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A Coaxial Probe Fixture Used for Extracting Complex Permittivity of Thin Layers

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Abstract

We have developed a broad-band technique for measuring the complex permittivity (\(\varepsilon\)) of dielectric materials, especially thin layers. Our method is based on the use of a coaxial probe. The extraction of the complex permittivity uses a capacitance model valid in a broad frequency range dependent on the sample dimensions and the boundary conditions. Compared to transmission line method, one advantage of the coaxial probe is to avoid the costly lithography process, especially for Silicon or SOI substrates. To illustrate our technique, circular samples with a diameter of 2.922 mm are characterised in the range 0.5 – 25 GHz for a thickness of 0.5mm and various relative permittivity up to 12 with a fixed electric conductivity of 0.2S/m.

Index Terms — Broad-band, Characterization and Dielectric Permittivity.

1. Introduction

The knowledge of dielectric properties is very important in studying the absorption of electromagnetic energy, and the propagation of signal in MMICs. Several techniques are found in the literature for determining the dielectric parameters [1]-[2]: cavity, transmission lines, open ended coaxial probes, MIM capacitance, free space [3], etc.

Cavities provide the most efficient permittivity characterization method when only a few frequencies are required [4]; so, suffer from disadvantage of being narrow-band [5]. Transmission line techniques are based on the use of lithography which is long and costly for some substrates like Silicon and SOI [6]. Based on measuring the scattering parameters of a discontinuity embedded in the transmission line, that technique is limited by the accuracy on relative permittivity and loss tangent in high frequency. This limitation is mainly due to the resonance occurring at half-wavelength frequencies [7].

Open-ended coaxial probes are not suitable to thin film layers [8], because this method can give erroneous results if there is even a tiny air bubble or gap near its mouth [9]. MIM capacitance technique is limited in the deduction of losses [10]. Ellipsometry technique, based on free space, provide the permittivity characterization when only one frequency is needed [3].

In recent latest years, the coaxial probe has received attention and has gained favour of many researchers because of its simplicity and is therefore suitable for industrial use [9]-[12].

We develop a procedure to extract complex permittivity for thin dielectric layers, for a broad-band range of frequencies, without the use of the lithography. The sample is completely surrounded by a metallization unlike Stuchly works or Martens [9] . This technique is essentially based on measuring the reflection coefficient from a coaxial transmission line, terminated with the material under test as shown in figure 1.
The method supposes that the material is not magnetic ($\mu_{\text{eff}}=1$). 

Electromagnetic simulations were made with a 3D simulator based on the Finite Integration Method (FIM) in order to analyse the frequency limitations of the probe.

The main frequency limitation of the probe is due to the resonance depending on the dielectric permittivity and boundary conditions on different sides of the probe.

The electric equivalent model of this probe is showed in figure 2.

In this work, we give the theory of the method before digging deeper of the method through its principle secondly. Simulation results in order to consolidate the theory will be done in the third point before seeing thickness effects and ending by a conclusion.

2. Principle of the method

Consider a uniform waveguide ended by a capacitance composed of the sample to characterize. The reflection is measured in two cases: With and without the sample. From the measured reflection, we define the termination admittance \[ y_{\text{mat}} = \frac{S_{11\text{CO}} - S_{11\text{mat}}}{R_0} \] \[ y_{\text{air}} \] (1)

where \( R_0 = 50 \Omega \), \( S_{11\text{CO}} \) the reflection coefficient measured from open-circuit and \( S_{11\text{mat}} \) the reflection coefficient measured with material.

Some hypotheses are made to simplify the extraction. We consider that the reflection coefficient is unity when we have the open circuit. The reference plan of the calibration is the plan \( P_0 \) (fig.2).

2.1. Capacitance model

From the electrical circuit the admittances are expressed by:

\[
\begin{align*}
    y_{\text{air}} &= G_{\text{cond}} + j\omega C_{\text{air}} \\
    y_{\text{mat}} &= G_{\text{cond}} + G_{\text{mat}} + j\omega C_{\text{mat}}
\end{align*}
\] (2)

From the effective permittivity depending on the dimensions of the probe, the intrinsic relative permittivity is calculated using a polynomial fitting function. The extraction of the conductivity requires an additional correction function depending on the frequency.

