Supercover model, digital straight line recognition and curve reconstruction on the irregular isothetic grids

David Coeurjolly, Loutfi Zerarga

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David Coeurjolly and Loutfi Zerarga

Laboratoire LIRIS
Université Claude Bernard Lyon 1
43 Bd du 11 novembre 1918
F-69622 Villeurbanne, France

Abstract

On the classical discrete grid, the analysis of digital straight lines (DSL for short) has been intensively studied for nearly half a century. In this article, we are interested in a discrete geometry on irregular grids. More precisely, our goal is to define geometrical properties on irregular isothetic grids that are tilings of the Euclidean plane with different sized axis parallel rectangles. On these irregular isothetic grids, we define digital straight lines with recognition algorithms and a process to reconstruct an invertible polygonal representation of an irregular discrete curve.

1 Introduction

When a straight line is digitized on a square grid, we obtain a sequence of grid points defining a digital straight-line segment. This computer representation of such a simple Euclidean object has drawn considerable attention in many applications (drawing [3], shape characterization [15,13,9], ...). The structure of DSL is now well known and links have been illustrated between DSL and objects from number theory or theory of words (see Rosenfeld and Klette [24] for a survey on digital straightness). Beyond this characterization, an important task in computer vision consists in the recognition of DSL segments. More precisely, given a set of pixels, we have to decide if there exists a DSL segment that contains the given pixels. Many efficient algorithms exist to implement such a recognition process [16,18,11,5]. Based on a digital straight line recognition algorithm, we can also define a segmentation process that decomposes a discrete curve into maximal DSL segments. The next step of the segmentation process is to reconstruct a polygonal curve from the discrete
data such that its digitization is equal to the original discrete curve. This process is called an invertible reconstruction of a discrete curve [4,26,12]. The invertible property is an important one in discrete geometry since it allows to convert discrete data to Euclidean ones such that no information is added nor lost.

In this article, we are interested in defining a geometry on irregular isothetic grids. More precisely, we consider grids defined by a tiling of the plane using axis parallel rectangles. Such a grid model includes, for example, the classical discrete grid, the elongated grids [25] and the quadtree based grids [17]. In [8], a general framework has been proposed that defines elementary objects and a digitization framework, the supercover model. An important aspect of this general framework is the consistency with classical definitions if the discrete space is considered.

Many applications may benefit from these developments. For example, we can cite the analysis of quadtree compressed shapes, or the use of geometrical properties in objects represented by interval or affine arithmetics (see discussion in [8]). Based on this irregular model, we define digital straight lines with recognition algorithms and a process to reconstruct an invertible polygonal representation of an irregular discrete curve.

Section 2 presents more formal definitions in the irregular grids: adjacencies relations, objects, arcs, curves and the supercover model. Based on a definition of the irregular isothetic digital straight lines, we present algorithms to recognize maximal irregular discrete straight segments and to reconstruct invertible polygonal arcs and curves (Section 3). Experiments and results are shown in Section 4.

2 Preliminary definitions

2.1 The irregular isothetic model

First of all, we define an irregular isothetic grid, denoted $\mathbb{I}$, as a tiling of the plane with isothetic rectangles. In this framework, the rectangles have not necessarily the same size but we can notice that the classical digital space is a particular irregular isothetic grid. In that case, all squares are centered in $\mathbb{Z}^2$ points and have a border size equal to 1. Figure 1 illustrates some examples of irregular isothetic grids. A rectangle of an isothetic grid is called a pixel. Each pixel $P$ is defined by its center $(x_P, y_P) \in \mathbb{R}^2$ and a size $(l_{x_P}, l_{y_P}) \in \mathbb{R}^2$. Before we introduce objects and straight lines in such grids, we need adjacency relations between pixels.
Fig. 1. Examples of irregular isotropic grids: (from left to right) the classical discrete grid \((x_P, y_P) \in \mathbb{Z}^2\) and \(l_P^x = l_P^y = 1\), an elongated grid \((l_P^x = \lambda, l_P^y = \mu)\) and \((x_P, y_P) = (\lambda i, \mu j)\) with \((i, j) \in \mathbb{Z}^2\), a quadtree decomposition (for a cell of level \(k\), \((x_P, y_P) = \left(\frac{m}{2^k}, \frac{n}{2^k}\right)\) and \(l_P^x = l_P^y = \frac{1}{2^{k+1}}\) for some \(m, n \in \mathbb{Z}\)); a unilateral and equitransitive tiling by squares: the size of the biggest square is equal to the sum of the two other square sizes; finally a general irregular isotropic grid.

