Raman Spectroscopy of Nanomaterials: How Spectra Relate to Disorder, Particle Size and Mechanical Properties

Gwénaël GOUADEC and Philippe COLOMBAN
Laboratoire de Dynamique, Interactions et Réactivité (LADIR), UMR7075 - CNRS & Université Pierre et Marie Curie - Paris 6, 2 rue Henry Dunant, 94320 Thiais, France

ABSTRACT

The purpose of this review is to provide non-specialists with a basic understanding of the information micro-Raman Spectroscopy (µRS) may yield when this characterization tool is applied to nanomaterials, a generic term for describing nano-sized crystals and bulk homogeneous materials with a structural disorder at the nanoscale - typically nanoceramics, nanocomposites, glassy materials and relaxor ferroelectrics. The selected materials include advanced and ancient ceramics, semiconductors and polymers developed in the form of dots, wires, films, fibres or composites for applications in the energy, electronic and aeronautics-aerospace industries. Following a short introduction, the text is divided into four sections:

• The 1st section outlines the principles of conventional µRS.
• The 2nd section introduces the main effects for nanomaterials, with special emphasis on two models that connect Raman spectra features to "grain size", namely the Phonon Confinement Model (PCM) and the Elastic Sphere Model (ESM).
• The 3rd section presents the experimental versatility of µRS applied to nanomaterials (phase identification, phase transition monitoring, grain size determination, defect concentration assessment, etc.).
• The 4th section deals with the micro-mechanical aspects of µRS ("Raman extensometry"). Special emphasis is placed on the relationship between the stress-related coefficients $S^{\varepsilon/\sigma}$ and the macroscopic response of the materials to the applied stress.

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1. INTRODUCTION

Most properties of traditional ceramics (notably a good shapability and low sintering temperatures) stem from the fact that their raw material -natural clay- is nanosized [1]. Besides, because of the sharpness of the human eye, the particle size of pigments must be smaller than 500 nm to homogeneously colour enamels and glasses [2]. Potters and ceramists have thus been using nanoscience for thousands of years [3,4] but a new generation of engineered nanomaterials (grain size <100nm) has been in development -if not already commercially available- for the last twenty years. Reducing the dimension of matter domains down to the nanometer scale confines the electronic and vibrational wavefunctions while increasing the specific surface, which results in unique properties and opens a wide range of potential applications in domains as different as [5-8]:

- **Optics:** pigments for the cosmetic industry (metal-oxides), fluorescent markers (quantum dots), photonic crystals (multiplexing and switching in optical networks), quantum computer components, light emitting devices [9], etc.
- **Mechanics:** cutting tools, wear-resistant and anti-corrosion coatings (cemented carbides), "nano-polishing" powders (SiC, diamond, boron carbide), fibres and fibre-reinforced composites, structural nanocomposites [10], etc.
- **Electrical devices:** miniaturized silicon chips, single electron transistors, relaxor ferroelectrics [11-14], carbon or silicon nanotube transistors, lithium batteries [15], solar cells [16], etc.
- **Magnetic devices:** data storage, giant magneto-resistances (reading heads), etc.
- **Reactivity:** improved combustion of fuel-rich propellants (Al, Ti, Ni, B) [17], filters (Ti/Zr oxides), nanosensors [18,19], catalysts [20], etc.
- **Biomedicine:** in vivo drug delivery, diagnostic and monitoring devices, [21] fluorescent markers, etc.

The challenge for the so-called nanotechnologies is to achieve perfect control of nanoscale-related properties. This obviously requires correlating the parameters of the synthesis process (self assembly, microlithography, sol-gel, polymer curing, electrochemical deposition, laser ablation...) with the resulting nanostructure. Not all conventional techniques are suitable for that purpose but Raman Spectroscopy (RS) has already proven to be. For quite a long time this technique was mainly devoted to fundamental research, but instrumental progress (laser miniaturization, CCD detection, notch filters and data processing softwares) have rendered it a general characterization method. Not only can it provide basic phase identification but subtle spectra alterations can be used to assess nano-scale structural changes and characterize micromechanical behaviour. RS thus is a unique tool for probing or mapping nanophases dispersed in a matrix (e.g. pigments in a ceramic glaze [2], precipitates in a fibre coating [22]), surface-formed nanophases (corrosion mechanisms [23]) and solid-state devices [24-27]. Some specific features can even be used to study a charge transfer [28,29], a film orientation [30], the size of clusters trapped in nano-cavities [31], Grüneisen parameter [32], configurational order (for instance the proportion of trans-gauche chains in Poly(ethylene terephthalate)-PET [33]) or intercalation [34], interfacial [35] and polymerisation [36] reactions.

The present article, which is an extended version of previous papers from our group [37-39], is intended to review the achievements of RS in the world of nanomaterials, both from the fundamental and experimental points of view. The selected materials include advanced and...
ancient ceramics, glasses, semiconductors and polymers developed in the form of dots, wires, films, fibres or composites for applications in the energy, electronic and aeronautics-aerospace industries. The interested reader might find useful complementary information in references [40-43] and a special issue of the Journal of Raman Spectroscopy [44].

- The 1st section outlines the principles of conventional micro-Raman Spectroscopy (µRS).
- The 2nd section introduces the main effects at stake for nanomaterials, with special emphasis on the Phonon Confinement Model (PCM) and the Elastic Sphere Model (ESM) that connect spectral features to "grain size". We made a special effort to select the keystone papers, those which introduced, popularised or significantly improved the different concepts.
- The 3rd section presents the experimental versatility of µRS as applied to nanomaterials (phase identification, phase transition monitoring, grain size determination, defect concentration assessment, etc.).
- The 4th section deals with the mechanical aspects of µRS ("Raman extensometry"). Special emphasis is placed on the relationship between the stress-related coefficients $S^{\epsilon/\sigma}$ and the macroscopic response of materials to the applied stress.

2. THE FUNDAMENTALS OF RAMAN SPECTROSCOPY

2.1 Vibrations in Crystalline Solids

All collective vibrations that occur in crystals can be viewed as the superposition of plane waves that virtually propagate to infinity [45]. These plane waves, the so-called normal modes of vibration, are commonly modelled by quasi-particles called phonons. A normal coordinate of the form $Q=Q_0\cos(2\pi v_{ib} t)$, which is actually a linear combination of bond lengths and bond angles, is associated with each normal mode. Depending on the dominant term in the normal coordinate, modes can be classified as either stretching ($\nu$), bending ($\delta$), torsional ($\tau$) or librational ($R'/T'$ pseudo-rotations/translations) and lattice modes (the latter include the relative displacement of the unit cells).

![Figure 1](image)

**Figure 1**: The transverse phonons ($\|k\|=\frac{2\pi}{\lambda}$) in a 1D-solid with unit cell parameter l.
For a three-dimensional (3D) solid containing \( N \) unit cells with \( p \) atoms each, \((3pN-6)\) different phonons can propagate and their wavevectors \((\mathbf{k})\) all point in a volume of the reciprocal space called the Brillouin Zone (BZ). There are modes with in-phase oscillations of neighbouring atoms and modes with out of phase oscillations. The former are called acoustic vibrations and the latter are called optical vibrations. On the other hand, phonons are referred to as being longitudinal or transversal depending on whether the atoms move parallel or perpendicular to the direction of wave propagation given by \( \mathbf{k} \). Phonons with the same two criteria are all gathered in the BZ on \( 3p \) (discrete) lines called the dispersion branches (see an example in Figure 17). Figure 1 is an illustration of the concept of phonons in crystals showing the transverse vibrations in a one-dimensional lattice where \( p=2 \).

### 2.2 The Raman Effect

The polarization of the dipoles excited in solids when a laser (amplitude \( E_0 \); frequency \( \nu_{\text{las}} \)) interacts with phonons (of frequency \( \nu_{\text{vib}} \)) depends on the polarisability tensor \( \bar{\alpha} \):

\[
\bar{P} = \bar{\alpha} \times E_0 \cos(2\pi \nu_{\text{las}} t)
\]

\( \bar{\alpha} \) terms can be individually described as functions of the normal vibration coordinates \( Q \) using a Taylor approximation:

\[
\alpha_{ij} = \alpha_{ij}^0 + \left( \frac{\partial \alpha_{ij}}{\partial Q} \right)_{Q=0} \times Q (i, j = x, y \text{ or } z)
\]

\[
P_i = \sum_j \alpha_{ij} \times E_j = \sum_j \left[ \alpha_{ij}^0 E_j \cos(2\pi \nu_{\text{las}} t) + \frac{E_j Q_0 \left( \frac{\partial \alpha_{ij}}{\partial Q} \right)_{Q=0}}{2} \left[ \cos(2\pi(\nu_{\text{las}} - \nu_{\text{vib}}) t) + \cos(2\pi(\nu_{\text{las}} + \nu_{\text{vib}}) t) \right] + \ldots \right]
\]

With the scattered electric field being proportional to \( \bar{P} \), Eq. (3) predicts both quasi-elastic (\( \nu = \nu_{\text{las}} \)) and inelastic (\( \nu = \nu_{\text{las}} \pm \nu_{\text{vib}} \)) light scattering. The former is called the Rayleigh scattering and the latter, which occurs only if vibrations change polarisability \((\partial \alpha_{ij}/\partial Q \neq 0)\), is the Raman scattering [46,47]. Raman spectroscopists normally refer to vibration modes by their wavenumber \( \bar{\nu} = \nu_{\text{vib}} / c \) (\( c \) the light speed, \( \bar{\nu} \) in cm\(^{-1} \) unit) and the classical electromagnetic theory of radiations from an oscillating dipole demonstrates that Raman peaks have a Lorentzian shape:

\[
I(\bar{\nu}) = I_0 \times \int_{(\text{BZ})} \frac{d^3\mathbf{k}}{\left[ \bar{\nu} - \bar{\nu}(\mathbf{k}) \right]^2 + \left( \frac{\Gamma_0}{2} \right)^2}
\]

\(^1\) There are \( 3pN \) degrees of freedom but the 6 rotations and translations of the whole solid are not considered to be proper vibrations.

\(^2\) The BZ describes the geometrical distribution of the wavevectors in the reciprocal space in the same way the unit cell describes the geometry and periodicity of the crystalline arrangement in the direct space.

\(^3\) The experimental bands are a convolution between this natural lineshape, the instrumental transfer function [48,49] and the disorder-induced distribution of vibrators. It is often taken as a Gaussian or a Voigt function (a perfectly symmetric convolution of Lorentzian and Gaussian functions).
In Eq. (4), $\bar{\nu}(\bar{k})$ represents the dispersion branch to which the mode belongs and $\Gamma_0$ is the half-width for the ordered reference structure.

The scattering of one photon ($\bar{k} \sim 0$) by n phonons (wavevectors $\bar{k}_i$) is governed by the momentum conservation rule:

$$\sum_{i=1}^{n} \bar{k}_i = \bar{k}_{\text{scattered}} - \bar{k}_{\text{incident}} \approx 0$$

(5)

Therefore, only vibrations from the centre of BZ (BZc), i.e. long wavelength phonons can be active in any one phonon process (first order spectrum). However, not all BZc phonons are active in RS. According to Eq. (3), $\partial \alpha_{ij}/\partial Q$ terms must be different from zero and this condition is governed by the symmetry of the crystals. Raman activity can therefore be predicted through Group Theory [52].

An interesting feature of Eq. (3) is to reveal the dual sensitivity of RS to the electrical ($\alpha_{ij}$) and mechanical ($\nu_{\text{vib}}$) properties of the investigated materials. Two kinds of parameters will therefore influence the spectra:

(i) parameters acting on the "mechanics" like atomic mass, bond strength or the system geometry (interatomic distances, atomic substitutions) will set the peaks positions (the eigenfrequencies of matter vibrations).

