,\text{hy},\text{min},B}\); \(g_{b,\text{h&d},\text{min},A}=g_{b,\text{h&d},\text{min},B}\)) can be attributed to different porosities of the initially selected particles due to different electric charge effects. The 5–6% difference between the minimum diameters observed in H-TDMA modes 1 and 3 (\(g_{b,\text{h&d},\text{min},A}=g_{b,\text{h&d},\text{min},B}\); \(g_{b,\text{hy},\text{min},A}=g_{b,\text{hy},\text{min},B}\)) appears to be largely due to volatilisation of NH₄NO₃, because the minimum diameter observed in mode 1 is essentially the same as the diameters observed in mode 3 at \(RH<95\%\) where volatilisation was found to be negligible for pure NH₄NO₃.

3. BSA apparently inhibits the volatilisation of NH₄NO₃, because no significant diameter reductions were observed at \(RH<30\%\) for mixed NH₄NO₃-BSA particles in contrast to pure NH₄NO₃ particles. Most probably the salt is embedded in a protein matrix, which limits the access of water vapor as found for the mixed NaCl-BSA particles. Moreover, the protein may influence both the chemical decomposition of the salt and the evaporation of the decomposition products (Cruz et al., 2000). In any case it can affect the atmospheric abundance and measurement of particulate ammonium nitrate (Bergin et al., 1997; Ten Brink et al., 1997; Moya et al., 2002).

The Köhler theory calculations illustrated by green lines in Fig. 16 have been performed using the SS-VA model with \(\Phi_{\text{BSA}}\) from Eqs. (19) and (26) and with \(\Phi_{\text{NH₄NO₃}}\) from Eq. (6) and Clegg et al. (1998), respectively. The diameters calculated with \(D_{m,s}=D_{b,\text{h&d},\text{min},A}\) were in fair agreement with the measurement values from neutralisation mode A at \(RH<90\%\) (deviations ≤5%). At lower \(RH\) and for \(D_{m,s}=D_{b,\text{hy},\text{min},A}\) the calculated diameters were 5–15% higher than the measurement data. The humidity dependence of the deviations between model and measurement data seems to reflect the humidity dependence of chemical decomposition. With \(\Phi_{\text{NH₄NO₃}}\) from Eq. (13) the diameters calculated with \(D_{m,s}=D_{b,\text{h&d},\text{min},A}\) were ~5% lower and with \(D_{m,s}=D_{b,\text{hy},\text{min},A}\) they were ~3% higher than the measurement values from neutralisation mode A at \(RH<90\%\). For the small mass equivalent growth factors at lower relative humidities the parameterisation by Brechtel and Kreidenweis (2000) is not applicable. Moreover, its derivation from H-TDMA experiments may have been affected by similar chemical decomposition or restructuring effects as observed in our experiments with pure NH₄NO₃ particles. Nevertheless, the fair agreement of modelling and measurement results at high \(RH\) confirms the suitability of the SS-VA modelling approach and the applicability of the parameterisation for \(\Phi_{\text{BSA}}\).

5 Summary and conclusions

In this study the H-TDMA technique and transmission electron microscopy have been used to investigate the hygroscopic growth and microstructural rearrangement of aerosol particles composed of the protein BSA and the inorganic salts NaCl and NH₄NO₃ upon interaction with water vapor. To characterise the hygroscopic growth, microstructural rearrangements, and phase transitions (deliquescence, efflorescence) of pure and mixed protein and salt particles, their mobility equivalent diameters were measured as a function of relative humidity (\(RH=0–95\%\)) in the two standard modes of H-TDMA operation, i.e. upon hydration (increasing \(RH\)) or dehydration (decreasing \(RH\)). In an additional third operation mode the size selected particles were conditioned at relative humidities of 0–95% but dried again upon particle
sizing in the second DMA. This mode comprises a full cycle of hydration & dehydration and provides complementary information about microstructural rearrangement processes or chemical decomposition and volatilisation of the investigated particles upon surface interaction with water vapor, droplet formation and evaporation.

The measurement results have been compared to Köhler theory calculations of hygroscopic particle growth using different types of models. In the applied full parameterisation (FP) models both the water activity and density of the aqueous solution were calculated with empirical or semi-empirical parameterisations. In the alternative volume additivity (VA) models only the water activity was calculated with parameterisations while the density of the mixture was assumed to be additively determined by the densities of the pure components (water, salt, protein).

For pure NaCl particles, a transformation from near-cubic or irregular to near-spherical shape was observed upon interaction with water vapor at relative humidities below the deliquescence threshold. The conversion was found to be kinetically limited on the second time-scale of the H-TDMA experiments and attributed to partial dissolution and recrystallisation of the salt surface. Deliquescence and efflorescence transitions and the hygroscopic growth of aqueous NaCl solution droplets were in good agreement with literature data and Köhler theory calculations.

Pure NH₄NO₃ particles exhibited no pronounced deliquescence or efflorescence transitions. Nevertheless, a hysteresis between hydration and dehydration was observed and attributed to decomposition and evaporation of NH₄NO₃ in highly supersaturated aqueous droplets. This process was negligible at very low and very high relative humidities. At RH=50–80%, however, it led to particle mobility diameter reductions of up to 10%. Köhler theory calculations taking these effects into account were in fair agreement with the hygroscopic growth observed at RH≥35% for NaCl-BSA and at RH≥90% for NH₄NO₃-BSA. The efflorescence threshold of NaCl-BSA particles decreased with increasing BSA dry mass fraction (up to 5% reduction of RHₑ), i.e. the protein inhibited the formation of salt crystals and enhanced the stability of supersaturated solution droplets.

