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Ionospheric Erosion by Alfvén waves

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Abstract: Using observations from the FAST small explorer spacecraft we present fields and plasma observations above the dayside auroral oval showing the erosion of ionospheric plasmas from the topside ionosphere by the action of Alfvén waves. Using interferometric techniques the waves are shown to approximately obey the expected dispersion for Alfvén waves with transverse scales extending from greater than electron inertial lengths down to ion gyro-radii. Measurements of the plasma density where these waves are observed show that over latitudinal widths exceeding 100 km total depletion of the cold ionospheric plasma can occur. The plasma within these depleted regions or cavities is composed of magnetosheath ion and electron distributions and upgoing transversely accelerated ions and downgoing field-aligned electrons distributed as conics and field-aligned beams respectively. Poynting flux observations on the density gradients comprising the cavity walls show that these waves are directed downwards and focused inwards towards regions of lower density. The wave phase velocity measurement in the plasma frame, while subject to significant uncertainty, is directed transversely outwards from the cavity. These observations suggest a feedback model for Alfvén wave focusing and ion heating on density gradients that can lead to intense ion outflow from the ionosphere and subsequent depletion of ionospheric plasmas.

1. Introduction

Low altitude polar orbiting satellites commonly observe low frequency electromagnetic fluctuations above the auroral oval (Louarn et al., 1994; Stasiewicz et al., 2000a). Several studies have shown that these fluctuations are oblique Alfvén waves with perpendicular structuring extending over a range of scales including the electron inertial length and in some cases the ion gyro-radii (Wahlund et al., 1998; Stasiewicz et al., 2000b; Chaston et al., 2004). The plasma environment in which these waves are observed is usually characterized at altitudes below 1 Earth radii by plasma density gradients, field-aligned accelerated electrons and transversely accelerated ions (Wahlund et al., 1994; Stasiewicz et al., 1997; Knudsen and Wahlund, 1998; Andersson et al., 2002). Several studies have shown how a spectrum of dispersive Alfvén waves can produce the observed field-aligned electron distributions (Kletzing, 1994; Thompson and Lysak, 1996; Chaston et al., 2004) and provide ion acceleration if scales of the order of the ion gyro-radii are present (Stasiewicz et al. 2000c; Chaston et al., 2004). However, there has been comparatively little attention given to the importance of strongly localized
transverse plasma density gradients above the auroral oval on Alfvén wave propagation with the exception of publications by Genot et al. (1999, 2004) and Seyler et al. (1995). This is a significant omission since often the most intense fields fluctuations are observed to be localized in field-aligned density cavities (Stasiewicz et al., 1998).

At altitudes as low as ~1000 km it has been demonstrated that the cavities in which Alfvén waves are imbedded are depleted, and in some cases devoid, of cold ionospheric plasmas with dn/n~1 (Chaston et al., 2000). Since the ionosphere is the dominant source of plasma at altitudes at least below 1 RE there must be some means by which this plasma is transported either vertically or radially to provide the cavitation. There have been a number of studies addressing the formation of density cavities by Alfvén waves in the auroral plasma based on various interpretations of the ponderomotive force associated with these waves. Li and Temerin (1993) showed through test particle simulations how plasma could be extracted from the auroral ionosphere due to the ponderomotive force associated with the gradient in altitude of the perpendicular wave electric field amplitude. The time scales for this mechanism are however of the order of minutes and perhaps to slow to account for a discrete density cavity formation. Bellan and Stasiewicz (1998) suggest that density cavitation in Alfvén waves may occur through a parallel ponderomotive force associated with the oscillating field aligned current in the wave. However, a comparison of cavity depth with the predicted depth for observed field-aligned current amplitudes indicated that this model was unable to yield sufficiently deep cavities (Chaston et al., 2000). Shukla and Stenflo (1999a) suggested that the parallel ponderomotive force balancing the thermal force due to Joule heating in the Alfvén wave field in the ionosphere may be sufficient to account from the depletions observed. This was supported by observations of the cavity depth and calculation of the joule heating expected for observed wave amplitudes. However given the almost collisionless nature of plasmas in the upper reaches of the ionosphere where these cavities are often observed this mechanism is questionable. Alternatively, Rankin et al. (1999) have suggested that density perturbations due to the ponderomotive force associated with the non-linear saturation of field line resonances above the aurora may be the source of density cavities observed. These density perturbations take the form of a driven ion acoustic wave or slow mode Alfvén wave which follow naturally from the coupling between the shear and slow mode Alfvén wave (or ion acoustic wave) in the presence of perpendicular gradients in the plasma pressure. This process has been demonstrated to produce density depletions of sufficient depth and width to account for observations from FAST and other auroral satellites.

The observations presented in this report however suggest a different mechanism for the formation of Alfvénic density cavities above the auroral ionosphere not dependent on the ponderomotive force but similar to those processes thought to responsible for the formation of what have become known as ‘lower hybrid cavities’ (Shuck et al., 2003). We begin in section 2 by presenting an overview of observations from the FAST satellite from a traversal above the dayside auroral oval where ionospheric density cavitation and electromagnetic waves are observed. In section 3 we employ interferometric techniques to identify these electromagnetic fluctuations as dispersive Alfvén wave turbulence extending over scales including the electron inertial length $\lambda_e$ and the energetic oxygen
gyro-radii $\rho_{O^+}$. Then in section 4 we explore the plasma processes occurring within an Alfvénic density cavity in more detail and employ measurements of the wave Poynting flux and interferometric techniques to demonstrate that the incoming Alfvén waves from the magnetosphere become focused on the cavity and are refracted by the cavity walls to produce perpendicular field structures on small transverse scales. In section 5 we present a schematic model based on the observations and compare the observations to simulation results and observations made of lower hybrid density cavities before concluding with a brief summary of the most important observational results.

2. Observations of Plasma Cavitation and Electromagnetic Waves

Figure 1 shows observations from the FAST satellite as it passed through a region of magnetosheath precipitation above the dayside auroral oval at an altitude of ~1700 km before entering the polar cap. The magnetosheath ion population can be seen in the first panel at energies above ~200 eV. At energies below 100eV a second ion population can be identified. The mass spectrometer data shows that these ions are primarily O$^+$ suggesting that they are of ionospheric origin. Figure 1 panel b shows that these ionospheric ions are observed transverse to the geomagnetic field at pitch angles slightly larger than 270 degrees showing that they have been locally accelerated transverse to $B_0$. Integration of these data, as shown in panel c, indicates that these ions are out-flowing from the ionosphere at a rate of up to $10^9$ ions cm$^{-2}$/s. A simple calculation shows that without replenishment the observed rate of ion outflow would lead to total depletion of the ionosphere on these fieldlines in ~60 minutes.