(ii) parameters acting on the "charge transfer" (onio-covalency, band structure, electronic insertion) will set intensity, on the basis of the vibration-induced charge variations occurring at the very bond scale.

As polarisability changes for different kinds of bonds, Raman intensity may not be used to quantitatively determine the amounts of different phases. This limitation can sometimes be an advantage since some secondary phase like an enamel pigment [60-62] or carbon in SiC fibers [38] can be detected in a very small quantity (even traces) and its crystalline structure identified [63]. Elements with high atomic numbers and that are situated on the right side of the periodic table (covalent materials in general) are good Raman scatterers whereas ionic structures are difficult to analyse with RS. As for metals, their surface plasmons limit light penetration. Thus, their Raman signal is extremely weak. There are, however, compounds like the superconducting YBaCuO oxides in which metal atoms produce a strong Raman signal, owing to their covalent bonding in certain directions of the structure [65,66]. Some transition metal ions from the 3d (chromium) or 4f (lanthanides) groups produce strong

\[ 4\pi\alpha(\nu) = \sigma(\nu) n c \]

(N1)

In Eq. (N1), $n$ is the refraction index and $c$ the light speed. There is also a formal equivalence between the Raman Intensity and $\sigma(\nu)$ (see page 375 in Ref. [54]) but it has rarely been characterized on experimental Raman spectra [55]:

\[ I_{\text{Raman}}(\nu) \propto n^2(\nu)^{+1}\sigma(\nu) ; n^2 = \text{Bose occupation factor} \]

(N2)

The presence of mobile charge carriers in ionic conductors can be identified by Raman bands with temperature dependent intensity [56,57]. More discussion on the ionic motions can be found in papers by Funke et al. [58,59].

Hexagonal close-packed metals like Be are an exception [64].
fluorescence signals which often mask the Raman spectra but can be used for short range structure [67] and/or residual stress [68] assessment.

2.3 Conventional Raman Spectrometers

Figure 2-a shows the principle of a Raman spectrometer. Up-to-date equipment would include holographic gratings, for improved excitation light rejection, a set of monochromators and a liquid nitrogen- or Peltier effect-cooled CCD mosaic for detection [46,69]. The laser source is often built-in but light coming from an external excitation source can also be used. In the "macro"-configuration, the beam section is ~1 mm² but the laser spot can be reduced to ~1 µm diameter by using the high-magnification microscope objectives with which most commercial Raman spectrometers are equipped. The technique involved is known as micro-Raman Spectroscopy (µRS). The main additional options are motorized stages for XY(Z) mappings and optical fibre plugs for connection to remote optical heads equipped with microscope objectives [70].

Raman maps are images generated from spectra recorded at discrete points of the sample (the recording is automated). They show the variation of any fitted parameter (i.e. intensity, width or position of one band) as a function of the point of analysis. If the mapping is regular and sufficiently tight, one gets a "smart map" of the parameter (colour or contrast scaling) superimposed with the optical image of the probed area (see Figure 14-b) [39]. Raman parameters can thus be correlated with the crossover from one specific region (phase) to another.

Raman mapping is not to be mistaken for direct Raman imaging where a large area of the sample is probed all at once and no fitting is required. More precisely, only photons from a narrow spectral domain are sent to the CCD mosaic and each pixel receives those coming from a given area of the sample. The intensity of the signal thus reveals the presence and location of any substance with a strong Raman signal in the selected spectral window. This is used by customs services to search for drugs hidden in permissible powders like sugar [71].
2.4 Lateral and "in-depth" Resolution of Conventional µRS

Owing to the diffraction of light, the intensity coming from a point observed through a microscope is distributed over an "Airy disk". The lateral resolution \( R \), which is the smallest distance between two points to still appear distinctively on the microscope image, is half the width of the Airy disks. According to the Rayleigh criterion [72]:

\[
R = \frac{0.61 \times \lambda}{NA}
\]

In Eq. (6), \( \lambda \) is the light wavelength and \( NA \) represents the numerical aperture (see Figure 2-b). As for the axial resolution (\( \Delta z \)) of µRS, an estimate is given by the depth of field, which is defined as half the width of the axial intensity profile. Born and Wolf came up with a famous analytical expression for \( \Delta z \) [73], which is well approximated by a simpler expression by Conrady [74]:

\[
\Delta z = \frac{\lambda}{n \sin^2 \theta} \quad \Rightarrow \quad \Delta z_{\text{through air}} = \frac{\lambda}{NA^2}
\]

Under "standard" conditions (\( n=1, \lambda=500\text{nm}, NA=0.5 \)), the typical lateral and in-depth resolutions of µRS are 1 and 2 \( \mu \text{m} \), respectively. Even with the smallest visible wavelength (~400 nm) and the highest numerical apertures (oil immersion objectives with \( n=1.515; NA=1.4 \)), one should not expect a lateral resolution better than \( R=0.2 \mu \text{m} \) (the Abbé criterion states that the wavy nature of light forbids to distinguish points closer than \( \lambda/2 \)) and a field depth below \( \Delta z=0.4 \mu \text{m} \) [75].

![Figure 3: The intensity profile obtained from a step by step Rayleigh mapping of a multilayered SiC/BN coating deposited on a Hi-Nicalon fibre (\( \lambda=632.8\text{nm}, \text{Obj.} \times 100 \text{ Olympus MSPlan ULND, NA=0.80} \)) can be deconvoluted by a function (shown in Ref. [76]) characterizing the distribution of energy in the spot (Adapted from Ph. Colomban, Spectroscopy Europe, 15[6], pp. 8-16, 2003).](image-url)
However, if a series of spectra are recorded at very close equidistant locations (X-Y stages commonly have a displacement resolution of one tenth of a micron), a reduced "effective" spot size is obtained through a convolution of the spot profile with the displacement step (see Figure 3 generated from a Rayleigh scattering mapping procedure; similar conclusions would apply to Raman images). Even then, there is still a high number of "nano-sources" contributing to the Raman signal.

2.5 Resonant Raman Spectroscopy (RRS)

If the energy of the laser excitation (usually in the UV-nIR range) is high enough to approach those of the various electronic states of the material (in other words if the material is coloured), Raman spectra may be mingled with photoluminescence spectra arising from excited electronic levels. The consequence is the strong enhancement of some vibrational modes (near-resonance/resonance Raman scattering) but one should notice that the probed chemical bonds are in a markedly disturbed state [22,26,27,77-79]. The light penetration is reduced to a few tens of nanometers only (Δz coloured in Figure 2-b), which makes μRS a good method for surface analysis [23,80]. If films or fibre-reinforced composites made of absorbent materials are polished with surface to growth direction and surface to fibre axis angles slightly different from, respectively, 90 and 0°, then in-line scans of the samples provide high spatial resolution across the film thickness [84-86] or the fibre-matrix contact region (interphase) [22].

The penetration depth δ of the light is directly related to the wavelength-dependent coefficient of linear absorption α(λ) (cm⁻¹):

\[
\delta = \frac{\lambda_{\text{excitation}}}{4\pi nk} = \frac{1}{\alpha(\lambda)} \tag{8}
\]

In Eq. (8), n and k are respectively the refraction and extinction indexes. δ is indeterminate in the (frequent) lack of absorption coefficients but switching excitation wavelengths close to the electronic absorption threshold can help separate surface from bulk Raman contributions [37]. This is illustrated in Figure 4, where polyaniline fibres spectra recorded with red, green and blue laser lines, are compared [87]. The bottom spectrum corresponds to the surface of these fibres (maximum electronic absorption) where a "type I" monoclinic form of polyaniline is dominant [88]. By contrast, the bulk of the fibre (as seen with blue excitation on the top spectrum) contains more of the type II orthorhombic form. Following the same principle, Shen and Pollak [49] or Yakimova et al. [48] used multiple laser lines to measure spectra at different depths below the surface of semiconductor films.

Note that when the absorption is very high, temperature may rise at the point of laser impact, even for a few μW/μm² irradiation. This effect is reduced if the sample is either dispersed in a non-absorbing matrix or put in a rotating cell or a low temperature cryostat but often results in a wavenumber shift or even a chemical degradation of the sample (oxidation, decomposition, etc.). It is then mandatory to calibrate the thermal effects [89-91]. Besides, whenever the absorbing phase is not dispersed in a transparent matrix, a significant part of the scattered light intensity may be reabsorbed.

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7 Resonance Raman spectra recorded with different wavelengths of excitation are also a way of characterizing excitons and polarons in semiconductors [81,82] and conducting polymers [83].
Figure 4: Raman spectra recorded on polyaniline/Camphor Sulfonic Acid fibres. The use of three different excitation wavelengths modifies the probing depth (Adapted from A. El-Khalki et al., Synthetic Metals, 139[2], pp 215-220, 2003).

2.6► Analysis of "Isolated" Units: the Molecular Scheme

Eq. (4) corresponds to a description where vibrations in solids are pictured as collective waves but another description applies to solids with bonds of different strengths. In this "molecular" description, clusters of strong covalent bonds are isolated from one another by weaker ionic bonds and, thus, become the relevant vibrational unit (localized vibrations). All atoms from this unit must exclusively belong to it (including, for example, oxygen atoms from polymerised oxides) for the normal coordinates of Eq. (2) & (3) to coincide with given bond lengths and bond angles. The spectra then reveal stretching and bending modes equivalent to those of polyhedral (mostly tetrahedral or octahedral) isolated molecules [92-95]. The difference arises from the cations generating T' (translational) and R' (rotational) libration modes. The molecular scheme describes most organic polymers but also crystalline/amorphous inorganic polymers such as silicates, phosphates, niobiates, titanates [96-98] and all compounds with polyatomic cations such as NH$_4^+$, H$_3$O$^+$ or N$_2$H$_5^{2+}$ (page 379 in Ref. [54]). A given vibration then always appears in the same region, its exact position giving information about the local environment of the corresponding bonds, both in the crystalline and amorphous states [94,99-104]. Yet, these bonds are probed with a one square micrometer section beam, which means one gets only an average view over their distribution.
2.7 "Nano-specific" Modes

There are two ways of truly isolating the Raman signal coming from nano-particles. One is by having a nanoparticle to be the only one of its kind in the laser's path (SERS) while the other involves a breaking of the $\lambda/2$ diffraction limit of optical microscopes (nano-Raman).

2.7.1 Surface-Enhanced Raman Spectroscopy (SERS)

The Raman signal may be amplified by several orders of magnitude for molecules adsorbed on roughened surfaces [105,106], colloid particles [107] and nanowires [108] of transition metals (mostly silver). This technique is called Surface-Enhanced Raman Spectroscopy (SERS) and the amplification results from the interaction between the electromagnetic field of the laser excitation and the surface plasmon of the metal. This enhancement may be so high that a signal can be recorded with just one or a few particles being probed simultaneously. Unfortunately, getting the right conditions for SERS requires much sample preparation and additional measurements are often necessary to interpret the SERS data collected [107,109]. SERS is seldom applied to solid films [110] and is mainly used in Biology, where "molecules" must be sufficiently diluted to follow their interactions (e.g. a protein with its "Redox" partner [111]). Roy et al. used SERS for a specific study of the surface carbon in Hot Filament CVD carbon [112,113]. Azoulay et al. also demonstrated the possibility of selecting single wall carbon nanotubes (SWCNTs) by SERS [114].