The measurement and modeling results obtained for mixed protein-salt particles lead to the following general conclusions:

Depending on their origin and conditioning, aerosol particles containing inorganic salts and proteins or comparable organic macromolecules can have complex and highly porous microstructures, which are influenced by electric charge effects and interaction with water vapor. The proteins tend to be enriched at the particle surface and form an envelope which inhibits the access of water vapor to the particle core and leads to kinetic limitations of hygroscopic growth, phase transition, and microstructural rearrangement processes. Besides these surface and kinetic effects, proteins and comparable organic macromolecules may also influence the thermodynamic properties of the aqueous bulk solution (solubilities, vapor pressures, and chemical equilibria, e.g. for the decomposition and evaporation of NH₄NO₃).

These effects should be taken into account in the analysis of data from laboratory experiments and field measurements and in the modelling of aerosol processes involving particles with complex composition. They can strongly influence the outcome of experiments performed on multi-second time scales, and depending on ambient conditions they may also play a significant role in the atmosphere (deliquescence, efflorescence, droplet growth, and CCN activation). In fact, irregular hygroscopic growth curves with local minima and maxima similar to the ones observed in this study, have recently been reported by Gysel et al. (2004) from H-TDMA experiments with water-soluble organics extracted from real air particulate matter and with humic-like substances. Nevertheless, the hygroscopic growth of particles composed of inorganic salts and proteins or comparable organic substances at high relative humidities can be efficiently described with simple volume additivity models, provided that the correct dry solute mass equivalent diameter and composition are known. A simple parameterisation of the osmotic coefficient has been derived from the osmotic pressure virial equation by Carnahan and Starling (1969) and appears to be well-suited for proteins and comparable substances. It is fully compatible with traditional volume additivity models for salt mixtures, and for its application only the density and molar mass of the substance have to be known or estimated.

First results from ongoing investigations with additional chemical components like ammonium sulfate and humic-like substances confirm the above conclusions. We consider the observed effects (microstructural rearrangements, kinetic limitations, electric charge effects) and their mechanistic understanding highly relevant for the interpretation and analysis.
of laboratory and field measurement data of aerosol particles interacting with water vapor – especially but not only for H-
TDMA experiments. Moreover, we think that the presented Köhler theory calculations provide a basis for efficient model-
ing of the influence of macromolecular organics on the hy-
groscopic growth and CCN activation of atmospheric parti-
cles.

6 Notation

Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tr>
<td>( a_w )</td>
<td>water activity</td>
</tr>
<tr>
<td>( A_\Phi )</td>
<td>Debye-Hückel coefficient</td>
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<td>( b_{\text{pit}} )</td>
<td>ion-interaction parameter</td>
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<tr>
<td>( c )</td>
<td>polynomial coefficient (water activity)</td>
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<td>( C(D) )</td>
<td>slip correction (Cunningham factor)</td>
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<td>( C_\Phi )</td>
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<td>( S_w )</td>
<td>water vapor saturation ratio</td>
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<tr>
<td>( s )</td>
<td>solute (dissolved substance, consisting of one or more chemical compounds)</td>
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<td>( \sigma_g )</td>
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Additional subscripts

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<th>Subscript</th>
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<td>( b )</td>
<td>mobility equivalent</td>
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<td>mass equivalent</td>
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References

Allen, M. D. and Raabe, O. G.: Slip correction measurements of spherical solid aerosol particles in an improved Millikan appar-
Andreae, M. O., and Crutzen, P. J.: Atmospheric aerosols: bio-
Andrews, E., and Larson, S. M.: Effect of surfactant layers on the size changes of aerosol particles as a function of relative humid-
Atkins, P. W.: Physical Chemistry, Oxford University Press, Ox-
ford, 1982.
Austin, J., Shindell, D., Beagley, S., Brühl, C., Dameris, M.,
Manzini, E., Nagashima, T., Newman, P., Pawson, S., Pitari,
G., Rozanov, E., Schnadt, C. and Shepherd, T.: Uncertainties and assessments of chemistry-climate models of the stratosphere,
Baker, M. B.: Cloud microphysics and climate, Science, 276, 1072–
1078, 1997.
M.: Evaporation of ammonium nitrate aerosol in a heated neph-
Brown, J. R.: Structure of Bovine serum albumin, Fed. Proc., 34,
Brechtl, F. J., and Kreidenweis, S. M.: Predicting particle supersat-
uration from hygroscopic growth measurements in the Humidi-
Brockmann, J. E., and Rader, D. J.: APS response to nonspheri-


Hanel, G.: The properties of atmospheric aerosol particles as functions of the relative humidity at thermodynamic equilibrium with the surrounding moist air, Rev. Geophys., 17, 73–188, 1976.


Zhang, Q. and Anastasio, C.: Free and combined amino compounds in atmospheric fine particles (PM2.5) and fog waters from Northern California, Atmos. Environ., 37, 2247–2258, 2003.