Similar plasma sources can account for the observed electron populations. Precipitating magnetosheath electrons can be identified in panel d by the peak in energy flux observed at ~200eV. Partly obscuring this peak, particularly after 06:44:47 UT, we can identify supra-thermal electron bursts (Johnstone and Winningham, 1982). Panel e shows that these bursts are largely field-aligned and downgoing (180$^\circ$). Since the energies of these bursts extend upwards from the lowest measured (5eV) it is speculated that at large fraction of these fluxes are accelerated ionospheric electrons.

These enhanced ion and electron fluxes are observed coincident with fluctuations in the electric and magnetic field measurements. Panel f shows the electric field measured in the spacecraft spin plane, perpendicular to the geomagnetic field, and pointing roughly northwards along the spacecraft trajectory ($E_\perp$ north or $E_x$). The observed field deviations are impulsive and disordered with no clear periodicity or scaling. Indeed Figure 1, panel g shows that over this interval the wave power falls monotonically with increasing frequency from 0 up to the 16 kHz Nyquist with no structuring in the vicinity of the proton or Oxygen gyro-frequencies. A similarly featureless spectrum can be found in the spectra of the magnetic field time series ($B_\perp$ east or $B_y$) shown in panel h. These data are measured perpendicular to the geomagnetic field and in the eastwards direction orthogonal to $E_x$. This measurement has been performed using both fluxgate and search coil magnetometers shown here by the black trace representing measurements from the fluxgate magnetometer alone and red traces showing a composite magnetic field
measurement from both the fluxgate and search coil magnetometers. For the operating mode of the spacecraft at this time the response of the fluxgate magnetometer falls off steeply above ~0.5 Hz above which the search coil magnetometer provides more reliable amplitude measurements. For this reason we have superimposed the search coil measurements on the fluxgate measurement to provide a more continuous representation of fluctuations in $B_A$ with increasing frequency. The lowest frequency variations in this time series correspond to large scale field-aligned currents through Ampere’s Law. It has been demonstrated previously (Ijima and Potemra, 1978; Peria et al., 2000) that these are distributed as sheets highly elongated in the east-west direction. Under this assumed current geometry positive and negative gradients in Figure 1 h indicate downward and upward current sheets respectively. Such features are typical of the cusp. These currents can be expected to close through Pedersen currents in the ionosphere which provides us with the expression for the perturbation fields due to the currents as $E_x/B_y=1/(\mu_0 \Sigma_p)$ (Sugiura, 1984) where $\Sigma_p$ is the height integrated Pedersen conductivity. At smaller spatial and temporal scales, however the field-aligned current may close locally via polarization currents as an Alfvén wave which at FAST altitudes provides $E_x/B_y = V_A(1+k_x^2 \lambda_e^2)^{1/2}$ (Goertz and Boswell, 1979) where $k_x$ is the perpendicular wave number, $\lambda_e=c/\omega_p$ is the electron inertial length and $\omega_p$ is the electron plasma frequency. Since $V_A$ and $\lambda_e$ are density dependent to determine the nature of the electromagnetic fluctuations observed based on $E_x/B_y$ requires a measurement of the density.

The observed field fluctuations are co-located with rapid variations in the current measured by the Langmuir probe ($I_{LP}$) and shown in panel i) by the black trace. The red trace in this panel is the current to the Langmuir probe from the field aligned motion of electrons as measured by the electrostatic analyzer experiment ($I_{ESA}$). This current has been evaluated by subtracting fluxes from the ESA measurements at energies below the spacecraft potential (which can be up to 20 V positive at this time), calculating the required moments and multiplying by the cross-sectional area of the Langmuir probe. From Figure 1 (i) it can be seen that $I_{ESA}$ forms a lower bound for $I_{LP}$. This leads us to write $I_{LP}=I_{thermal}+I_{ESA}$ where $I_{thermal}$ is the contribution to $I_{LP}$ from the thermal plasma current. When $I_{LP}=I_{ESA}$ the dominant current to the probe is that due to field-aligned electrons. Since the Langmuir probe is biased 15 V positive with respect to the satellite this indicates that at these times the total current is carried by electrons with energies of at least 15 eV. Consequently, it can be concluded that when $I_{LP}=I_{ESA}$ the measured plasma at these times is devoid of the usually dominant ambient ionospheric component (which usually provides the thermal plasma current to the LP) and the total plasma density is given by the moment of the ESA observations taken at energies above the spacecraft potential.

Outside those regions where $I_{LP}$ is depressed we observe plasma emissions allowing us to calibrate $I_{LP}$ to give the density of the thermal plasma. This has been determined statistically using this event and other similar events at approximately the same altitude to be $n_{thermal}=(0.2\pm0.1) I_{thermal}$ for sphere 6 on FAST when operated in current mode (under the assumption that the cold ionospheric or thermal plasma temperature is roughly the same throughout). To obtain density measurements where the current to the probe is a mixture of the thermal current due to the ambient ionospheric plasma and that due to field
aligned electrons the density is given by subtracting $I_{\text{ESA}}$ from the $I_{\text{TP}}$ to give $I_{\text{thermal}}$ and then using the above calibration to give the thermal plasma density. The total density is then given by adding the thermal plasma density to that measured by the ESA above the spacecraft potential. The net result for total density in this case is shown in Figure 2. This result shows sections over horizontal widths of $>100$ of km (based on a spacecraft speed of $\sim 7$ km/s) where the cold or thermal ionospheric plasma has been completely removed and replaced by significantly smaller densities of energetic electrons (red) (which are field-aligned). Significantly, it is in those regions where the cold ionospheric plasma has been depleted that the largest oscillations in the field quantities are observed.