2.7.2 Nano-Raman

In Near-Field Scanning Optical Microscopy (NSOM in the US; SNOM in Europe), the $\lambda/2$ diffraction limit of optical microscopes (Abbé criterion) is surpassed thanks to the addition of a small aperture made at the end of a tapered probe, frequently a metal-coated optical fibre tip. This confines the optical field and thus imposes the lateral resolution [115]. The probe must be kept extremely close to the sample using micro-manipulation tools borrowed from Atomic Force and Scanning Tunneling Microscopes (AFM/STM) and the technique becomes NSOM-Raman or, simply, "nano-Raman", when a NSOM equipment is coupled with a Raman spectrometer [116-124]. Even under the most favourable operating conditions, the excitation is reduced by the optical fibre cut-off and only a faint signal is collected from the small volume that is excited. This is why nano-Raman proved to be efficient only with very good Raman scatterers [120,121,123]. More recently, SERS capability was implemented on nano-Raman equipments by the addition of a vibrating apertureless metallic tip brought close to the surface of the sample [125-128]. This is called Tip Enhanced Raman Spectroscopy (TERS). The intensity enhancement varies in $d^{-12}$ (d being the probe-sample spacing) [129] and getting a good TERS signal is thus far from trivial.

SERS and nano-Raman will not be further discussed in this review. The focus shall instead be placed on the nano-related information that can be retrieved using conventional µRaman spectrometers that have nowadays become standard in a number of research and industrial laboratories, owing to the availability of convenient commercial instruments.
3. THE VIBRATIONAL SPECTRA OF NANOMATERIALS

The translational symmetry of crystalline materials is broken at grain boundaries, which results in the appearance of specific surface and interface vibrational contributions [130]. Besides, the grains outer atomic layers often react with neighbouring species (lattice reconstruction, passivation/corrosion layers, contamination) and experience steep thermo-chemical gradients during processing, which generates new phases, with their own spectral contributions. These two elements are often neglected in RS but we can expect them to become very significant in nano-crystals, where the concentration of grain boundaries is very high.

3.1 Phase Identification and Phase Transitions in Nanoparticles

In many nanomaterials, the Raman spectrum remains sufficiently similar to that of the corresponding single crystal to facilitate direct identification of the phases [28,32,131-146]. Once the Raman spectra are known, phase transitions can be characterized (transition temperature, transition pressure, transition order) through mode variation, much the same way as in bulk materials [93,138,147-159]. Besides, the observation of any theoretically forbidden mode is a very sensitive probe of lattice distortions [132,160].

Barborini and co-workers showed with RS that the structure of gas phase-deposited TiO$_2$ clusters turned from rutile to anatase whenever they reached 5nm in diameter [158]. A difference in surface energy usually plays a determinant role in such phenomenon, as proposed a long time ago by R.C. Garvie for zirconia [161]. Similarly, Fray and Payne showed how the temperature of the orthorhombic-tetragonal phase transition of BaTiO$_3$ ceramics depended on the grain size [159].

3.2 Analysis of Amorphous Domains

Micro Raman spectroscopy is sometimes more powerful than X-ray analysis for detecting and monitoring crystallisation/amorphisation [93,101,147,162-165] in covalent materials. Of course, both crystallographers and Raman spectroscopists characterize disorder through peak broadening. Yet, while a loss of long distance translational periodicity (of high atomic number atoms) is always associated with broadening in the case of diffraction patterns, only lattice and librational (R', T') modes are sensitive to the same "long distance" disorder in RS [166]. The width of the other Raman modes is mainly sensitive to the "local" crystal field, more specifically the short range order in the first (0.1-0.5 nm) and second (0.5-5 nm) atomic shells. If the "molecular" description of vibrations applies (see §2.6), then Raman bending modes are even specifically sensitive to local geometric disorientation and Raman stretching modes to the neighbouring disorder (particularly atoms from other sublattices or electric defects resulting from substitutions/vacancies).

In fact, diffraction discriminates "periodical" domains from "disordered" ones but does not easily differentiate clear-cut separations in the real space and progressive orientational disorders (para-crystal), especially in strongly covalent structures such as organic and inorganic polymers (pp. 615-620 in Ref. [167]). In materials, mainly polymers, which present
interlocking submicronic "crystalline" and "amorphous" conformational domains [168-175], the distinction is sometimes possible using µRS. The simplest way to picture the problem is to fit lattice modes with two components, one representing the amorphous state and the other the crystalline state. The area ratio of the two underlying areas yields a good estimate of crystallinity [176,177]. Figure 5 illustrates this point with a spectrum of the polyamide 6.6 fibre. Polarized analysis clearly shows the orientational effect of straining (fibre extrusion) on the nanocrystals whereas the specific analysis of the low frequency components, which show the collective chain movements, facilitates the separate analysis of the amorphous (wide Gaussian band) and crystalline (narrow Lorentzian) phases. These results were used to demonstrate that the mechanical fatigue of the fibres results from the progressive transformation of the amorphous phase [170,171,173]. Nanophase separation was also investigated in glasses where the connectivity of constitutive polyhedra sets the wavenumbers [178]. Some bands could be attributed to definite clusters on the basis of comparison with experimental spectra of reference crystalline phases [178] or first principle Density Functional Theory (DFT) calculations [95,179].

Figure 5: Low wavenumber Raman spectra of the PA 66 polyamide fibre (FUHP grade, Rhodia) recorded with the exciting electric field polarized either parallel (//) or perpendicular (⊥) to the fibre axis (λ exc=514.5nm) [172]. The collective mode at ~100cm⁻¹ is highly polarized. The zoom shows how the crystalline and amorphous (much wider) contributions can be analysed separately [170].

3.3 Size Determination in Nanomaterials

Two models are widely used to derive particle size from Raman spectra: the Phonon Confinement Model (PCM) projects Raman "inactive" bulk modes onto the BZc whereas the Elastic Sphere Model (ESM) describes the free oscillations of homogeneous spheres.

3.3.1 The Phonon Confinement Model (PCM)

Richter et. al. proposed a very intuitive Phonon Confinement Model (PCM) for the phonons in nanospheres of diameter L [180]. They simply multiplied the plane wave describing a
phonon, with wavevector \( \vec{k}_0 \), in a perfect crystal (\( \Phi(\vec{k}_0, \vec{r}) = u(\vec{k}_0, \vec{r}) e^{i\vec{k}_0 \cdot \vec{r}} \), \( u \) having the same spatial periodicity as the lattice) by a Gaussian function:

\[
\Phi(\vec{k}_0, \vec{r}) = e^{-\frac{(\vec{r} - \vec{k}_0)^2}{\alpha^2}} \times u(\vec{k}_0, \vec{r}) e^{i\vec{k}_0 \cdot \vec{r}}
\]  

(9)

Assuming \( u(\vec{k}_0, \vec{r}) \sim u(\vec{r}) \) and using FT to refer to Fourier Transforms, Eq. (9) is equivalent to:

\[
\Phi(\vec{k}_0, \vec{r}) \propto \text{FT}^{-1} \left[ \text{FT} \left( e^{-\frac{(\vec{r} - \vec{k}_0)^2}{\alpha^2}} \times e^{i\vec{k}_0 \cdot \vec{r}} \right) \right] = \int d^3 \vec{k} \; C(\vec{k}_0, \vec{k}) e^{i\vec{k}_0 \cdot \vec{r}}
\]  

(10)

with \( C(\vec{k}_0, \vec{k}) = \frac{1}{(2\pi)^3} \int d^3 \vec{r} \; e^{-\frac{(\vec{r} - \vec{k}_0)^2}{\alpha^2}} \times e^{i\vec{k}_0 \cdot \vec{r}} \times e^{i\vec{k} \cdot \vec{r}} \)

(11)

Thus, the wave associated with a phonon confined in an imperfect crystal simply is a superposition of plane waves with \( |C(\vec{k}_0, \vec{k})|^2 \) weight. Recalling that each wave gives rise to a Lorentzian (Eq. (4)), Raman intensity is eventually given by:

\[
I(\nu) \propto \int_{\text{BZ}} d^3 \vec{k} \; \left| C(\vec{k}_0, \vec{k}) \right|^2 \frac{1}{(\nu - \nu(\vec{k}))^2 + \left( \Gamma_0 \right)^2}
\]  

(12)

Eq. (12) mathematically expresses the Raman selection rule breaking induced by phonon confinement\(^8\) with a weighed exploration of the dispersion curve. Taking \( k_{\text{BZ}} \) as the edge of BZ, \( q \) as the reduced wavevector (\( q = k / k_{\text{BZ}} \)) and assuming isotropic mode dispersion \([181]\), Eq. (12) yields:

\[
I(\nu) \propto \int_{q=0}^{q=1} dq \; e^{\frac{k_{\text{BZ}}^2 (q-q_0)^2 L^2}{2\bar{\nu}}} \times \frac{1}{(\nu - \nu(q))^2 + \left( \Gamma_0 / 2 \right)^2}
\]  

(13)

This is the equation to which most authors refer when using the PCM \([180-187]\)\(^9\). For Quantum Dots (QDs), NanoWires (NWs) or slabs, the PCM is easily adapted using the appropriate expressions for the \( d^3 \vec{k} \) integration volume in Eq. (12) \([190-194]\)\(^10\). Knowledge of

\(^8\) As a consequence of Heisenberg’s uncertainty principle, the uncertainty \( \Delta k = \Delta p / \hbar \) on the wavevector must remain above or equal to \((2L)^{-1}\).

\(^9\) Based on the triple hypothesis that modes from different crystallites are uncorrelated, that lifetimes can be simulated with Lorentzian broadening \((\Gamma_0)\) and that susceptibility variations \((\Delta \chi)\) are proportional to the normal vibrations coordinates, Nemanich, Solin and Martin \([188]\) predicted the Raman intensity on probing of N orthorhombic crystallites to be:

\[
I(\nu) \propto S(\vec{k}_0, \vec{\nu}) = \frac{N}{c^4 \sqrt{T}} \left[ \frac{n_B(\nu) + 1}{\nu} \right] \nu^{-4} \sum_{k_j} \left| C(\vec{k}_j, \vec{\nu}(\vec{k})) \right|^2 \left| F(\vec{k} - \vec{k}_0) \right|^2 \times \frac{\Gamma_0^2 / 4 \pi}{\left( \nu - \nu(\vec{k}) \right)^2 + \left( \Gamma_0 / 2 \right)^2}.
\]  

(13)

In this Equation, \( S(\vec{k}_0, \vec{\nu}) \) is the Fourier transform of polarisability variations associated with Raman scattering, \( (n_B(\nu) + 1) \) is the Bose population factor \( (n_B(\nu) = 1 / (e^{\nu/kT} - 1)) \), \( C \) is the Raman coupling coefficient for branch \( j \) and \( |F(\vec{k} - \vec{k}_0)|^2 \) is the uncertainty on the wavevector induced by phonon confinement \([188,189]\). This approach is entirely equivalent to the PCM if \( F \) function is assumed to be Gaussian and the occupation term is neglected (this simplification is justified when only one band is modeled).

\(^10\) Note that the PCM failed to predict the Raman shift in silicon spherical or columnar nanocrystals. Zi et al. showed with a Bond Polarisability Modelling that it could rather be predicted using the following expression \([195]\):
the Vibrational Density of States (VDOS) is required for computing Eq. (13) and is obtained either from neutron scattering measurements, from data on structurally parent structures or from \textit{ab initio} calculations based on a rigid-model structure [183,184,196-198]. The PCM, which does not apply to acoustic modes (their energy is nil at BZc) and is very seldom used with TO modes (on account of their low dispersion [193,199]), is almost exclusively applied to LO modes. With LO dispersion usually being maximum at BZc, the integration in Eq. (13) introduces additional contributions on the low frequency side of the single crystal mode and the resulting peaks are asymmetric. Peak adjustment is not always mandatory once phonon confinement has been invoked. In first approximation, the peak shift is indeed proportional to the inverse of the grain size [188,200]. The overall half-width at half-height also is, as was reported for nanocrystalline CeO$_2$ [197,198] (see Figure 6) or boron nitride [188] and can be verified with data on Ge [185].