**Definition 1 (ve–adjacency, e–adjacency)** Let \(P\) and \(Q\) be two pixels. \(P\) and \(Q\) are ve-adjacent if:

\[
|x_P - x_Q| = \frac{l_P^x + l_Q^x}{2} \quad \text{and} \quad |y_P - y_Q| \leq \frac{l_P^y + l_Q^y}{2},
\]

or

\[
|y_P - y_Q| = \frac{l_P^y + l_Q^y}{2} \quad \text{and} \quad |x_P - x_Q| \leq \frac{l_P^x + l_Q^x}{2}.
\]

\(P\) and \(Q\) are e-adjacent if we consider an exclusive “or” and strict inequalities in the above ve-adjacent definition.

In the following definitions, we use the notation \(k\)-adjacency in order to express either the ve-adjacency or the e-adjacency. Using these adjacency definitions, several basic objects can be defined:

**Definition 2 (k–path)** Let us consider a set of pixels \(\mathcal{E} = \{P_i, i \in \{1, \ldots, n\}\}\) and a relation of \(k\)-adjacency. \(\mathcal{E}\) is a \(k\)-path if and only if for each element \(P_i\) of \(\mathcal{E}\), \(P_i\) is \(k\)-adjacent to \(P_{i-1}\).

**Definition 3 (k–object)** Let \(\mathcal{E}\) be a set of pixels, \(\mathcal{E}\) is a \(k\)-object if and only if for each couple of pixels \((P, Q)\) belonging to \(\mathcal{E} \times \mathcal{E}\), there exists a \(k\)-path between \(P\) and \(Q\) in \(\mathcal{E}\).

**Definition 4 (k–arc)** Let \(\mathcal{E}\) be a set of pixels, \(\mathcal{E}\) is a \(k\)-arc if and only if for each element of \(\mathcal{E} = \{P_i, i \in \{1, \ldots, n\}\}\), \(P_i\) has exactly two \(k\)-adjacent pixels, except \(P_1\) and \(P_n\) which are called the extremities of the \(k\)-arc.

**Definition 5 (k–curve)** Let \(\mathcal{E}\) be a set of pixels, \(\mathcal{E}\) is a \(k\)-curve if and only if \(\mathcal{E}\) is a \(k\)-arc and \(P_1 = P_n\).

If we consider pixels such that \(l_P^x = l_P^y = 1\) and \((x_P, y_P) \in \mathbb{Z}^2\) (i.e. a 2D digital space), all these definitions coincide with the classical ones [22,23]. More precisely, the ve–adjacency (resp. e–adjacency) is exactly the 8-adjacency (resp. the 4-adjacency). In the following, we only consider geometrical properties of
such objects. A complete topological analysis of $k$–curves and $k$–objects is not addressed here.

2.2 Supercover model on the irregular isothetic grids

Before defining the digital straight lines on the irregular isothetic grids, we have to consider a digitization model. In the following, we choose to extend the supercover model. This model was first introduced by Cohen-Or and Kaufman in [10] on the classical discrete grid and then widely used since it provides an analytical characterization of basic supercover objects (e.g. lines, planes, 3D polygons, ...) [2,1].

**Definition 6 (Supercov on irregular isothetic grids)** Let $F$ be an Euclidean object in $\mathbb{R}^2$. The supercover $S(F)$ is defined on an irregular isothetic grid $\mathbb{I}$ by:

$$S(F) = \{ P \in \mathbb{I} \mid B(P) \cap F \neq \emptyset \}$$

$$= \{ P \in \mathbb{I} \mid \exists (x,y) \in F, |x_P - x| \leq \frac{l_P^x}{2} \text{ and } |y_P - y| \leq \frac{l_P^y}{2} \}. \quad (1)$$

where $B(P)$ is the rectangle centered in $(x_P,y_P)$ of size $(l_P^x,l_P^y)$ (if $l_P^x = l_P^y$, $B(P)$ is the ball centered in $(x_P,y_P)$ of size $l_P$ for the $L_\infty$ norm).