3. Cross Spectral Measurements and Alfvénic Turbulence

With a reliable measurement of density in hand we now require a measurement of the wavevector to identify the electromagnetic fluctuations based on $E_x/B_y$. To achieve this we employ interferometric techniques to determine an average value for $k$ in the spin plane ($k_{\text{sp}}$). This approach is similar to that exploited Wahlund et al. (1998) and Stasiewicz et al. (2000b) using Freja measurements with the exception that we employ a wavelet based approach and obtain a 2-D measurement of the wavevector. In this approach the wave vector is determined by measuring the phase difference between electric field measurements in the spin plane at multiple points separated by a known distance in this plane (Labelle and Kintner, 1989). The FAST satellite provides several such baselines allowing interferometric measurements such as these to be performed. The configuration of the FAST fields instrument is shown in Figure 3. We use the measured electric fields given by the potential difference between spheres 5 and 8, 7 and 8, 1 and 2, and 1 and 4. This provides two orthogonal baselines for relative phase determination in the spacecraft spin plane with $x_{58-78}=25.5$ m and $x_{12-14}=12$ m respectively. We now make the assumption that there is a single wave vector ($k_{\text{sp}}$) for each wave frequency in the spacecraft frame ($\omega_{\text{sp}}$). Under this assumption if $\phi_{58-78}(\omega_{\text{sp}})$ and $\phi_{12-14}(\omega_{\text{sp}})$ are the phase differences measured along each baseline then $k_{\text{sp}}(\omega_{\text{sp}})$ projected along each baseline is given by

$$k_{\text{sp}}(\omega_{\text{sp}}) = \frac{\phi_{58-78}(\omega_{\text{sp}})}{x_{58-78}}$$

and

$$k_{12-14}(\omega_{\text{sp}}) = \frac{\phi_{12-14}(\omega_{\text{sp}})}{x_{12-14}}.$$ 

Since $k_{58-78}(\omega_{\text{sp}})=k_{\text{sp}}(\omega_{\text{sp}}) \cdot x_{58-78}/x_{58-78}$ and $k_{12-14}(\omega_{\text{sp}})=k_{\text{sp}}(\omega_{\text{sp}}) \cdot x_{12-14}/x_{12-14}$ then the angle between $k_{\text{sp}}$ and the $x_{12-14}$ baseline is,

$$\theta_{12-14}(\omega_{\text{sp}}) = \tan^{-1}\left(\frac{\phi_{58-78}(\omega_{\text{sp}})}{\phi_{12-14}(\omega_{\text{sp}})} \cdot x_{12-14}/x_{58-78}\right).$$

Since the baseline orientation relative to $B_o$ is known from fluxgate magnetometer measurements it is then straightforward to find the orientation of $k_{\text{sp}}$ to $B_o$ and hence $k_{\text{sp}}$.

Figure 4a shows the wavelet transform of the electric field measurements from spheres 1 and 2 over the interval from 06:44:14 UT to 06:44:27 UT. The black trace in this panel represents the plasma density which has been scaled to fit in this panel. Comparing the wave spectra and the density measurement indicates that the wave power is enhanced in density cavities. Panel b shows the phase difference ($\phi_{12-14}$) for the $x_{12-14}$ baseline with the coherence for this baseline shown in panel c. The same is shown for the $x_{58-78}$ baseline in panel d however we have omitted the coherence measurement in this case because it is almost identical to that shown in panel c. The periodic variation of phase shown in panel
b and c is due to the spacecraft rotation and the relative orientation of k and the dipole in the spin plane. Since \( \phi_{12-14} = x_{12-14} \cdot \mathbf{k}_{sp} \) or \( \phi_{58-78} = x_{58-78} \cdot \mathbf{k}_{sp} \) and the rest frame wave frequency is given by \( \omega = \omega_{sp} \mathbf{k}_{sp} \cdot \mathbf{v}_{sp} \), then the variation of the measured phase with spacecraft rotation is,

\[
\phi_{12-14} = x_{12-14} \left( (\omega_{sp} - \omega)/(v_{sp} \cos \theta_{sp}) \right) \cos \theta_{12-14} \tag{2}
\]

And,

\[
\phi_{58-78} = x_{58-78} \left( (\omega_{sp} - \omega)/(v_{sp} \cos \theta_{sp}) \right) \cos \theta_{58-78} \tag{3}
\]

where \( \theta_{sp} \) is the angle between \( \mathbf{k}_{sp} \) and the spacecraft velocity vector. Clearly for a fixed phase, \( \omega_{sp} \) is smallest when \( \theta_{12-14} \) or \( \theta_{58-78} \) are 0 or \( \pi \) and goes to infinity when \( \theta_{12-14} \) or \( \theta_{58-78} \) become \( \pi/2 \) or \( 3\pi/2 \). This pattern is represented in panels b and d by the U-shaped variations in phase with singularities at half the satellite spin period. At these singularities for a given \( \phi \), the spacecraft frame frequency \( \omega_{sp} \rightarrow \infty \), indicating that \( \mathbf{k}_{sp} \) and \( \mathbf{x} \) at this spin phase are orthogonal. Comparing the form of panel b with the angle between \( x_{12-14} \) and \( \mathbf{B}_0 \) in the spin plane shown in panel e suggests that \( \mathbf{k}_{sp} \) is very nearly perpendicular to the geomagnetic field and parallel/anti-parallel to \( \mathbf{v}_{sp} \).

In general Panels b and d of Figure 4 show that with increasing frequency, in the spacecraft frame, the magnitude of the phase difference between each dipole pair increases towards \( |\pi| \) radians and then decreases. This change in the sign of the slope of phase with frequency occurs where the longest electric field dipole for each baseline matches half the wavelength projected along the dipole leading to an antenna null. The measured phase difference where this occurs is given by \( \phi_{12-14} = \pm \pi (1 - x_{12}/x_{14}) = \pm 0.8 \pi \) and \( \phi_{58-78} = \pm \pi (1 - x_{58}/x_{78}) = \pm 0.9 \pi \). Once these phase differences have been exceeded the measured phase needs to be corrected to give the actual phase as,

\[
\tilde{\phi}_{12-14} = \phi_{12-14} \quad \text{if } |\phi_{12-14}| \leq 0.8 \pi \tag{4}
\]

\[
\tilde{\phi}_{12-14} = 2 \cdot \text{Sign}(\phi_{12-14}) \cdot 0.8 \pi - \phi_{12-14} \quad \text{if } |\phi_{12-14}| > 0.8 \pi
\]

and,

\[
\tilde{\phi}_{58-78} = \phi_{58-78} \quad \text{if } |\phi_{58-78}| \leq 0.9 \pi \tag{5}
\]

\[
\tilde{\phi}_{58-78} = 2 \cdot \text{Sign}(\phi_{58-78}) \cdot 0.9 \pi - \phi_{58-78} \quad \text{if } |\phi_{58-78}| > 0.9 \pi
\]

Further nulls can be expected as the wavelengths approach the dimensions of the other electric field dipoles however these are beyond the frequency range where high coherence is obtained and do not effect the results reported here.