In the paper introducing the PCM [180], Richter \textit{et al.} took $\alpha = 2$. Fauchet and Campbell later tested several forms for the weighing function introduced in Eq. (9) [194]. They came to acknowledge the choice of a Gaussian form but chose the more confining parameter $\alpha = 8\pi^2$ first proposed by Tiong \textit{et al.} [199], which corresponds to a rigid confinement hypothesis ($|C(\vec{k}_0,\vec{k})| = 0$ for $r = 1/2$) [181,184,186,198,201]. A bond polarisability modelling of vibrations in silicon nanocrystals also returned a value of 9.67 for $\alpha$ [202]. As a matter of fact, $\alpha$ may be considered, with $L$, like an adjustment variable of the model [185]. Besides, $L$ should not systematically identify with the grain size. Phonons can indeed be confined by any "spatially limiting" feature in the grain (twins, stacking faults, inclusions, vacancies, boundaries, pores, etc.). $L$ is therefore equal to $2\pi/\Delta k$, where $\Delta k$ is the extension of BZ domain of which the modes are activated. It is nothing but a coherence length which can correspond to a grain size [180,192,203-206], defects/impurities interspacing [186,197,201,207,208], the extension of cation-ordered domains in incommensurate phases [92], that of undamaged crystalline domains in ion-implanted GaAs [199], the size of polytypic domains [182,209,210] or clusters in semiconducting alloys [183,184,211] and ferroelectrics [12]. The physical interpretation of $L$ therefore is a key element. For instance, Weber thought it was the grain size in CeO$_2$ but found an order of magnitude discrepancy with results from electronic microscopy [198]. In fact, Kosacki \textit{et al.} showed $L$ was the distance between defects in the oxygen lattice of ceria (see Figure 18-b and attached comments) [197]. Carles \textit{et al.} showed that the meaning of $L$ even changes in germanium particles depending on their size. $L$ corresponds to the actual size for the bigger grains, but represents the domain size in smaller grains where alloying has taken place [181]. See also Fig 16 and the discussion for SiC "grain size".

Although Richter \textit{et al.} took $\vec{k}_0$ at the BZc, their model did not preclude it from standing somewhere else (which many authors have forgotten). Adding this degree of freedom to the model finds a physical justification in at least two situations. First, when nanoparticles are surrounded by a parent material, the phonons can be reflected by grain boundaries and their interferences can "activate" modes away from BZc. This effect was mentioned by Arora and co-workers for CVD-diamond particles embedded in amorphous carbon. They fitted the spectra with as many as 20 contributions calculated with Eq. (13) at specific values of $\vec{k}_0 \neq 0$

\[
\nu_{\text{vn}} = \nu_{\text{bulk}} - A \left( \frac{a}{L} \right)^{\gamma}
\]

\text{(N4)}

In equation (N4), $a$ is the lattice constant whereas $A$ and $\gamma$ fully characterize the nanocrystal geometry.
Second, in their "Random Stacking Fault" model of disorder in silicon carbide, Rohmfeld et al. used a Bond Polarisability Model (BPM) to calculate the influence of stacking defects occurring with \( \Delta L \) interspacing [182,209]. They concluded to the extinction of BZc modes to the benefit of modes with wavevectors equal to \( \mathbf{k}_m=(2m+1)\pi/\Delta L \); \( m=0,1,2... \), which is analogous to the application of Eq. (13) at \( k_m \) points. Even though disorder and nanosize effects often participate together to phonon confinement, their relative contributions can theoretically be isolated whenever \( k_0 \) is allowed to vary:

- disorder will disturb short range order and fold the BZ. \( \mathbf{k}_0 \) will be away from BZc and L should then be inversely proportional to the density of defects.
- if the confinement results from the existence of domains in which order is perfect, typically nanocrystals, then the activated modes should be centred in \( \Gamma (\mathbf{k}_0=0) \) and L will represent the grain size.

\[
\Gamma (\text{cm}^{-1}) = 10.1 + 124.7/d_g (\text{nm})
\]

**Figure 6**: The half-width at half height of CeO\(_2\) Raman band (466 cm\(^{-1}\)) plotted as the inverse of the grain size obtained by X-ray diffraction. Reprinted from Solid State Ionics, 149[1-2], I. Kosacki et al., Raman scattering and lattice defects in nanocrystalline CeO\(_2\) thin films, pp 99-105, 2002, with permission from Elsevier.

In Reference [180], Richter et al. attributed the Raman signal not accounted for by the PCM to fully amorphous matter (they actually worked on microcrystalline silicon). This explanation was later used by several authors [192,201,213-215] but should not hide the fact that the PCM is based on approximations and neglects some peculiarities of vibrations in nanomaterials:

1) **the PCM supposes isotropy**: As is, the PCM only applies to materials with homogeneous structure in all directions of space (spherical model). An "isotropic dispersion hypothesis" is
probably acceptable for almost any material in the limit of $k_\theta$ close to BZc [185] but integrating Eq. (13) along the main directions of the BZ returns more satisfactory results [216]. Carles et al. proposed a way of simply taking anisotropy into account [181]: all directions are plotted on the same reduced wavevector axis and wavenumbers are simply averaged. As for $\Gamma_0$, it is adjusted with an anisotropy parameter based on the maximum branch "splitting" observed between different directions.

**ii)** the PCM supposes uniform size and shape: Another approximation is made with the PCM when a Gaussian weighing function is introduced in Eq. (9). This assumes all crystallites have the same shape -either spherical [180] or orthorhombic [188]- and size, whereas the actual distributions must be taken into account in a model describing reality [185,193,203,217,218].

**iii)** the PCM neglects surface/interface phonons: The PCM progressively loses its relevance when the particle size decreases and the surface [219-225]/interface [220,226] modes (which it does not account for) become preponderant in the signal. Richter et al. were aware of this limitation when they proposed the PCM [180] and Roy et al. simultaneously considered confined bulk modes (PCM description) and surface phonons in CdS/CdSe nanoparticles embedded in glass matrix [223]. The surface modes in ionic crystals become important below ~100 nm [227,228] but can be predicted using a "Dielectric Continuum Approach" (DCA). Surface Optical modes (SO) are expected at wavenumbers $\bar{v}_{SO}$ in the intermediate region between the TO and LO modes, which splitting is a consequence of the long range Coulomb interaction. In spherical crystals of Blende type semiconductors [224,227,229]:

$$\bar{v}_{SO} = \sqrt{\frac{\ell+1}{\ell} \frac{\bar{v}_{TO}^2 + \frac{\varepsilon_\infty}{\varepsilon_M} \bar{v}_{LO}^2}{\varepsilon_\infty / \varepsilon_M}}$$  \hspace{1cm} (14)$$

In Eq. (14), $\ell = 1, 2, 3 \ldots$, $\varepsilon_\infty$ is the high frequency dielectric constant of the semiconductor and $\varepsilon_M$ is the frequency-independent dielectric constant of the surrounding medium. The radial dependence of surface modes is in the $r^{\ell+1}$ form and only the $\ell = 1$ surface mode (the so-called Fröhlich mode), with its constant amplitude, is thus expected to make a significant contribution. Surface optical modes were similarly described for semiconductors of the Wurtzite type [226] and metals [230]. Surface/Interface modes for the specific geometries of nanocylinders and nanowires [222], spherically capped QDs/Quantum Wells (QWs) [231] and Multiple QWs (MQWs) [232,233] have also been addressed.

**iv)** the confinement function has limited physical meaning: Most critics formulated against the PCM concerned the arbitrariness of the confinement function. As a matter of fact, the PCM only is a phenomenological tool and even its best advocates acknowledge it cannot be expected to fully account for the lineshape when it relies on propagating phonons ("bulk" dispersions curves) to describe confined modes. Alternative and more "physical" descriptions of optical modes confined in nanocrystals were mostly proposed by semiconductor specialists. First, it was predicted [234] and confirmed experimentally for PbS [235] that TO and LO modes couple with each other in nanocrystals. Besides, the dipoles generated in polar semiconductors by optical vibrations generate electromagnetic fields and interact with electrons (polarons) or electron-hole pairs (excitons). This so-called Fröhlich interaction is weak in single crystals but leads to a strong resonance of LO and SO modes in confined
semiconductors: quantum dots, wires and superlattices [196,220,224,234,236-240]). Pusep et al. tried to adapt the PCM to the electron-LO coupling in doped semiconductors [241] but accurate descriptions require continuous approaches like the one proposed by Roca, Trallero-Giner and Cardona [234], later improved by Vasilevskiiy and co-workers [242]. Note that in conducting/coloured nanomaterials (carbon, conducting polymers, etc) and superlattices, a Fano coupling is possible between the continuum of electronic states and the discrete energy levels of the phonons [212,243-246].

3.3.2 → The Elastic Sphere Model (ESM)

The use of bulk dispersion curves is questionable when there is a lot of reduction in particle size [9,238]. Meyer et al. used Molecular Dynamics Simulations to calculate the nanoparticle Vibrational Density Of States (VDOS) and demonstrated the importance of grain boundary-related contributions [247]. An alternative to considering the vibrations as ensuing from a disturbed infinite crystal (what the PCM does) is to adopt a first principle description of vibrations in a free sphere. This problem was theoretically discussed in 1882 by Lamb [248]. A brief description will be given but detailed information can be found elsewhere (with a broad spectrum of notations) [249-257]. Imagine a sphere of radius R with vector \( \mathbf{u}(M,t) \) as the displacement field induced by propagating waves at a given point (\( M \)) and for a given time (t). Assuming the sphere is homogeneous (constant density \( \rho \)) and elastic, then elastodynamics theory commands the waves to satisfy the general Navier equation:

\[
\ddot{\mathbf{u}} = \left( \frac{\lambda + 2\mu}{\rho} \right) \nabla (\nabla \cdot \mathbf{u}) - \frac{\mu}{\rho} \nabla \times (\nabla \times \mathbf{u}) = \nabla^2 \nabla (\nabla \cdot \mathbf{u}) - \nabla^2 \nabla \times (\nabla \times \mathbf{u}) = \left( \nabla^2 \mathbf{u} - \nabla^2 \mathbf{u} \right) + \nabla^2 \Delta \mathbf{u} \quad (15)
\]

In Eq. (15), \( \ddot{\mathbf{u}} \) represents the second time derivative of vector \( \mathbf{u} \), \( \lambda \) and \( \mu \) are the so-called Lamé coefficients characterizing the bulk mechanical properties\(^{11} \) while \( v_L \) and \( v_T \) are respectively the longitudinal and transverse sound propagation velocities. A general law states that a scalar potential \( \phi \) and a 2-component vector potential \( \psi \) exist with which \( \mathbf{u} \) can be expressed as the sum of one irrotational (\( \mathbf{u}_1 \)) and two divergence-free (\( \mathbf{u}_2 \) and \( \mathbf{u}_3 \)) components:

\[
\Phi = \frac{1}{\hbar} j_l (k_l r) Y_l^m (\theta, \phi) e^{i\omega t} \quad ; \quad k_L = \frac{2\pi n}{v_L}
\]

\[
\psi = \frac{1}{k} j_l (k_l r) Y_l^m (\theta, \phi) e^{i\omega t} \quad ; \quad k_T = \frac{2\pi n}{v_T}
\]

\[
\mathbf{u}_1 = \nabla \Phi
\]

\[
\mathbf{u}_2 = \nabla \times (\mathbf{r} \nabla \psi)
\]

\[
\mathbf{u}_3 = k_T \nabla \times (\mathbf{r} \nabla \psi)
\]