Properties of this model are discussed in [8].

![Fig. 2. Illustration of the supercover digitization of a curve (left) and of a straight line (right).](image)

Figure 2 illustrates some examples of the supercover digitization of Euclidean objects. If $\mathbb{I}$ is the classical digital space (i.e. $(x_P,y_P) \in \mathbb{Z}^2$ and $l_P^x = l_P^y = 1$), many links exist between the supercover of an Euclidean straight line and classical digital straight line definitions [1,24]. Since we have not any assumption on the irregular grid, no strong topological property can be stated on the supercover of an Euclidean straight line.

**Proposition 1 ([8])** Let $l$ be an Euclidean straight line and a $\mathbb{I}$-grid, the $S(l)$ is a single $ve$–object.
3 Irregular isothetic digital straight line definition and recognition

3.1 Definitions and IDSL Recognition

Definition 7 (Irregular isothetic digital straight line) Let $S$ be a set of pixels in $\mathbb{I}$, $S$ is called a piece of irregular digital straight line (IDSL for short) iff there exists an Euclidean straight line $l$ such that:

$$S \subseteq \mathbb{S}(l).$$  \hspace{1cm} (3)

In other words, $S$ is a piece of IDSL iff there exists $l$ such that for all $P \in S$, $\mathbb{B}^\infty(P) \cap l \neq \emptyset$.

To detect if $\mathbb{B}^\infty(P) \cap l$ is empty or not, we use the notations presented in Figure 3. Hence, $\mathbb{B}^\infty(P) \cap l$ is not empty iff $l$ crosses either (or both) the diagonals $d_1$ or $d_2$ of $P$.

![Diagram](image)

Fig. 3. Notations used to detect if the pixel of center $(x_P, y_P)$ belongs to the super-cover of a straight line $l$ ($d_1$ and $d_2$ are the diagonals of the rectangle $P$).

Without loss of generality, we suppose that $l$ is given by $y = \alpha x + \beta$ with $(\alpha, \beta) \in \mathbb{R}^2$ (an appropriate treatment can be design to handle the straight lines $x = k$ with $k \in \mathbb{R}$). To solve the recognition problem, we use the following statement:

$$\mathbb{B}^\infty(P) \cap l \neq \emptyset \iff l \cap d_1 \neq \emptyset \text{ and } \alpha \geq 0$$ \hspace{1cm} (4)

or

$$l \cap d_2 \neq \emptyset \text{ and } \alpha < 0$$ \hspace{1cm} (5)

During a recognition process, it is convenient to consider the set of Euclidean straight lines whose digitization contains the set of pixels $S$: if such a set is empty, we can conclude that $S$ is not a discrete straight line segment. In the literature, the set of Euclidean straight lines whose digitization contains $S$ is called the preimage of $S$. Many works have been done concerning the preimage analysis in the classical discrete grid [14,18,19].
Given a pixel \( P \), Equation (4) can be represented by two inequalities in the \((\alpha, \beta)\)-parameter space:

\[
\mathcal{E}^+(P) = \begin{cases} 
\alpha \left( x_P - \frac{v_x}{2} \right) + \beta - y_P - \frac{v_y}{2} & \leq 0 \\
\alpha \left( x_P + \frac{v_x}{2} \right) + \beta - y_P + \frac{v_y}{2} & \geq 0
\end{cases}
\]

(6)

Details on the computation of these inequalities can be found in [8]. If we consider Equation (5), we may obtain the following inequalities:

\[
\mathcal{E}^-(P) = \begin{cases} 
\alpha \left( x_P - \frac{v_x}{2} \right) + \beta - y_P + \frac{v_y}{2} & \geq 0 \\
\alpha \left( x_P + \frac{v_x}{2} \right) + \beta - y_P - \frac{v_y}{2} & \leq 0
\end{cases}
\]

(7)

\( \mathcal{E}^+(P) \) is defined for \( \alpha \geq 0 \) and \( \mathcal{E}^-(P) \) for \( \alpha < 0 \). We can now define the preimages of a piece of IDSL:

**Definition 8 (Preimages of an IDSL)** Let \( S \) be a piece of IDSL, the two preimages \( \mathcal{P}^+ \) and \( \mathcal{P}^- \) of \( S \) are given by:

\[
\mathcal{P}^+(S) = \bigcap_{P \in S} \mathcal{E}^+(P) \quad \text{and} \quad \mathcal{P}^-(S) = \bigcap_{P \in S} \mathcal{E}^-(P).
\]

(8)

Hence, the recognition process can be described as follows:

**Proposition 2** Let \( S \) be a set of pixels in a \( \mathbb{I} \)-grid. \( S \) is a piece of IDSL iff \( \mathcal{P}^+(S) \neq \emptyset \) or \( \mathcal{P}^-(S) \neq \emptyset \).

Using Proposition 2, the recognition of a piece IDSL leads to a linear programming problem: we have to decide whether a linear inequality system has a solution or not. To solve this problem, two different classes of algorithms exist: the IDSL identification algorithms which decide if \( S \) is an IDSL or not, and the IDSL recognition algorithms which return the complete preimages (maybe empty) of the recognized IDSL. To solve the identification problem, incremental \( O(n) \) solutions exist if \( n \) is the number of linear constraints \( (i.e. \) the number of irregular pixels in our case) \([20,6]\). To completely describe the preimages, the incremental Preparata and Shamos algorithm \([21]\) may be used whose computational cost is optimal in \( O(n \log n) \). In \([8]\), an algorithm based on a linear programming procedure is proposed to recognize IDSL given a set of pixels. This algorithm can also be used to segment an irregular arc, \( i.e. \) to decompose the arc into maximal piece of IDSL (see Figure 4).

The segmentation of a curve gives information concerning the geometry of the curve. In the next section, we detail an algorithm to obtain an invertible polyline from the irregular set of pixels.
3.2 Invertible reconstruction of irregular arcs and curves

In the following, we propose an algorithm to construct an Euclidean polyline from a discrete curve such that its digitization is equal to the original discrete curve. If we consider the supercover digitization model, a polyline $L$ is an invertible reconstruction of a discrete curve $S$ if it lies inside the discrete curve. More precisely, for each Euclidean point $p$ on $L$, there exists a pixel $P$ in $S$ such that $p$ belongs to $P$.

Usually, the reconstruction task is a post-treatment of a DSL segmentation algorithm: first we decompose the discrete curve into maximal DSL, then, for each piece of DSL, we compute a representative Euclidean segment. The main drawback of this approach is that it is difficult to ensure the reversibility of the polyline vertices [4,12]. In the classical discrete grid, Sivignon et. al. [26] propose an invertible reconstruction algorithm in which both the recognition and the Euclidean segment extraction are performed at the same time. More precisely, the authors reduce the problem forcing the first extremity of the segments to be inside the discrete curve. Then, they perform an analysis on the preimage of the segment to compute the second extremity.

In the following, we propose a similar algorithm without the computation of the preimages that would have required complex linear programming procedures. The main idea is to use a visibility test technique commonly used in computational geometry to solve shortest path extraction problems [7].

3.2.1 Visibility cone based approach

First, we define the predicate $\text{TURNO\text{P}OSITIVE}(a, b, c)$ which is true if the points \{a, b, c\} in the plane are sorted counterclockwise. Note that such a predicate can be computed according to the sign of the determinant $det(ab, bc)$. 
Let $S = \{P_i\}_{i=0\ldots n}$ be a $k$–arc, we first fix the first extremity $p_0$ of the first segment such that $p_0 \in P_0$. Given the pixel $P_i$ $k$–adjacent to $P_0$, we denote $e_0$ the Euclidean segment shared by the two pixels $P_0$ and $P_1$. We consider the first cone $C_0(p_0, s, t)$ with center $p_0$ and defined by the two points $s$ and $t$ such that $\{p_0, t, s\}$ is sorted counterclockwise (i.e. $\text{TURNPOSITIVE}(p_0, t, s)$ is true) and such that $s$ and $t$ coincide with the extremities of $e_0$ (see Figure 5–(left)). $C_0$ is a visibility cone since for each point $p$ in the intersection between $C_0$ and the pixels of $S$, the segment $[p_0p]$ lies exactly in $S$. In other words, the supercover digitization of $[p_0p]$ is a subset of $S$.