If we momentarily assume that the transverse phase velocity of the observed fluctuations is much less than the spacecraft speed (i.e. that the observed phase structuring is due largely to Doppler shift) then \( \omega = \mathbf{k}_{sp} \cdot \mathbf{v}_{sp} \) and we can predict the variation of the phase nulls with frequency in the spacecraft frame (Temerin, 1979). From previously we found that roughly \( \mathbf{k}_{sp} \parallel \mathbf{v}_{sp} \) In this case the Equation 2 and Equation 3 can be rearranged to give the variation of spacecraft frame frequency with phase as,

\[
f_{12-14} = \frac{v_{sp}}{2\pi} \sqrt{\left( \frac{\phi_{12-14}}{2\pi} \cdot x_{12-14} \cos \theta_{12-14} \right)} \tag{6}
\]

And,
Substituting the angle for the nulls into these expressions gives the curves shown in panels b and d of Figure 4. The close agreement with the variation of the frequency and phase shown by these curves and the frequency of the observed nulls indicates that the assumptions of transverse wave phase speeds less than the spacecraft speed and of $k_{sp}$ largely perpendicular to $B_o$ (and so also parallel/antiparallel to $v_{sp}$) are reasonable and can be used as a simple check on the more complete analysis where these assumptions are removed.

The results from the complete interferometric analysis using Equation 1 are shown in Figure 5. These results represent an average taken over the entire interval contained in Figure 1. In obtaining these results we have excluded those measurements with two-point coherency less than 0.7 and those intervals where either one of the baseline are within 10° of the projection of the geomagnetic field into the spin plane. We have also excluded those transforms with rapidly or erratically varying phase with frequency. These exclusions significantly reduce the temporal resolution of the measurements made but provide a more reliable average result. The error bars shown throughout this Figure 5 represent one standard deviation in the averaged results. These are of course symmetric about the averaged value but with some exceptions are generally plotted in one direction only due to the logarithmic scaling.

Figure 5 a shows the variation of $k_{sp}$ with spacecraft frame frequency. The red line shows the expected result for field structures which are stationary in the plasma frame and provide the observed spacecraft frame frequency purely through spacecraft Doppler shift. Up to about 200 Hz the Doppler-shift yields a reasonable approximation of the wavenumbers and is well within one standard deviation of the averaged value as shown by the error bars. Panel b of Figure 5 shows the angle between $k_{sp}$ and the projection of the geomagnetic field ($B_o$) into the spin plane ($B_{sp}$). For the interval considered $B_o$ and $B_{sp}$ are separated by ~5°. Over the frequency range plotted we find angles ranging between 80° and 85°. These angles represent a lower limit of the actual angle between $k$ and $B_o$, since it is probable that a component of $k$ exists perpendicular to the spacecraft spin plane. Due to the inclination of the spin plane relative to $B_o$, the presence of this unmeasured component means that the magnitude of $k$ along $B_{sp}$ will be over estimated and hence the angle of $k$ to $B_o$ underestimated. Nonetheless, in the measurements presented in this panel it should be noted that the averaged values are everywhere within one standard deviation of being exactly perpendicular and so $\theta_{sp} \rightarrow 0°$.

Panel c of Figure 5 shows the wave frequency in the plasma frame. This has been obtained by subtracting the spacecraft Doppler shift from the observed spacecraft frame wave frequency. In performing this calculation we have included the contribution from the poleward plasma convection of ~1 kms$^{-1}$ estimated by integrating the measurements from the ion spectrometer experiment. Since the Doppler shift and the spacecraft frame frequency over most of the observed frequency range have very similar magnitudes the errors in the wave frequency are large. Because of this the averaged wave frequencies
shown here represent an upper limit for \( \omega_{sp} \) with the magnitude of the error bars indicating that within 1 standard deviation of the average values we find a wave frequency of 0 Hz. The blue and green horizontal lines in this panel show the value of the local Oxygen (\( f_{O+} \)) and Hydrogen cyclotron frequencies (\( f_{H+} \)) respectively. From these observations it can confidently be said that \( \omega_{sp} \) in the plasma frame is less than \( \Omega_{O+} \) for spacecraft frame frequencies at least below 100 Hz in the spacecraft frame. Panel d of Figure 5 shows the wave phase speed \( \omega_{sp}/k_{sp} \). As with the wave frequency measurement the errors in evaluating this quantity are substantial. However, a time domain cross-correlation analysis to be discussed in the next section also yields phase speeds similar to these values.

The identification of the field fluctuations as turbulence requires scale invariance in the observed wave power spectra. Figure 5 e shows the k-spectra of the observations in the spin plane. The red-line represents a \( k_{sp}^{-1.7} \) the power law spectra fitted to the observations over the first decade on the k-scale. This is the expected dependency for Komolgorov fluid turbulence. Beyond this range the wave power falls ever more rapidly with increasing \( k_{sp} \). The red dashed vertical line in this plot shows the wave number corresponding to the electron inertial length (\( 2\pi/\lambda_e=2\pi/145 \text{ m}^{-1} \)). Clearly there are scales present in the observed field fluctuations that extend downwards to include this length. Interesting it is at wavenumbers a few times smaller than \( 2\pi/\lambda_e \) that the observed k-spectra begins to deviate from the Komolgorov like power-law. In the local approximation, and for the parameters present and this altitude, the wave dispersion for an electromagnetic wave at frequencies below \( \Omega_{O+} \) and at small transverse scales can be described by \( \omega/k_{||}=V_A(1+k_{\perp}\lambda_e^2)^{-1/2} \) (Goertz and Boswell, 1979). This wave carries a parallel electric field given by \( E_{||}/E_{\perp}=k_{\perp}k_{||}\lambda_e^2/(1+k_{\perp}\lambda_e^2) \). Consequently when \( k_{\perp}\lambda_e\rightarrow1 \) the wave becomes dispersive and may dissipate through electron Landau damping to provide the observed deviation from the power law spectra for \( k_{\perp}\lambda_e\geq1 \).