In Eq. (16) and (17), \( j_l \) are spherical Bessel functions of the first kind and \( Y_l^m \) are the usual spherical harmonics. The radial quantum number \( n \) indicates the mode order (\( n=0 \) for surface modes [250,258]) while the orbital quantum number \( l \) and its z-axis component \( m \) (-\( l \leq m \leq +l \)) define the symmetry of the vibrations and the number of nodal surfaces\(^{12} \). \( \phi \) governs

\(^{11} \) They are related to Young’s Modulus (\( E \)) and Poisson’s Ratio (\( \sigma \)) via the following relations:

\[
\lambda = \frac{\sigma E}{(1+\sigma)(1-\sigma)} \quad ; \quad \mu = \frac{E}{2(1+\sigma)}
\]

\(^{12} \) Duval et al. added a forth parameter -the polarization index \( p \)-, to distinguish spheroidal modes from torsional ones [259].
longitudinal (compressive) waves (P-waves in seismology) whereas $\Psi$ is associated with transverse (shear) waves (S-waves in seismology). For convenience, replace the vector base classically used in problems with spherical symmetry (Figure 7-a) by the following one:

\[
\begin{align*}
\vec{e}_{\text{lm}}(\theta, \varphi) &= Y^m_l(\theta, \varphi)\vec{e}_r, \\
\vec{n}_{\text{lm}}(\theta, \varphi) &= r\nabla Y^m_l(\theta, \varphi), \\
\vec{m}_{\text{lm}}(\theta, \varphi) &= \vec{e}_r \times \vec{n}_{\text{lm}}(\theta, \varphi)
\end{align*}
\]

In this new base, Eq. (18) to (20) can be rewritten as follows (the prime indicates differentiation with respect to $r$):

\[
\begin{align*}
u_i &= j_i\left(k_{\text{L}}r\right)\vec{e}_{\text{lm}}(\theta, \varphi) + \frac{j_i\left(k_{\text{L}}r\right)}{k_{\text{L}}r}\vec{n}_{\text{lm}}(\theta, \varphi), \\
u_2 &= (1+1)\frac{j_1\left(k_{\text{L}}r\right)}{k_{\text{L}}r}\vec{e}_{\text{lm}}(\theta, \varphi) + \left(\frac{j_1\left(k_{\text{L}}r\right)}{k_{\text{L}}r} + j_1\left(k_{\text{L}}r\right)\right)\vec{n}_{\text{lm}}(\theta, \varphi), \\
u_3 &= -j_1\left(k_{\text{L}}r\right)\times \vec{m}_{\text{lm}}(\theta, \varphi)
\end{align*}
\]

A distinction is now possible between two families of modes (see Figure 7-b&c):

Modes with purely radial displacement ($u_3 = 0$) are called spheroidal modes. Modes with purely tangential displacement ($u_1 = u_2 = 0$), occurring with no volume change, are called torsional modes.

**Figure 7**: a) Description of one nanoparticle in the Elastic Sphere Model (ESM) – b) Oscillation of a free sphere in one spheroidal mode – c) Oscillation of a free sphere in one torsional mode.

Duval was the first to establish the selection rules for the ESM [260]. Since the modes irreducible representations had to coincide with those of the sphere group, he showed that only purely spherical (irreducible representation $D_8^{(0)}$) and quadrupolar (D$D_8^{(2)}$) spheroidal

---

13 Duval et al. added a forth parameter -the polarization index $p$-, to distinguish spheroidal modes from torsional ones [259].
modes are Raman active (while all torsional modes are forbidden)\textsuperscript{14}. Their relative intensity is
terminal but only the first order "surface" ones, those shown in Figure 8, have significant
contributions [258,261-263]. Their identification is easy since only $D_{g}^{(0)}$ is polarized (parallel
polarization). An expression for the stress field can be derived from Equations (24) to (26)
and the subsequent application of stress free boundary conditions for $r=R$ eventually yields
the vibration eigenfrequencies $\nu_{n}$\textsuperscript{15}. For $l=0$ spheroidal modes, a good approximation of $\nu_{n}$ is
given by [257]:

$$\nu_{n} = \frac{\nu_{L}}{R} \left( \left( n+1 \right) \pi - \arcsin \frac{4}{\left( n+1 \right) \pi} \left( \frac{\nu_{T}}{\nu_{L}} \right)^{2} \right)$$

(27)

No analytic solutions can be obtained for the other modes, which have to be calculated
numerically, but the wavenumbers are always proportional to $R^{-1}$ (see Figure 8):

$$R = \frac{\nu_{L}}{c \nu_{L}^{(i)}}$$

(28)

$$R = \frac{\nu_{L}^{(i)}}{c \nu_{L}^{(i)}}$$

(29)

\textbf{Figure 8 :} Size dependence of the $D_{g}^{(0)}$ and $D_{g}^{(2)}$ modes in PbSe quantum dots. Reprinted
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\textsuperscript{14}In group theory, $D_{i}^{(j)}$ notation indicates modes of $(2j+1)$ degeneracy with either symmetry ($i=g$) or antisymmetry ($i=u$) with
respect to an inversion centre.

\textsuperscript{15} Some authors added electromagnetic continuity as a grain boundary condition [234,242].
In Eq. (28) and (29), $c$ is the light speed in vacuum while $A$ and $A'$ are dimensionless constants. These equations were used to measure the radius of silver clusters in ancient and advanced materials\(^{16}\) [264-267] or particles size in cordierite [262], TiO$_2$ [268-270], silicon [271,272], PbSe [273], etc. Note that the scattering efficiency of the particles scales like $\nu^{-3}$ [261]. Consequently, directly applying Eq. (28) and (29) when size is distributed will lead to an overestimation of $R_{\text{ave}}$. Besides, the ESM assumes the nanoparticles are homogeneous and only modes with $\lambda$ much greater than the interatomic distance, mostly the low energy fundamental and 1$^{\text{st}}$ harmonic modes, are described [259]. On account of that restriction, the ESM is often referred to as a predicting model for "confined acoustic modes", although optic phonons were occasionally studied using the same model [274].

Just like for the PCM, the use of the ESM for grain size determination comes with certain approximations. As is, the model strictly applies to equal size, "free-standing", isotropic spheres. The triple degeneracy of $D_g^{(2)}$ mode is lifted for ellipsoidal particles [260,275] and Hernandez-Rosas et al. recently proposed a generalised model for oblate spheroids [276]. Like for the PCM, it is also possible to include the size distribution [218,265,277,278] and the problem of anisotropic materials was discussed by Murray et al. [279]. It had been previously dealt with by Fujii et al. who tried calculations based on the longitudinal and transversal sound velocities for the main crystallographic directions of silicon but they found no agreement with their experimental results [271].

It has been assumed for a long time that the ESM held in matrices with Lamé coefficients sufficiently different from those of the nanospheres [280,281], but the presence of a matrix also activates a torsional surface mode (l=1) which eventually dominates the spectra [260,280,281]. Moreover, some couplings of the Raman active modes with matrix vibrations can be expected [250-252,256,277,279-282], knowing that the smaller the nanoparticles, the stronger the coupling [251,257]. They were modelled by a "Complex Frequency Method" (CFM) [259,279]. If the nanoparticles are in relatively high concentration, which will surely be the case in active devices like QDs networks, a collective Fröhlich Mode will also contribute to the Raman spectrum [283].

### 3.3.3 → Validity Domains of the PCM and the ESM

Figure 9 illustrates the different approaches to the RS of nanoparticles. In grains much larger than the wavelength, phonons propagate almost in the same way as in perfect "infinite" crystals. The only perturbation then comes from vibrations involving the outer atomic layers, which do not meet the bulk conditions [37,80,196]. The structural transition between the surface and the bulk of each grain obviously is progressive but let us assume, for simplicity, that there is an homogeneous surface shell of definite thickness $t$. Figure 9-a then shows how the skin to bulk volume ratio reaches a critical value for $D/t \sim 5$, where $D$ is the grain diameter. When the grain size further decreases, the confinement of optic modes begins and the PCM starts applying. Soon, the relative proportion of "non-bulk" skin and surface modes increases and, below a certain size, the very notion of collective vibrations disappears. As a principle, the ESM must then be considered but there is no clear-cut grain dimension for which one

\(^{16}\) Most authors only considered Ag$^0$ [264] but clusters integrating Ag$^+$ ions are rather expected in a iono-covalent matrix (there are Ag$^+$ ions at the surface of the clusters formed in oxides fired at high temperatures [4]). Analysis with different excitations should reduce Ag$^+$ contribution through metallic silver exaltation.
should switch from the PCM to the ESM. They do not necessarily exclude each other and, on occasion, were even used simultaneously [204,255,284,285].

**i)** The PCM should be applicable between the grain size at which "bulk" dispersion curves lose all significance (~5nm [206,238]) and a high-end value where confinement has no effect on the spectrum, which will obviously depend on the mode dispersion around BZc [40,193,197,285]. Note that surface modes add a significant contribution for grain sizes up to 8 nm in SnO$_2$ [286] and even 20 nm in ZrO$_2$ [287].

**ii)** The typical grain size below which nanocrystals can not be assumed homogeneous and the ESM therefore no longer applies [250] is between 1 [266] and 5 [259,285,288] nanometers, which is in good agreement with the ~40 interatomic distances predicted by Wittmer *et al.* [289]. Note if particles with a size slightly above this limit are embedded in a glass phase, the "so-called" boson peak of the matrix (see § 4.1) may hide the free vibrations described by the ESM, unless wave-guided spectroscopy is used [266]. There is no theoretical upper limit to ESM applicability but the low frequency modes gradually enter the Rayleigh wing (quasi-elastic diffusion; see § 2.2) as size go increasing and become unusable for a value that depends on both the material and the experimental resolution of the spectrometer [255,290].

![Diagram](Figure 9 : a) The "surface to bulk" volume ratio in nanospheres of diameter D and constant "skin thickness" t (see text) - b) Applicability range of the different descriptions for the vibrations of spherical crystals (ESM = Elastic Sphere Model ; PCM = Phonon Confinement Model). The grain size values are indicative and actual limits depend on the material.)
One should not forget that peak altering effects like internal stress\textsuperscript{17} [9,185,187,216,217,219,292], growth directionality [81], non-stoichiometry [186], local heating [190,222,293], couplings or defect-induced diffusions [293] may add to the size effect on Raman spectra of nanomaterials. The stress will act on the position of the peaks [187], defects (non-stoichiometry for instance) will widen them [186,187,190] and temperature will act on both position and width. Falkovsky and Camassel wrote a short review on the contribution of all kinds of defects to optical peaks widening [294].