According to the previous definitions, the cone $C_0$ describes a subset of the preimages $\mathcal{P}^+({\{P_0, P_1\}})$ and $\mathcal{P}^-({\{P_0, P_1\}})$ in the parameter space. Indeed, each straight line $(p_0p)$ crosses the pixels $P_0$ and $P_1$. More precisely, the set of straight lines contained in the cone $C_0$ is the segment in the $(\alpha, \beta)$-parameter space which corresponds to the intersection between the preimages $\mathcal{P}^+$ and $\mathcal{P}^−$ and the straight line defined by the point $p_0$. Hence, as proposed in [26], we could have performed all computations in the parameter space $(\alpha, \beta)$ but the analysis using visibility cones leads to a more efficient algorithm.

![Fig. 5. Illustration of the visibility cone based algorithm: (from left to right) the first cone $C_0$, the update of the cone considering the pixel $P_2$ and an example when the visibility fails.](image)

The algorithm can be sketched as follows: for each pixel $P_i$, we consider the shared segment $e_i$ between $P_{i-1}$ and $P_i$. Then, we have a simple procedure to update the current cone $C_{j}(p_j, s, t)$ according to $e_i(u, l)$ (such that $\text{TURNPOSITIVE}(p_0, t, u)$ is true). The different cases are presented in Figure 6. Note that using the predicate $\text{TURNPOSITIVE}$, Algorithm 1 is valid whatever the orientation of the curve and the segment $[ul]$ is not necessarily vertical nor horizontal.

From the different cases presented in Figure 6, we can design a simple algorithm (Algorithm 1) with three possible outputs: the visibility fails, the cone is updated or the cone remains unchanged.

When the update procedure fails, it means that there is no euclidean straight line going through $p_j$ and crossing the pixel $P_i$. In that case, we need to start a new recognition process. Hence, we set up a new cone $C_{j+1}(p_{j+1}, s, t)$ where $s$ and $t$ are given by the edge $e_i$. To compute the new center of the cone $p_{j+1}$ we use a similar strategy as in [26]: we consider the bisector of the cone
Fig. 6. Illustration of the different cases when we update a cone: (from left to right) the cone is not modified, only the point $t$ is moved, only the point $s$ is moved, both $s$ and $t$ are moved, and finally, the visibility fails.

**Algorithm 1** Visibility cone update procedure

Let $C_j(p_j, s, t)$ be the current cone and $e_j(u, l)$ the shared segment between $P_j$ and $P_{j-1}$

if (not $\text{TurnPositive}(p, t, u)$) or $\text{TurnPositive}(p, s, l)$ then
  return $\emptyset$ (the visibility test fails)
else
  if $\text{TurnPositive}(p, t, l)$ then
    $t \leftarrow l$
    return $C_j(p_j, s, t)$
  end if
  if (not $\text{TurnPositive}(p, s, u)$) then
    $s \leftarrow u$
    return $C_j(p_j, s, t)$
  end if
end if

(dashed straight lines in Figure 5) and we define $p_{j+1}$ as the midpoint of the intersection between the bisector and the pixel $P_{j-1}$ (this intersection is not empty since $P_{j-1}$ has already been considered). The idea of this strategy is to obtain a polyline as centered as possible in the discrete curve. By definition of Algorithm 1, the segment $[p_j, p_{j+1}]$ lies inside the irregular discrete curve. Hence, if we repeat the above process for each pixel of the $k-$arc, the final polyline is an invertible reconstruction of the arc (see Figure 5-(right) and 7).

**3.2.2 Overall algorithm**

**Algorithm 2** Invertible reconstruction of a $k$-arc

Let $S = \{P_i\}_{i=0..n}$ be a $k-$arc and $p_0$ the first point in $P_0$

Set $j = 0$

Initialization of the cone $C_j(p_j, s, t)$ using $P_0$ and $P_1$ such that $\text{TurnPositive}(p_j, t, s)$ is true