The other dashed vertical lines in this panel represent the Oxygen and Hydrogen gyro-radii (\( 2\pi/p_{O+}=2\pi/60 \) - green line and \( 2\pi/p_{H+}=2\pi/20 \) - orange line) of the energetic ionospheric plasma. These are measured by the FAST mass spectrometer calculated over the energy range from 5 to 100 eV for the backward looking hemisphere of the instrument to avoid the influence of magnetosheath ions and the effects of spacecraft ram respectively. The energies from this measurement averaged over the interval shown in Figure 1 are \( \sim10 \text{ eV} \) and \( 18 \text{ eV} \) respectively. These energies do not represent the temperature of the bulk ionosphere but rather the average energy of the tail of the ionospheric distribution at energies above 5eV. It is shown in Figure 2 panel a that the density of this energetic portion of the ion distribution can be as large as few \( 100 \text{ cm}^{-3} \) within regions of depleted density. The observed wavenumbers shown indicate wave scales extending down to and including the energetic oxygen gyro-radius but with wave power falling sharply at smaller scales and failing to reach the energetic proton gyro-radius. It has been shown previously that at wave scales approaching ion gyro-radius electromagnetic waves in this frequency range may strongly energize ions and thereby dissipate (Chen et al., 2001). Dissipation by this means may account for the increasing rate of decline in \( E_{sp}^2(k_{sp}) \) for \( k_{\perp}p_{O+}\geq1 \). These observations are consistent with that
expected for turbulence with power-law like k-spectra containing inertial and dissipative ranges.

To establish that we are observing specifically Alfvénic turbulence we compare the wave impedance with the expected dispersion for small-scale Alfvén waves in the observed plasma environment. It is well known in the local approximation that this is given by

$$\frac{E_x}{B_y} = V_A \sqrt{\left( I + k_x^2 \lambda_e^2 \right) \left( I + k_x^2 \rho_i^2 \right) \left( \frac{I}{\Omega_i^2} - \frac{\omega^2}{\Omega_i^2} \right)}$$

Where $\rho_i$ is the average ion gyro-radius and $\omega$ is the wave frequency in the plasma frame. For wave frequencies in the plasma frame approaching $\Omega_i$ this relation provides essentially electrostatic waves and is invalid for waves where $\omega \geq \Omega_i$. In calculating the predicted $E_x/B_y$ ratio from this expression we ignore the finite frequency correction. This is because the errors given by the standard deviation in the measured wave frequency are significantly larger than the average wave frequency and extend to include 0 Hz. This does alter significantly the result below frequencies of 100 Hz in the spacecraft frame (or $k_{sp} \approx 0.1$). Panel f shows the comparison between the observed $E_x/B_y$ ratio and the predicted ratio from Equation 8 as functions of $k_{sp}$. Each red line represents the predicted result but with $V_A$ shifted by one standard deviation above and below its average value. The error bars on the observed $E_x/B_y$ curve show that the model prediction lies with one standard deviation of the observations throughout, but generally predicts a wave somewhat more electrostatic than is observed. Given the highly variable density profile throughout this interval this is not an unexpected result since it has been shown elsewhere that coupling to drift modes density gradients can provide smaller $E_x/B_y$ ratios than found in the homogeneous case (Chaston et al., 2005) given by Equation 8. In any case, since the overall trend observed in $E_x/B_y$ matches the predicted results to within one standard deviation we identify these waves as dispersive Alfvén waves.

4. Inside an Alfvénic Density Cavity

To identify the processes occurring within these density depletions we now examine the fields and plasma within a single ‘well behaved’ cavity as shown in Figure 6 and identified in Figure 1. Panel a of this figure shows a Gaussian shaped depression created by the depletion of the cold thermal ionospheric plasma as indicated by the close agreement between the total density and the energetic electron density. Panels b, c and d show that localized within the transverse width of the cavity are electromagnetic fluctuations. The large scale electric field structure underlying the oscillations shown in panel b indicates an electric field pointing southwards then northwards across the cavity. Since the spacecraft at this time is moving southward these fields are converging. In the electrostatic interpretation (Mozer et al., 1977) this suggests excess negative charge within the cavity and the presence of upward parallel electric fields at this altitude or some altitude below the spacecraft. Panel c shows the electric field projected along $B_0$ in the satellite spin plane. Since the spin plane at this time is within $~5^\circ$ of $B_0$, this measured field provides an indication of the parallel electric field across the cavity ($E_z$ or $E_\parallel$). (Alternatively, these fields could be explained by transverse electric fields in the direction of the spacecraft spin axis, however these would need to exceed 1 V/m to account for the observations). This field has a significant DC component directed upwards across the
base of the cavity consistent with the direction of the converging transverse fields in the
electrostatic interpretation. Panel d shows the magnetic field measured across the cavity
from the search coil and fluxgate magnetometers filtered above 0.5 Hz. The back trace in
this panel is a composite measurement from the search coil and fluxgate magnetometers
while the red trace is the result from the fluxgate magnetometer alone. These
measurements show the presence of field-aligned currents on a variety of scales across
the width of the cavity.

The enhanced electric and magnetic field fluctuations within the density the cavity are
co-located with enhanced ion and electron fluxes shown in the remaining panels. The
burst of ions at energies below 100 eV shown in panel e has its peak fluxes coincident
with the largest electric field amplitudes. The integrated result shown in panel g indicates
that these ions provide significant fluxes of upward moving ions from the base of the
cavity. Panel i shows that these ions are distributed largely at angles just greater that 270°
indicating some form of transverse acceleration. In the same panel we can also identify a
very brief burst of upgoing ions at angles close to 360° consistent with the existence of
the quasi-stationary parallel electric field shown in panel c. The electrons within the
cavity as shown in panels h and j have energies generally less than 200 eV and are
distributed largely along the geomagnetic field and flow downwards (180°) towards the
Earth. These observations suggest that these cavities are regions where waves become
focused, produce small scale transverse structure and subsequently cause field-aligned
electron acceleration and transverse ion acceleration.