4. SELECTED CASE STUDIES

4.1 The Structural Variety of Glass Ceramics


Ceramics and glass-ceramics obtained from liquid precursors (molten glass and salts, solutions, gels, organic precursors [1,295-297]) form a large range of nanophased materials. The transition from the liquid to the solid state "freezes" a local steric disorder and thermal annealing is necessary for long distance Coulombian interactions to stabilize the

\textsuperscript{17} Residual stresses are unavoidable, even in free particles (the reduction of the surface atoms coordination number reduces the bond lengths [291]). They were investigated in detail by Gomonnai et al. [219] and Sirenko et al. [9].
thermodynamically stable crystalline phase. In these materials, strongly covalent species like the SiO$_4^{4-}$ or PO$_4^{3-}$ tetrahedra often "see" a site symmetry different from the average one predicted by crystallographic study [297,298]. For instance, Figure 10-a compares the Raman spectrum of a 2GeO$_2$-Al$_2$O$_3$~2H$_2$O gel prepared through alkoxides hydrolysis-polycondensation with those of the phases obtained after thermal treatment up to 1450°C [299]. The intermediate Al$_2$Ge$_2$O$_7$ phase (stable from 1250 to 1300°C) has low symmetry monoclinic structure but fine low frequency Raman peaks, characteristic of an ordered compound, while the spectrum of crystalline mullite is as broad as that of the glass, in spite of a higher symmetry orthorhombic structure. This relates to an orientational disorder induced by oxygen vacancies in the AlO$_4$ tetrahedra. Moreover, since the occurrence of broadening indicates distorted entities, it is obvious from the figure that GeO$_4$ tetrahedra as well as GeO$_6$ octahedra are more distorted in the mesoporous glass than in the gel phase [299]. In the example of the perovskite-related niobiates from Figure 10-b, Nb-O modes around 800 cm$^{-1}$ split because of oxygen vacancies in the NbO$_6$ octahedra. The (T', R') modes involving the Ba atoms located at the corners of the unit-cell are not affected by these vacancies in Ba$_6$Nb$_2$O$_{11}$ (hence the fine peaks) but split in Ba$_4$Ca$_2$Nb$_2$O$_{11}$ because chemical and mass decoupling isolate Ba and Ca sub-lattices [300]. The same kind of vibrational decoupling with defects has been observed for many silicates [297,298,301].

Two silicate spectra are shown in Figure 11-a&b. Most types of glass contain nanometric crystallites and the spectrum of silicates (SiO$_2$ tetrahedral network) is intermediate between that of a disordered network and the superposition of contributions from definite vibrational
entities: tetrahedra rings in vitreous silica (the narrow defect bands in Figure 11-a originate from the vibrations of 3-fold (D_2) and 4-fold (D_1) rings [302-305]) and complex arrangements of SiO_4 tetrahedra in alkali/earth-alkali silicates [302]. The deformation (\(\delta_{\text{Si-O-Si}} \sim 500 \text{ cm}^{-1}\)) and elongation (\(\nu_{\text{Si-O}} \sim 800-1200 \text{ cm}^{-1}\)) modes depend on the connectivity of the SiO_4 tetrahedra and can be fitted with components called \(Q_n\) and \(Q_{n'}\), respectively (n represents the number of Si-O-Si bridges per tetrahedron) [306-308]. The position and area of these components then constitute characteristic parameters of silicate glass nanostructures and can be used for garnering additional information such as the original composition or the sintering temperature [306,307].

The most specific part of glass spectra is a contribution peaking at \(\sim 50-100 \text{ cm}^{-1}\), which is called the Boson Peak (BP) because its intensity obeys Bose-Einstein distribution. Since F function from Eq. (N3) never descends to zero in amorphous materials, their VDOS \(G(\nu)\) is fully active and Raman intensity is given by [309]:

\[
I(\nu) = \frac{n^2(\nu + 1)}{\nu^2} C(\nu) G(\nu)
\]

(30)

The BP mostly originates from the probe-excitation coupling function \(C(\nu)\), the reason why it best shows on \(I/[\nu(n^2(\nu+1))]\) "reduced intensity" curves. There is an ongoing debate to ascertain whether the extra vibrations from the BP correspond to propagating or localized modes but all interpretations make the BP a way of characterizing glass intermediate range order at the nanometer scale:

**i)** Some teams believe that collective acoustic waves are possible in glass, even at very low frequencies, but that the transverse acoustic branch is flattened [310-312]. Yet, \(C(\nu)\) is expected to scale as \(\nu^2\) for slightly distorted plane-wave vibrations [313] when Surotsev and Sokolov demonstrated experimentally that glasses rather exhibit the following behavior [314]:

\[
C(\nu) = A \times \left( \frac{\nu}{\nu_{\text{BP}}} + B \right)
\]

(31)

**ii)** Duval *et al.* explain the change in the VDOS by elastic constants fluctuations in the random non-continuous structure of the glass [319]. In this scheme, amorphous regions whose only difference lies in the strength of their bonds coexist and the denser ones (referred to as "blobs") confine the vibrations. Surotsev recently improved the model by taking into account the contact between the "blobs" instead of considering a separation by soft matter [321]. This refinement introduces some diffusive character to the BP.

---

18 Note that the spectrum does not strictly identify with the VDOS. Moreover, by comparison with Eq. (N2), \(C(\nu)G(\nu)\) is analogous to the conductivity of the material. Quasi-Elastic and Inelastic Neutron Scattering also give insight into the frequency dependence of conductivity through the \(\nu \propto \sigma(\nu)\) function (Chap. 21, 23, 25 and 30 in Ref. [54]).

19 If one assumes, following the standard Debye model for acoustic branches, that \(G(\nu)\) is proportional to \(\nu^2\), then the reduced intensity is expected to be proportional to \(C(\nu)\) (see Eq. (30)).

20 Slopes different from 2 on Log-Log scale plots of \(C(\nu)\) were tentatively explained by the fractal nature of the tetrahedral network in gel-derived silica glass (silica aerogels) [313,315-318].

21 The once popular model from Martin and Brenig attributed the activation of Raman acoustic modes to density fluctuations modelled with a phenomenological Gaussian function [320].
iii) The Soft Potential Model (SPM) considers the extra vibrations as Quazi-Localized Vibrations (QLVs) that resonate with sonic waves. These QLVs are vibrations created by disorder (or, possibly, low lying optical modes) that concern all atoms but with only a small group of them vibrating with significant amplitude. The model was recently improved by Gurevich et al. who introduced anharmonic effects [322].

4.2 Analysis of Localized Species and Sublattices

Features from μRS can be specific to localized vibrations of weakly bonded or light species like, for instance, $S_2^-$ ions entrapped in Lapis Lazuli [61]. In Bi2201 and Bi2212 bismuth cuprates, some modes are characteristic of the atom to which oxygen is bonded [323] while the activation of forbidden modes is related to the order of the mobile oxygens [324,325]. Similarly, Figure 12 shows how polyaniline polymerisation produces little spectral modifications [88] while the orientational medium range disorder induced by the grafting (for protonic conduction) of sulfonic groups on the PTFE framework of Nafion™ polymer membranes produces obvious effects below 400 cm$^{-1}$ [326].

![Figure 12](image_url)

**Figure 12**: a) Comparison between the spectra from polyaniline precursor monomer ($\sim$1 nm) and polyaniline in one emeraldine base form ($\sim$ 200 nm) (Adapted from S. Folch et al., Macromol., 32, 3080, 1999) – b) Comparison of PTFE and Nafion (PTFE-grafted with sulfonic groups) Raman spectra (Adapted from A. Gruger et al., Vibr. Spectr., 26, 215, 2001).

In fact, μRS is very sensitive to sublattices in those many structures built with vibrationally independent species. Whenever the sublattices have chemical independence (e.g. iono-covalent silicate or phosphate frameworks hosting alkali ions), they give independent Raman
contributions. If these contributions are taken apart by mass discrepancy, defects from either sublattice, for instance the cation and oxygen sublattices of perovskites, can be analysed separately [300,327,328]. The short distance cationic order in ZrTiO$_4$ [92,191] has also been investigated by RS but one of the best examples of sublattice discrimination remains ionic conductors 22. For instance, Figure 13 shows how a good energetic gap makes it possible to separate the short range ordered domains of conducting ions in β-alumina (a superionic solid selected in the seventies as a potential electrolyte): Ag$^+$ sub-lattice melts around 200K whereas alumina host lattice is stable up to 2000K [56,329,330]. Because of their light weight and high polarisability, protonic species exhibit particularly interesting dynamics, their vibrations being often independent from the host lattice (modes are localized and weakly coupled with the others) [54,331].

Figure 13 (Adapted from Ph. Colomban et al., J. Chem. Phys., 75[3], pp 1388-1399, 1981) a) The ~25 cm$^{-1}$ peak of β-alumina is characteristic of the conducting short range ordered Ag$^+$ bi-dimensional sub-lattice - b) The half-width of the peak makes it possible to identify the melting temperature of the sub-lattice.

4.3 Carbon Allotropy

The technique of µRS has been widely used to study carbon allotropes (diamond, graphite, fullerenes, nanotubes ...). It is indeed one of the few techniques sensitive to the full range of structural states present in this class of materials, from perfectly crystalline to amorphous. The common crystalline phases of carbon yield very simple spectra: diamond (sp$^3$ hybridisation) peaks at 1332 cm$^{-1}$ (single mode of T$_{2g}$ symmetry) whereas graphite (sp$^2$ hybridisation) has doubly degenerate E$_{2g}$ modes at 42 and 1582 cm$^{-1}$. The latter is referred to as G band and corresponds to vibrations in the graphene planes (which crystalline quality can be measured by the width of G band [169]) whereas the former corresponds to weak interplanar Van der Waals interactions (the reason for its low energy). Two additional modes appear whenever flaws are created, grain size is reduced or graphene planes are curved [169] (Figure 14-a).

22 In ionic conductors, mobile ions are weakly bonded, which will add to mass contrast in distributing the vibrational energies
These modes are called D and D’ (the letter stands for "disorder"). D’ results from the splitting of G band and peaks around 1620 cm$^{-1}$, at the value where the dispersion curve of graphite is the flattest. The intensity ratio of G to D’ depends on the proportion of distorted graphene planes [332]. Assuming Raman scattering efficiencies $\sigma$ are system-independent, then the number $n$ of consecutive graphene planes should obey the following law [332]:

$$\frac{I_G}{I_{D'}} = \left( \frac{n-2}{2} \right) \frac{\sigma_G}{\sigma_{D'}}$$

(32)

The interpretation of D band has been much debated. Despite its proximity to the diamond peak, D is derived from graphite (the very low efficiency of diamond scattering would otherwise make it much weaker). In 2000, Ferrari and Robertson suggested that D band resulted from a resonant enhancement of the modes from graphite dispersion curves having the same wavevector $k$ as the exciting photons [189]. This assignment provided an explanation for some peculiar features of D band, such as the excitation dependence of its wavenumber (Figure 14-a), but remained unsatisfying. Thomsen et al. showed that an unusually enhanced double resonance mechanism was at play for D band [333].

Figure 14: a) Raman spectra of the carbon nanoparticles in Hi-S Nicalon SiC fibres (Nippon Carbon) as a function of the laser excitation wavelength $\lambda$. (Adapted from G. Gouadec et al., Comp. Sci. Techn., 62, pp 505-511, 2002) - b) Tuinstra and Konig's calibration (Eq. (33)) was used to build a 2D “map” of carbon grain size in a SA3 SiC fibre (Ube Ind.). This is called "smart mapping" [39,213,215,334]. Reproduced with permission from "Raman Analyses and Smart Imaging of Nanophases and Nanosized Materials", Ph. Colomban, Spectroscopy Europe, 15[6], pp 8-16, 2003. Copyright John Wiley & Sons Ltd.