$p_j$ is the first vertex of the final polyline

for $i$ from 2 to $n$ do
  Compute the shared segment $e_i$ between $P_i$ and $P_{i-1}$
  $C' \leftarrow$ Update the visibility cone using algorithm 1
  if $C' = \emptyset$ then
    Compute the point $p_{j+1}$ using the bisector of $C_j$ and the pixel $P_{j-1}$
    Initialization of a new cone $C_{j+1}$ with $p_{j+1}$ and $e_i$
    Mark $p_j$ as a vertex of the final polyline
  else
    $C_j \leftarrow C'$
  end if
end for

Algorithm 2 presents the complete incremental reconstruction algorithm based on the visibility cone update procedure. Since Algorithm 1 updates the cone is $O(1)$, the overall computational cost of Algorithm 2 is $O(n)$ if $n$ is the number of irregular pixels. Compared to the segmentation algorithm based on
the complete preimages, the IDSL segments may be shorter since subsets of
the preimages are considered. However, this restriction allows us to construct
an invertible polyline.

![Illustration of the reconstruction algorithm: (left) the sequence of cones during
the visibility test and (right), the reconstructed polygonal curve.]

3.2.3 Invertible reconstruction of $k-$curves

If we consider an irregular $k-$curve $S = \{P_i\}_{i=0..n}$, the reconstructed polyline
must be closed and thus defines a simple polygon. Hence, we can use Algorithm
2 for the pixels $P_0$ to $P_n$ and add a specific analysis to handle the adjacency
between $P_n$ and $P_0$ that creates as few as possible new vertices. Let $C_j(p_j, s, t)$
be the last visibility cone such that the intersection between $P_n$ and this cone
is not empty. Several cases occur (see Figure 8): for example, if $p_0 \in C_j$, we
close the polyline using the segment $[p_jp_0]$. Otherwise, we may move $p_0$
along $(p_0p_1)$ if there exists an intersection between $C_j$ and the straight line $(p_0p_1)$
that lies inside $P_0$ (see Figure 8-(b)). In that case, we still close the curve using
$[p_jp_0^\prime]$ and the global reversibility of the polygonal curve can be easily proved.
Other cases can be derived (for example using the visibility from $p_0$ to $P_n$) but
additionnal vertices may be inserted to the polygonal curve (see Figure 8).

![Different cases to end the reconstruction of a $k-$curve: (a) and (b) we can
close the curve using $[p_0p_j]$ or $[p_0^\prime,p_j]$, (c) a new vertex $p_{j+1}$ must be inserted, and
(d) we have to test cases (a), (b) or (c) using the cone $C_{j+1}$ centered in $p_{j+1}$.]

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4 Experiments

We have constructed a C++ library to handle elementary irregular objects (irregular pixels, \( k \)-arcs and \( k \)-curves). Using this library, we have implemented the reconstruction algorithm described in the previous section (the code is available on the following web page: http://liris.cnrs.fr/~dcoeurjo/Code/Reconstruction). Figure 10 presents the result of Algorithm 2 on an irregular \( k \)-arc. Since the classical digital grid is a specific irregular isothetic grid, Algorithm 2 can also be used to reconstruct a polygonal curve from a classical 4-connected curve (see Figure 10). In this case, results are similar to [26].

![Fig. 9. Result of Algorithm 2 on an irregular \( ve \)-arc: the input \( ve \)-curve and the invertible reconstruction using Algorithm 2.]

![Fig. 10. Result of Algorithm 1 on a classical 4-connected curve: the input 4-connected curve and the invertible reconstruction using Alg. 2.]

5 Conclusion

In this article, we have presented a global digitization framework on irregular isothetic grids: the supercover model. Based on this digitization scheme, we have defined the digital straight lines and briefly presented algorithmic solutions to solve the recognition and segmentation problem. We have also presented an \( O(n) \) on-line algorithm to reconstruct a polygonal curve from a discrete irregular arc or curve. Since the classical regular digital grid can be seen as a particular irregular grid, all the presented framework is consistent with classical definitions and algorithms. To achieve the linear in time computational cost, we have only considered specific subsets of the preimages.
defined by the visibility cones. Thus, the reconstruction may not be optimal
in the number of segments. Additional processes similar to [12] in the classical
discrete case could be investigated.

Since adaptive grids or QuadTree based decompositions are specific irregular
isothetic models, an important future work is to use the proposed framework
to provide geometric tools to characterize object boundaries in such grids.
Furthermore, topological definitions and data structure to handle irregular
objects is an important on going research topic.

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