Figure 7 provides evidence for the focusing of incoming wave power into the density
depletion. Panel a shows the wave power peaking in the density depletion as indeed was
found for all the observed density depletions shown in Figure 3. Panel b shows the
estimated field-aligned wave Poynting flux. This quantity has been calculated using the
composite 3-D search coil/fluxgate magnetometer measurements and E_x above 0.5 Hz.
Since the fluctuation amplitudes in B_y are significantly larger than in B_x, and the
polarization of the electric field in such events from FAST has been shown previously to
be aligned north-south (Stasiewicz et al., 2000a), the unmeasured contribution to the
field-aligned wave Poynting flux, |E_xB_y|/\mu_0 , is expected to make a smaller contribution to
the field-aligned Poynting flux than |E_yB_x|/\mu_0 . Consequently, S_x shown here is
representative of the field-aligned Poynting flux. Significantly the largest field-aligned
Poynting fluxes are observed on the walls of the cavity with somewhat of a gap in the
center of the cavity and are primarily pointing down the magnetic field line towards the
Earth. Panel c shows that the wave Poynting flux measured along the spacecraft
trajectory and perpendicular to B_o (S_z). Since the field-aligned magnetic wave-field, B_z,
is much smaller than the transverse magnetic wavefield the contribution of |E_yB_z|/\mu_0 to
S_z is minimal unless E_y is larger than 1 V/m. Since fields of this magnitude are rarely
measured it is reasonably to assume that S_z shown here is a meaningful representation of
the Northward directed wave Poynting flux. This measurement indicates that the
transverse wave Poynting flux is convergent or focused on the cavity with S_x pointing
southward and northward on the northern and southern sides of the cavity respectively.
Panel d shows the wave phase velocity across the cavity in the plasma frame. The gaps
here occur where either of the two baselines become close to the projection of B_o in the
spin plane and where the phase variation with $\omega_{sp}$ is erratic. As detailed in section 3 this measurement is subject to errors of magnitude similar to the magnitude of the measurements themselves and so are not conclusive. However, the wave phase velocity in the cavity is divergent with $v_{sp}$ pointing northward and southward on the Northern and Southern sides of the cavity respectively. This result is confirmed by the time domain result displayed in panel e where the delay between wave phase fronts measured along the $x_{58-78}$ and $x_{12-14}$ baselines has been measured. The colored lines here indicate the transverse wave phase speed for fluctuations above 2.5 (black), 5 (blue), 10 (green) and 20 Hz (red) and indicate divergence from the centre of the cavity. The magnitudes of these speeds are similar to that found by the frequency domain technique.

Discussion

The observations presented here suggest a model for the propagation of Alfvén waves above the auroral oval and the subsequent acceleration of ionospheric plasmas leading to density cavity formation and the erosion of the auroral ionosphere. A schematic showing Alfvén waves incident on the ionosphere based on these observations is shown in Figure 8. This figure illustrates the refraction of a downward propagating shear Alfvén wave on a pre-existing density depression showing specifically the rotation of the phase fronts on the Alfvén speed gradients comprising the cavity walls. The refraction of the phase fronts on the cavity walls accounts for the outward directed phase velocities found across the cavity as observed in Figure 7. The inward focused Poynting flux observed indicates that the wave group velocity is convergent on the cavity. These observations are consistent with the reversely propagating nature of the inertial Alfvén waves where the transverse wave group and phase velocities are oppositely directed and importantly shows that the wave refraction on the cavity walls leads to the focusing of Alfvén wave energy within the cavity.

The refraction of the incoming wavefronts on the cavity walls leads to phase mixing and continuously provides smaller scales perpendicular to $B_0$ at a rate determined by the magnitude of the density gradient. Ultimately this process is limited by dissipation. As mentioned in section 3 when $\lambda_v \rightarrow \lambda_e$ or $\rho_i$ the wave is damped by field-aligned electron acceleration and transverse ion acceleration respectively. For the observed parameters phase mixing from the largest scales observed down to scales of the order of $\lambda_e$ could occur on time scales of the order of seconds (simulations to be discussed later show this time to be less than one Alfvén wave period). Once these scales have been attained and the wave carries an appreciable parallel electric field, instabilities driven by electrons accelerated in these waves may lead to the production of secondary waves with frequencies close to $\Omega_e$ causing transverse ion acceleration/heating via cyclotron resonance or via the disruption of the ion orbit in waves produced by instability on scales approaching ion gyro-radii. Based on the rather featureless form of the observed wave spectra the second of these acceleration mechanisms seems more probable. Indeed, the Kolmogorov like $k_{sp}^{-1.7}$ wave spectra observed is unlikely to be the result of a linear cascade to smaller scales due the wave refraction on the density gradient. Rather, the observed wave spectra suggest a non-linear cascade with dissipation occurring for scales $\leq 2\pi\lambda_e$. 
The net result of the production of small scale structure in $k_{sp}$ is the acceleration and eventual loss of plasma from the cavity. This is facilitated by the mirror force of the diverging geomagnetic field accelerating the transversely accelerated ions upwards and ambi-polar electric fields acting on ionospheric electrons and dragging them upwards with the ions to maintain charge neutrality. The plasma loss from the cavity walls leads to steeper density gradients and hence more rapid phase mixing and stronger focusing. It may also lead to larger parallel electric fields in the wavefront and hence stronger electron acceleration and so greater instability. This provides a positive feedback loop whereby the plasma loss process itself increases the rate of plasma loss. The process may initially be started by the focusing of incoming Alfvén wave Poynting flux due to dispersive effects in pre-existing shallow transverse density dips (Rankin et al., 2004). With several iterations of the feedback loop these dips will deepen to form cavities which will eventually broaden as the density on its edges is depleted. In this way density cavities may be unstable in the presence of Alfvén waves and very deep density cavities may be formed. With sufficient time adjacent cavities may join together to produce the density profile shown in Figure 1 where a large section of the topside auroral ionosphere has been eroded.

The scenario described above has been simulated through the use of a fluid code (Genot et al., 1999) and more recently through the use of a 2-D PIC code (Genot et al., 2000, 2001, 2004) developed by Mottez et al. (1998). These authors have been able to follow the initially linear and then non-linear evolution of the system as a purely parallel ($k_A=0$) polarized Alfvén wave encounters a density cavity similar to that presented from observations in Figure 6a. While the periodic boundary conditions employed in these simulations does not allow an exact comparison with the observations some salient feature emerge. Firstly, as the wave refracts on the density gradients comprising the cavity walls scales of the order of $\lambda_e$ are formed in $\sim1/20$ of an Alfvén wave period. Genot et al identify the usual linear $E_\parallel$ on transverse these scales scales as well as an additional linear contribution to $E_\parallel$ due to the polarization drift on the density gradient which induces space charges. On density gradients satisfying $1/n\partial n/\partial x \geq k_\perp$ this contribution can significantly enhance the linear parallel field in the wave. This is indicated by the grey-scale in Figure 9a which shows a snapshot of $E_\parallel$ in the PIC simulation along a $1/4$ Alfvén wavelength parallel to $B_0$ (Z). Large scale enhancements of $E_\parallel$ (lightest and darkest shades) are observed on the transverse density gradients represented by the closely spaced density contours in this panel. This result is most clearly shown however, by averaging the parallel field of Figure 9a along $B_0$ to yield the dashed line in Figure 9b which peaks close to the maxima in $dn/dx$ (dot-dashed line in this panel). Secondly, as shown by the solid line and arrows in Figure 9b these authors find that the largest Alfvén wave Poynting fluxes are found on the density gradients (dot-dashed lines) and that this Poynting flux is focussed inwards towards the centre of the cavity. This is independent of wave phase and is consistent with the observations from FAST shown in Figure 7c. Thirdly, the field-aligned electron acceleration that occurs in the linear parallel Alfvén wavefield on the density gradient triggers a Buneman instability followed at a later stage by a beam-plasma instability which generate non-linear electrostatic structures on scales of the order of the Debye length. These structures can be found on the negative
transverse density gradient in Figure 9a and are identified as electron holes and weak double layers typically with electric field amplitudes larger than that of the Alfvén wave field. Such features have been identified in Alfvén waves from FAST when high resolution fields measurements are available. Consequently, these PIC simulations concur with observations to show that the interaction of the Alfvén wave with a density gradient self-consistently produces structuring in the electric field on transverse scales of the order of the cavity itself (several $\lambda_c$) down to Debye lengths.