Whatever the exact nature of D band, it was soon shown that it depended on carbon grain size, a feature for which an empirical law was proposed in 1970 by Tuinstra and Koenig [200]:

$$\frac{I_{D'}}{I_{G_{514.5}}} = \frac{C(\lambda)}{L_g(nm)}$$

(33)

This calibration is not valid below 2 nm [189].
The so-called "Tuinstra and Konig" calibration has been used extensively for the "qualitative" control of carbon structural transformations, mostly in amorphous carbon [335,336] and Diamond-Like Carbon (DLC) [337-343] films but also on radial cross sections in carbon micro-rods [344] and electrodes [345]. A direct proportionality between $I_D/I_G$ ratio and the $sp^3$ content, as obtained from EELS experiments, has been reported in amorphous carbon films [346].

In 1985, Kroto et al. were the first to find experimental evidence of crystalline forms of carbon other than diamond and graphite [347]. These corresponded to an assembling of pentagonal, hexagonal and heptagonal carbon rings to form spheroids (fullerenes) [348]. Crystallization by closing of rolled graphene planes is also possible, in which case nanotubes (NTs) are formed [349]. These NTs have enormous application potential as they are among the hardest known material and are able to conduct single charges unidirectionally [350]. Figure 15-a shows how one \{n,m\} couple of integers is sufficient to fully characterize a NT. This tube is obtained by the rolling of the chiral vector $\vec{c} = n\vec{a}_1 + m\vec{a}_2$ in a graphene plane and its diameter $d_{NT}$ and chiral angle $\theta$ are simply given by:

$$d_{NT} = \frac{\|\vec{c}\|}{\pi} = \frac{l_b}{\pi} \frac{\sqrt{3}n^2 + m^2 + nm}{\pi}$$

$$\theta = \arcsin \left( \frac{m\sqrt{3}}{2\sqrt{n^2 + m^2 + nm}} \right)$$

Figure 15-b shows the Raman spectra of some Double Walled CNTs (DWCNTs). The bond angles and lengths no longer correspond to a perfect $sp^2$ hybridisation but Raman modes can still be derived from graphite dispersion curves [351,352]. Eklund et al. showed G wavenumber remains at 1581 cm$^{-1}$ in NTs with radii above 15nm but drops to 1465 cm$^{-1}$ below [353].

![Diagram](image)

**Figure 15**: a) Nanotubes can be described by the rolling of a chiral vector $\vec{c} = n\vec{a}_1 + m\vec{a}_2$ in a graphene plane – b) Raman spectra of Double Wall Carbon Nanotubes (DWCNTs) filled with PbI$_2$. Reprinted with permission from Puech et al., Phys. Rev. B72, 155436, 2005. Copyright 2005 by the American Physical Society.
It should be noted that the Radial Breathing Mode (RBM) shown in Figure 15-b can be used to measure $d_{NT}$ accurately [354]. Based on a zone folding model, Eklund et al. [353] predicted the relationship between $\nu_{RBM}$ and $d_{NT}$, which was calibrated afterwards [355-358]:

$$d_{NT} \text{ (nm)} = \frac{223.75}{\nu_{RBM} \text{ (cm}^{-1})}$$

(36)

NTs with different $\{n,m\}$ may be similar in diameter but they will resonate for different laser energies [359,360]. These energies correspond to interband transitions between the valence and conduction band at Van Hove singularities. The relationship has been established and $\{n,m\}$ can then be precisely found on the basis of $\mu$RS [361]. This is interesting because $\{n,m\}$ is determinant for many properties. For instance, nanotubes with $|n-m|=3q$ (q integer) are metallic whereas those for which $|n-m|=3q\pm1$ are semiconductors [362]. The behaviour of the D [363,364], G [365] or $D^*$ [364] bands has also been studied extensively. References [351] and [352] provide thorough descriptions of the RS of CNTs.

### 4.4 Nanophased SiC Fibres

SiC fibres, which are among the most stable inorganic fibres, are mostly produced by the 3D reticulation of a polymeric precursor[25]. Their nano-crystalline structure offers the best compromise between a good homogeneity (a characteristics of the amorphous state) and a high bond density (a characteristics of the crystalline state). Their very smooth surface and the lack of defects explain tensile strengths $\sigma_r$ as high as 3 GPa. These fibres are designed to reinforce composites working at very high temperatures (~1200-1400°C) in oxidizing and corrosive atmospheres (carbon fibres oxidize at 500°C whereas alumina, zirconia and mullite fibres properties degrade above 1100-1200°C [366] as they crystallise).

Micro-Raman spectroscopy is particularly well suited to study SiC fibres because it gives a good signal for both SiC and the secondary carbon phase. Figure 16-a illustrates this fact with SiC decarburation in NLM fibres submitted to alkaline corrosion. First, the different forms of partially oxidised or nitrided carbon can be identified [23]. As for SiC spectrum, it mainly consists of peaks around 795 and 970 cm$^{-1}$. They correspond respectively to the transverse optical (TO$_1$ and TO$_2$; degenerate) and longitudinal optical (LO) modes of $\beta$-SiC[26], which X-ray diffraction identified as the phase present in Nicalon (NLM, Hi & Hi-S) [370], SA [371] and Sylramic [372] fibres. Additional bands correspond to SiC polytypism (see Figure 17: Brillouin Zone folding generates satellite lines on the low energy side of TO and LO bands [213,214,373-378]), amorphous SiC (broad symmetric background) and asymmetric VDOS projections when "random" faulting in the stacking sequence folds BZ in countless ways [373].

---

24 $D^*$ is the overtone of D-band. It is alternatively referred to as $G'$ by analogy with a second order band found in disordered graphite (see Figure 21).

25 The main alternative is Chemical Vapour Deposition (CVD) of SiC on a carbon fibre core (SCS-6 fibre from Textron).

26 In SiC structures, Si and C "bilayers" are referred to as "h" if they are deduced from the underlying bilayer by a simple translation. However, if an additional 180° rotation (around the Si-C bonds linking the bilayers) is required for superposition, then bilayers are referred to as "k". Each periodic stacking sequence defines a polytype which is classified according to Ramsdell notation by first giving the number N of bilayers in the stacking cell and then the cell type [367-369]. The "all k" polytype ($\beta$-SiC phase) is the 3C (cubic) polytype. All other polytypes ($\alpha$-SiC phase) are either NH (hexagonal) or NR (rhombohedral).
Figure 16: a) Effect of alkaline corrosion by NaNO₃ salt on the Raman spectrum of annealed NLM SiC fibres (λ_laser=457.94nm). Note the core spectrum was recorded on a fibre cross-section which has been exposed to corrosion (Adapted from Ph. Colomban et al., Materials and Corrosion, 53[5], pp 306-315, 2002) - b) Raman spectra recorded with 632.1nm excitation on one NLM SiC fibre annealed for 10hr, at 1600°C, under reducing atmosphere. The fit was obtained using the PCM [213,214] and a:SiC stands for "amorphous" silicon carbide – c) High Resolution Transmission Electron Microscopy (HRTEM) micrograph of one NLM fibre, after 10 hr reducing annealing at 1600°C [210]. The picture shows one SiC nanocrystal embedded in amorphous SiC (Courtesy of M. Havel & L. Mazerolles).

SiC contributions from the spectra in Figure 16-b were fitted according to the PCM (see §3.3.1). This returned "coherence lengths" of 6.5±1.2 nm (TO) or 3.8±0.9 nm (LO), in good agreement with the size of SiC polytype domains appearing in Figure 16-c. We performed
similar fits on spectra of Hi-S, SA and Sylramic nearly stoichiometric 3rd generation SiC fibres [379], obtained from grafted polycarbosilane [371,380-383]. Only the Hi-S bands could not be adjusted at $k_0=0$, indicating a greater stacking disorder. The coherence length was higher for Sylramic and SA fibres, in agreement with a higher grain size (100-500 [381] and 200 [384] nm, respectively, against 20 nm in the Hi-S [380]).

![Dispersion curves for the 3C, 2H and 4H polytypes, in equivalent directions of the reciprocal space. The "extended Brillouin zone" obtained by unfolding hexagonal (or rhombohedral) polytypes curves matches the "standard zone" of 3C SiC [245,385]. 3C-SiC modes marked with open circle are inactive but can be measured on the Raman spectra of 2H polytype (black circles) where they correspond to BZc.](image)

**Figure 17**: Dispersion curves for the 3C, 2H and 4H polytypes, in equivalent directions of the reciprocal space. The "extended Brillouin zone" obtained by unfolding hexagonal (or rhombohedral) polytypes curves matches the "standard zone" of 3C SiC [245,385]. 3C-SiC modes marked with open circle are inactive but can be measured on the Raman spectra of 2H polytype (black circles) where they correspond to BZc.

4.5 CeO$_2$

The electrical properties and chemical reactivity of nano-crystalline CeO$_2$ make it interesting for applications such as gas sensor, fuel cells electrolyte material, catalyst for oxygen storage, etc [154,197,216]. Ceria only first order Raman active mode is the triply degenerate symmetrical stretching vibration of the CeO$_8$ vibrational unit at $\sim 465$ cm$^{-1}$. Only the oxygen atoms move in this mode [197,216,386], which is therefore very sensitive to the oxygen sublattice disorder resulting from processing and/or grain-size-induced non-stoichiometry. Spanier et al. simultaneously considered phonon confinement, stress, size distribution and non-stoichiometry as possible causes for grain size induced variations of ceria Raman spectra [216]. Figure 6 above showed the influence of grain size on the linewidth for ceria samples prepared on Al$_2$O$_3$ substrates, with a polymer precursor spin-coating process ensuring a remarkably homogeneous grain size distribution [387]. The broadening is obvious on Figure 18-a, which shows PCM-derived fits of Raman spectra [197]. The confinement lengths are plotted in Figure 18-b as a function of the grain size measured by X-ray diffraction: the extension of the homogeneous domains reaches a maximum for grain diameters around 100 nm. Since a direct relationship is expected for the 465 cm$^{-1}$ band with the oxygen sublattice, Kosacki et al. proposed that L corresponded to the average distance between oxygen...
Below 100 nm, the "modelled" correlation length decreases with the grain size following a cubic root law and this can be successfully accounted for by the reduction of vacancy formation enthalpy for nanocrystalline microstructures [197,387].

**Figure 18**: a) Grain size effect on ceria Raman signature. The fits were obtained using the PCM (§ 3.3.1) – b) Comparison of the confinement length L obtained through the PCM with the grain size obtained by X-ray diffraction. Reprinted from Solid State Ionics, 149[1-2], I. Kosacki et al., Raman scattering and lattice defects in nanocrystalline CeO₂ thin films, pp 99-105, 2002, with permission from Elsevier – c) The spectra of gadolinium-doped ceria single crystals highly depend on the doping level (I. Kosacki and Ph. Colomban, Private Communication)

Figure 18-c shows the evidence for the stronger influence of substitutional disorder over the stoichiometric one. The broadening in Gd-substituted CeO₂ is indeed much more important than the one associated with grain size-induced non stoichiometry only (Figure 18-a). A separation of the short-range disorder and size-induced band broadening was similarly achieved for nano-InVO₄ oxide (an electrode material for Li⁺ intercalation) [26,27]. Note all samples in Figure 18-c are single crystals with the same highly symmetric structure. Their X-ray diffractograms would look very much alike and only fine refinements would therefore take them apart.
5. THE MECHANICAL CHARACTERIZATION OF NANOPHASES BY MICRO-RAMAN SPECTROSCOPY

A growing number of devices involve nanophased materials. Hence there is a need for in situ non-destructive characterization methods. We have already seen that µRS nano-sensitivity to chemical bonds (stretching and bending modes) and their spatial arrangement (libration and external modes) makes it a good tool for probing crystallo-chemistry and reactions. We shall now demonstrate how nanoprecipitates can be used as "mechanical probes" [388-393]. In fact, very few experimental techniques lend themselves to micromechanical characterization of heterogeneous materials. Most of them are not specific and all of them have limitations. First, X-rays [394-396] and neutron [397,398] diffractions only work on crystallized samples. Ultrasound analysis gives a dynamical view of cracking rather than stress measurements [399-401], photoelastometry supposes perfect transparency [402,403] and SEM observations of resin grids only give an indirect measure of the surface deformations [404-406]. Other specific methods exist like instrumented (micro-nano)-indentation [407-411], fragmentation [412-417], "pull-out" [418], "push-out" [419] and "microdroplet" [414] tests but the validity of the models used for data interpretation is questionable due to their usually large number of parameters. Besides, these methods are sometimes inapplicable. For instance, carbon fibre-reinforced composites cannot be tested by conventional push-in micro-indentation because the fibres have a small diameter and cleave too easily.