2.1. Polynomial fitting function

The parameters of this model are obtained from the electromagnetic simulations of different permittivity values, with and without losses.

We assume the complex dielectric permittivity linked to the effective permittivity by the following relation:

\[ \varepsilon_r' = a\varepsilon_r' + b \] (4)

where “a” and “b” are adjusted coefficients to minimize the fitting error.

The accuracy obtained on the relative permittivity depends on the metallic conductors, and leads also to a parasitic dependence with the frequency of the extracted conductivity.

Our investigations proved that best results are obtained when the sample is circular, and if it’s totally surrounded by metallic walls. The choice of the connector to use is important in terms of frequency range
2.3. Extraction Method Flow Chart

We illustrate the global method in the following flow chart.

![Diagram Flow Chart of the Method](image)

The method is based on the use of measurements and Electromagnetic simulations.

In fact, metal conductivity appears in the final results because of the contact between the dielectric and the metallization (copper in our case).

### 3. Simulation results

Our purpose is to extract initial dielectric relative permittivity up to 25GHz. We use a connector K (2a=1.27mm and 2b=2.9mm) specified up to 40GHz. The probe length is l=10mm with a diameter of 2.922mm. We consider different relative permittivity from 4 to 12 with a constant conductivity of $\sigma_{\text{dieu}}=0.2\text{S/m}$ considered to be constant in broad-band.

The sample thickness is $e=500\mu\text{m}$. The probe conductor (metal) is copper with conductivity of $\sigma_{\text{cop}}=58,13.10^6\text{S/m}$.

#### 3.1. Extraction of permittivity and electric conductivity

These results show that the relative permittivity can be extracted with an error less than 2%, from electromagnetic (E.M) simulations.

The operating frequency band is limited by the resonances of the cavity formed by the dielectric under test. The electric conductivity extracted when relative permittivity varies from 4 to 12 is shown in Figure 4b.

![Electric Conductivity (S/m) Extracted from E.M.S before corrected the conductivity of the sample.](image)

We observe some variations of the extracted conductivity according to the permittivity. So, we develop another principle of correction through MATHCAD to get high in frequency. We developed a routine to make that correction. Here are results we obtain.

![Electric Conductivity (S/m) Extracted from E.M.S after corrections of conductors losses.](image)
These results show that depending on the value of the relative permittivity, the extraction of electric conductivity is limited in frequency.

3.2. Extraction of variable electric conductivity

Now, we change the sample conductivity when the relative permittivity is $\varepsilon_r=12$ and its diameter is $d=2.922\text{mm}$, using the connector K. We set up the following conductivities: $\sigma_{\text{die}}=0.2; 0.5$ and 1 S/m (Figure 5).

![Figure 5. Electric Conductivity (S/m) Extracted from E.M.S with different conductivity values.](image)

These results are in agreement with electromagnetic simulations (E.M.S). The method used proves that conductivity doesn’t influence the principle adopted up. Using this fixture, we can notice also if you can’t make correction on the conductivity, you will just extract easily that up around 10GHz. But if you do this, the frequency bandwidth will grow up to 20.5GHz.

4. Conclusion

In this paper we have discussed a new coaxial probe technique for accurate extraction of the relative permittivity of thin film. We demonstrated that approach can be readily applied with good precision to layers having thickness greater than 400µm.

The frequency range depends on dielectric dimensions. The probe with circular sample and metallic walls operates up to 25 GHz for relative permittivity up to 10. We observe some undulations coming from the driving line mismatch, but this affects the accuracy on of the permittivity extraction. In low frequencies, some problems of mesh refinement from the electromagnetic simulator affect the accuracy. The sample diameter must be chosen equal to the outside conductor of the connector to optimise the frequency range of the characterisation. The sample thickness associated to the value of the relative permittivity determines the capacitance to be extracted.

This method has been applied to circular samples with a diameter of 2.922 mm, a thickness of 0.5mm, characterised in the range 0.5 – 25 GHz for relative permittivity up to 12 with an electric conductivity of 0.2S/m.

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