Of particular interest to this study is however the structuring in the electric field at frequencies less than the oxygen-gyro frequency (~28 Hz) as measured in Figure 5. This can be most transparently examined from a fluid approach. Fluid models for the production of small scale dispersive Alfvén waves and or Alfvénic turbulence in a low beta plasma have been developed based largely on non-linearities associated with the current carried by the wave. Chmryev et al. (1992) have shown that non-linearly interacting electron current sheets in inertial Alfvén waves may lead to the formation of vortices which break-up into smaller scales vortices leading to an energy cascade from larger to smaller scales. Shukla and Stenflo, 1999b have shown that smaller scale dispersive waves can grow from electron beams driven by larger scale waves. Penano and Ganguli (2002) suggest that the operation of a dispersive Kelvin-Helmholtz instability driven by the shear in the $E \times B_0$ flows in the wave fields of larger scale waves may drive smaller scale dispersive Alfvén waves. Although these authors did not extend this modeling beyond the linear case, such a process could lead to a cascade from larger to smaller scales. Seyler (1990) demonstrated from fluid simulations how inertial Alfvén waves above the auroral may evolve non-linearly through collisionless tearing to produce transverse electric field power spectra that tend to a universal $k^{-5/3}$ power law as we show from observations in Figure 5e. Significantly they showed that the observed $E_{\perp}/B_\perp$ spectra obeyed the expected linear result as observed (Wahlund et al. 1998; Stasiewicz et al., 2000b) and shown here in Figure 5f. In a more recent development of this model Seyler and Wu (2001) and Wu and Seyler (2003) have investigated the linear properties of the instabilities generating the Alfvénic turbulence in the simulation and identify a current convective interchange instability as the primary cause of the cascade to smaller scales and the cause of broadband ELF observed (Seyler and Tu, 2003). Alternatively, filamentation instabilities (Champeaux et al., 1999; Shukla and Stenflo, 1999b) may be important in focusing the wave energy and also for producing small scales however the efficacy of this instability for a low beta plasma remains unproven.

A clear indication of the importance of non-linear effects in the wave dynamics inside the density cavity is the large magnitude of the parallel electric field observed as shown in Figure 6c which at times exceeds 100 mV/m. This is amplitude is more than 2 orders of magnitude larger than given by the linear expression for the parallel electric field due to linear electron inertia presented in section 3. Observations of this kind in Alfvén waves are however not unusual and have been reported elsewhere by (Chust et al., 1998; Stasiewicz et al., 1998; Chaston et al., 1999; Ergun et al., 2004) however the origin of these large fields remains unknown. In the fluid description of the plasma the parallel electric field associated with a field-aligned current, such as that carried by an Alfvén wave, is given by the electron parallel equation of motion. This equation shows that the
parallel field can be supported by a number of effects including linear (Goertz and Boswell, 1979), non-linear (Ronnnarck, 1999) electron inertia, parallel electron pressure gradients (Hasegawa, 1976) and anomalous resistivity (Lysak and Carlson, 1981; Streltsov and Lotko, 1996). Incidentally, all of these contributions to $E_{\parallel}$ were included in the simulation performed by Lysak (1983) with the exception of those due to the finite electron pressure gradient. Observations reported by Ergun et al (2004) however suggest that the parallel field may not be well described by the two-fluid approach at all, and a full kinetic treatment such as those typically invoked in the study of strong double layers is required. In fact using Vlasov simulations Singh (2002) has presented a model similar to that first proposed by Mishin and Forster (1995) in which a double layer forms where the field-aligned current in an Alfvén wave encounters a density cavity. In this model transitory parallel fields as large as 100 mV/m are possible for observed parameters. From a single point measurement it is, however, extremely difficult to reliably determine the means by which larger parallel fields in Alfvén waves are supported and we reserve further discussion for a more detailed study.

A significant result of the extreme density depletion provide by Alfvén waves in these cavities is that the electron plasma frequency is less than the electron cyclotron frequency ($\omega_{pe} < \omega_{ce}$). Consequently the Alfvén wave accelerated electrons within these cavities may be unstable to the cyclotron maser instability and hence such cavities may be a source for auroral kilometric radiation (AKR). An Alfvén wave source for AKR has in fact been suggested previously by Olsson et al. (2004). This may be particularly relevant for the Alfvén wave accelerated magnetosheath and or plasma sheet electrons which after reflection from the magnetic mirror form so called ‘electron conics’ bracketing the electron loss cone as visible in Figures 1e particularly at ~06:44:55 UT and hence provide a positive $df/dv_\perp$ and a free energy source for the cyclotron maser instability as described by Melrose (1982).

Finally, the observations reported here are similar to those of what has been termed ‘lower hybrid cavities’ as first reported by Labelle et al. (1986) from sounding rocket observations. These structures have been observed with widths transverse to the geomagnetic field of the order of 20 m and density depletions of 10s % in which waves with frequency in the vicinity of the lower hybrid frequency are found. These have been associated with ion heating (Lynch et al., 1999) and a number of mechanisms have been proposed to account for the ion heating observed (Knudsen et al., 2004). The mechanism attributed for the formation of these cavities whereby pre-existing depletions focus the lower hybrid waves, enhance the wave amplitude, provide ion heating and thereby further density cavitation is in essence the same as that described here for the Alfvénic cavities which are the subject of this paper. However, an obvious difference is that the width of the Alfvénic cavity is much larger than the gyro-radii of energized ions observed within it and so the ion heating mechanisms described by Reitzel and Morales (1996) and Knudsen et al. (2004) which rely on gyro-radii larger than the width of the cavity may be ineffectual in the Alfvénic cavity case. Observations reported by Pincon et al. (1997) and theoretical work by Seyler (1994) and Schuck et al. (1998) suggested that the waves observed in lower hybrid cavities are lower-hybrid eigenmodes. It is also possible that, in the Alfvénic cavity case considered here, the observed fluctuations at the largest
transverse scales could be described as transverse eigenmodes. This has been previously suggested by Stasiewicz et al. (1997). The largest scales are certainly comparable to the width of the cavity and the lowest frequency oscillations observed appear to be contained within it. However, because the phase velocity of the waves is much less than that of lower hybrid waves, and in fact less than the spacecraft speed, it is significantly more difficult to reliably unravel the phase structure of the wave within the cavity than for the lower hybrid case. Because of this we are unable to conclude that we are observing transverse Alfvén eigenmodes inside the cavity. Nonetheless, the Alfvénic cavities we observe could be described as the electromagnetic, low frequency, version of lower hybrid cavities.

Conclusions

In conclusion, we have observed dispersive Alfvén waves on transverse scales including the electron inertial length and energetic ion gyro-radii located in deep density depressions above the auroral ionosphere. The plasma in these cavities may be depleted by more than 50% and in the most depleted cases the ambient ionospheric plasma, usually by far the dominant plasma component at the altitudes of observation, is completely absent. In these cases the cavities are populated by energized field-aligned electrons and transversely accelerated ionospheric ions and plasmas from magnetospheric sources. The field-aligned wave Poynting flux (and hence the wave group velocity) is directed downwards across the density depletion while the transverse wave Poynting flux is directed inwards towards the centre of the cavities observed. There is some evidence to suggest that the wave phase velocity is oppositely directed outwards from the cavity consistent with what would be expected from the refraction on the cavity walls of an initially downward propagating wave. These observations suggest a feedback scenario for plasma loss from the ionosphere facilitated by the production of dispersive Alfvén waves on transverse density gradients and the acceleration of the plasma on the gradients by these waves.

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Figure 1. FAST observations of dayside ionospheric erosion. a) Ion energy spectrogram for the hemisphere opposite to the spacecraft velocity vector. b) Ion pitch angle spectrogram covering the hemisphere opposite to the spacecraft velocity vector. c) Integrated field-aligned ion flux over the same pitch angle range. d) Electron energy spectrogram. e) Electron pitch angle spectrogram. f) Electric field measured perpendicular to $B_0$ along the spacecraft trajectory and pointing roughly northwards. g) Power spectra of panel f). h) Magnetometer measurements perpendicular to $B_0$ and pointing roughly eastwards- black is the fluxgate measurement alone red is fluxgate plus search coil measurement. i) Langmuir probe current (black) and field-aligned current from the electrostatic analyser experiment on FAST (see text for explanation).
Figure 2. Calibrated langmuir probe data (black) from Figure 1 i) and electron density from the electrostatic analyser experiment. The calibration method is described in the text.
Figure 3. Electric field configuration of the FAST satellite in the spin plane.
Figure 4. Phase measurements in the spin plane. 

a) Wavelet spectrogram of the perpendicular to Bo northward pointing electric field. The black trace in this panel shows the density scaled to fit in this panel. 

b) Relative phase between the 1-2 and 1-4 electric field dipoles. The black line in this trace is the predicted spacecraft frame frequency for Doppler shifted structures with transverse size equal to the length of the 1-4 dipole. 

c) Two-point coherence of the measurements from the 1-2 and 1-4 dipoles. 

d) Same as b) except for the 7-8 and 5-8 dipoles. The black line in this panel is the predicted spacecraft frame frequency for Doppler shifted structures with transverse size equal to the length of the 5-8 dipole. 

e) The angle between the 1-2 dipole and B₀.
Figure 5. Wave properties from interferometry. a) Wave number in the spin plane \(k_{sp}\). b) Angle between \(k_{sp}\) and \(B_o\) in the spin plane. c) Wave frequency, the blue line is the average ion-gyro frequency \(\Omega_{i+}\). d) Wave phase speed in the spin plane. e) Power spectra of the wave electric field in the spin plane as a function of \(k_{sp}\). The vertical red line represents the average electron inertial length \(\lambda_e\), the green line is the oxygen gyro-radius \(\rho_{o+}\), and the yellow line is the proton gyro-radius \(\rho_{i+}\). The sloping red line is a fit of a \(k^{-1.7}\) spectral law to the first decade of observations in \(k_{sp}\). f) Ratio of perpendicular to \(B_o\) electric field in the spin plane to the magnetic field perpendicular to both \(B_o\) and the spin plane. The black line shows the expected result for inertial Alfven waves with the red lines showing one standard deviation in \(V_A\). The error bars throughout show 1 standard deviation from the average.
Figure 6. Individual cavity case study. a) Density from the calibrated Langmuir probe (black), electrostatic analyser for electrons (red), and electrostatic analyser for ions (green). b) Perpendicular to \( B_\parallel \) electric field pointing roughly northwards. c) Approximate parallel to \( B_\parallel \) electric field. D) Magnetic field measurements perpendicular to \( B_\parallel \) and pointing roughly eastwards. The red trace is from the fluxgate magnetometer and the black trace from the fluxgate magnetometer plus the search coil magnetometer. e) Ion energy spectrogram for the hemisphere opposite to the spacecraft velocity vector. f) Ion pitch angle spectrogram for the hemisphere opposite to the spacecraft velocity vector. g) Integrated ion flux for the hemisphere opposite to the spacecraft velocity vector. h) Electron energy spectrogram. i) Electron pitch angle spectrogram.
Figure 7. a) Wavelet spectrogram of the perpendicular to Bo wave electric field pointing roughly northwards, the black trace is scaled density. b) Field-aligned wave Poynting flux. c) Transverse wave Poynting flux. d) Wave phase speed spectrogram from interferometry. e) Wave phase speed from a time domain cross correlation analysis for fluctuations above 2.5 (black), 5 (blue), 10 (green) and 20 Hz (red).
Figure 8. Idealized scheme for the interaction of a shear Alfvén wave with a densith cavity above the auroral oval based on observations.
Figure 9. Results from the 2-D PIC simulation of Genot et al.  

a) Parallel wavefield (E_{||}) over 1/4 Alfvén wavelengths along the geomagnetic field and ~6 electron skin depths (\lambda_e=c/\omega_p) across. Gray-scale shows the parallel electric field with positive values shown by lighter shades and negative values by darker shades on a linear scale. Contours show density with a normalized interval of 0.2.

b) Averaged results from panel a). The solid line shows the transverse wave Poynting flux (S_x), the dashed line is E_{||} and the dot-dashed line is the density gradient (dn/dx). The gray shaded portion shows the inner cavity bounded by the maxima in the density gradient.