5.1► Raman Stress Sensitivity

5.1.1.► The Anharmonicity of Atomic Bonds

Below, we will assume that each stretching mode is specific to one given chemical bond. As long as elongation is limited, the bond can be modelled by a spring of length $l_b$, reduced mass $\mu$ and constant stiffness $k_b$. This is the so-called harmonic model where the interatomic potential has the form $V(l_b) = \frac{k_b}{2}(l_b - l_0)^2$:

$$V_{\text{vib}} = \frac{1}{2} \frac{k_b}{\mu}$$

(37)

$$k_b = \frac{\partial^2 V}{\partial l_b^2}$$

(38)

There is no $l_b$ dependence for the wavenumber in Eq. (37) and the harmonic potential does not predict any stress sensitivity for Raman bands. Yet such modelling rules out the phenomenon of bond dissociation $(l_b \rightarrow \infty)$ and does not correctly account for atoms non inter-penetrability $(l_b \rightarrow 0)$. In fact, the interaction potential should not be limited to a quadratic term and all real bonds are somewhat anharmonic (Figure 19). They include attractive and repulsive contributions, for which Mie and Grüneisen proposed the following expression, with $A$, $R$, $a$ and $r$ being positive constants [420]:

$$V(l_b) = V_0 + V_{\text{attractive}}(l_b) + V_{\text{repulsive}}(l_b) = V_0 - A \times l_b^{-a} + R \times l_b^{-r}$$

(39)
Table 1: Parameters of Mie-Grüneisen potentials in solids [421].

<table>
<thead>
<tr>
<th>Bonding</th>
<th>a</th>
<th>r</th>
</tr>
</thead>
<tbody>
<tr>
<td>Van der Waals</td>
<td>6</td>
<td>12</td>
</tr>
<tr>
<td>ionic</td>
<td>1</td>
<td>9</td>
</tr>
<tr>
<td>covalent</td>
<td>a+r</td>
<td>~3</td>
</tr>
</tbody>
</table>

In spite of its very significant influence on the physical behaviour of materials (only it can explain thermal expansion or the finite value of thermal conductivity [422]), anharmonicity is often considered as a simple perturbation: in what is referred to as the "quasi-harmonic" approximation, one considers that Eq. (37) and (38) are applicable to real potentials. According to Figure 19, this means atoms are bonded by strings whose stiffness \( \left( \frac{\partial^2 V}{\partial l_b^2} \right) \) increases under compression and decreases under tension.

In the case of the "quasi-harmonic" approximation, Eq. (39) is equivalent to:

\[
\frac{dV_vib}{V_0} = \frac{dk}{2} = \frac{1}{2} \frac{a(a+1)(a+2)A}{r(r+1)(r+2)} R \times l_b^{-(r+3)} \times dl_b
\]

Introducing the bond elongation \( \epsilon_l = (l_b-l_0)/l_0 \), a Taylor expansion of \( l_b^{\epsilon} = l_0^{\epsilon}(1+\epsilon_l)\epsilon_l \) (small strain assumption) and the requirement for the potential first derivative to be nil at \( l_b=l_0 \) yield:

\[
\frac{dV_vib}{V_0} = \frac{(a+r+3)}{2} \times \epsilon_b
\]

\[
V_vib = \frac{V_0}{V_0} \left( 1 - \frac{(a+r+3)}{2} \times \epsilon_b \right)
\]

There is therefore a direct proportionality factor between the wavenumber shift and bond deformation\(^{27}\):

\[
V_vib = V_0 + S_b \times \epsilon_b^{\%}
\]

\(^{27}\) The superscript "\%" will indicate deformation is given as a percentage.
From a macroscopic point of view, a tensile (resp. compressive) stress is expected to decrease (resp. increase) \( \nabla \). The effect will be more significant as the coefficients \( a \) and \( r \) will be high, in other words as the bonds will be weak\(^{28}\).

### 5.1.2. Raman Spectroscopy of Single Crystals under Hydrostatic Compression

Many RS experiments carried on stressed materials concern single crystals hydrostatically compressed in diamond anvil cells (DACs), where the pressure \( P_h \) is transmitted by a fluid [424-426]. Wavenumbers then obey quasi-linear dependencies to \( P_h \) [367,427-430]:

\[
\nabla_{\text{vib}} = \nabla_0 + a P_h + b P_h^3 \sim \nabla_0 + a' P_h
\]

Such a behaviour indicates an equivalency between the macroscopic (Eq. (44)) and microscopic (Eq. (43)) responses to external solicitations. DAC experiments are usually used to measure the Grüneisen parameters of Raman modes [367,427-429,431-434]:

\[
\gamma_m = -\frac{\partial \log \nu_m}{\partial \log V} = \frac{1}{\beta_T} \frac{\partial \log \nabla_m}{\partial \rho}
\]

In Eq. (45), \( V \) is the volume and \( \beta_T \) the isothermal compressibility. \( \gamma_m \) is almost independent of the mode in isotropic solids with one kind of bond controlling the lattice dynamics. This is the case for covalent/ionic-covalent materials like diamond and 3D semiconductors from groups IV and III-V, where \( \gamma \) is close to 1 [424,425]. It becomes about 2 in II-VI semiconductors and rises to 3 in alkali halides crystals [425]. In molecular crystals, \( \gamma \) often changes from one mode to another [424] with, usually, \( \gamma_{\text{internal modes}} \ll \gamma_{\text{external modes}} \).

In an isotropic material under hydrostatic compression:

\[
P_h = \frac{dV}{V_0} = 3 \varepsilon_i
\]

The combination of equations (41), (45) and (46) then leads to:

\[
\gamma = \frac{a + r + 3}{6}
\]

The Grüneisen parameter then becomes a direct characteristic of interatomic potentials (\( a \) and \( r \) parameters were introduced in Eq. (39)).

### 5.1.3. Raman Spectroscopy of Single Crystals under General Stress

If a deformation is applied to a single crystal, vibrational mode independence is lost and phonon-phonon couplings occur [435]. The fundamental equation of Dynamics then becomes:

---

\(^{28}\) The anharmonicity of the bonding potential is referred to as a "mechanical anharmonicity". Note that "electrical anharmonicity" also exists in RS. It corresponds to a second order Taylor expansion of the polarisability in Equation (2) [423].
The wavenumber shifts can then be directly linked to any macroscopic stress/strain via the elastic compliance tensor and the $K_{ijlm}$ coefficients that describe the strain-induced deformation of the bonding potentials; in other words: anharmonicity [435]. Few of these coefficients are independent in high-symmetry crystals (see [436] in cubic crystals or [437,438] for hexagonal corundum). The mathematical expressions for the stress dependency of optical modes in cubic crystals can be found for given crystallographic directions [90,435] and planes [439-443]. Ager et al. reported less than 15% disagreement between the biaxial residual stress measured by RS in a diamond film (deposited on a titanium alloy) using linear combination of uniaxial stresses perpendicular to the growth direction, and the theoretical value expected from elasticity theory [441]. The same kinds of measurements are common for semiconductors [444,445].

5.1.4. The Case of Non-crystalline Materials

In polycrystalline or amorphous materials, the tensorial formalism is irrelevant (stress directions are unknown). We must therefore adopt a "statistical" approach. Let $\theta_b$ be the initial angle between a bond and the solicitation axis in a material macroscopically strained to $\Delta \varepsilon_M \%$. The simplest assumption is to consider that this bond is strained by an amount of $\Delta \varepsilon_b \% = \Delta \varepsilon_M \% \cos \theta_b$. The resultant shift is an integration of Eq. (43) over all bonds:

$$\Delta \nu_{\text{tot}} \approx S^e \times \int_{\theta=0}^{\theta=\pi} \left[ p(\theta) \times \Delta \varepsilon_M \cos(\theta) \right] d\theta$$

In Eq. (49), $p(\theta)$ represents the probability for $\theta_b$ to be $\theta$. If the material is isotropic, then $p(\theta)$ is a constant and:

$$\Delta \nu_{\text{tot}} \sim S^e \times \Delta \varepsilon_M \%$$

Therefore, a proportionality factor $S^e$, expressed in units of cm$^{-1}$/%, links the wavenumber shift to the macroscopic strain in isotropic materials. Besides, if Hooke’s law applies over the full strain exploration$^{31}$, then:

$$\Delta \nu = S^e \times \frac{100 \times \Delta \sigma}{E} = S^\sigma \times \Delta \sigma$$

$^{29}$ Compliance terms $S_{ij}$ are defined according of Voigt's notation by $e_i = S_{ij} \times \sigma_j$ ($e$ = strain; $\sigma$ = stress; $i$ = 1 to 6 correspond to directions xx, yy, zz, yz, xz and xy respectively, with $e_{22} = 2 \times e_{yy}$, $e_{33} = 2 \times e_{zz}$ and $e_{xy} = 2 \times e_{yz}$).

$^{30}$ Some errors in formulas from Ager et al. [441] and Cheong et al. [442] were listed in Reference [379].

$^{31}$ Hooke’s law ($\sigma = E e$) supposes a proportionality factor (the so-called Young’s modulus) exists between stress ($\sigma$) and deformation ($e$).
The applied stress $\Delta \sigma$ and Young’s modulus $E$ are expressed in GPa. From hereon, the $S^{\varepsilon/\sigma}$ symbol, let us name it the Raman Mechanical Coefficient (RMC)$^{32}$, will be used whenever comments apply to both $S^\sigma$ and $S^{\varepsilon}$. $S^{\varepsilon/\sigma}$ is usually negative: wavenumbers decrease under tension and conversely$^{33}$.

The technique of micro-Raman Extensometry ($\mu$RE) consists in deriving a $S^{\varepsilon}$ value from a reference sample subjected to controlled strain (Figure 20) for later in situ strain determination in a composite [80,388,391-393,414] (see § 5.2 and 5.3). The peculiarity of nanophased materials is that stress relaxation is expected at grain interfaces/interphases. The numerical values of the RMC end up being lower than in a single crystal. They are even lower if nanocrystals from a secondary phase are used as the mechanical probe: the more dispersed a phase, the lower its contribution to stress transfer and the lower the corresponding $S^{\varepsilon/\sigma}$ (Figure 21. For instance, $S^\sigma$ for O-Si-O bending mode (~ 450 cm$^{-1}$; see Figure 11) is -5 cm$^{-1}$/GPa in amorphous silica fibres, where tetrahedra are continuously bridged by oxygen atoms, but is 5-10 times lower for isolated rings of only 3-4 tetrahedra [446].

![Figure 20](image-url): Calibration of the Raman Mechanical Coefficient ($S^{\varepsilon/\sigma}$) of carbon G band (see § 4.3) for 3 IM7 fibres (Adapted from Ph. Colomban et al., Composites Part A, 37[4], pp 646-651, 2006).

5.2. In-situ micro-Raman Extensometry of Ceramic Fibre-reinforced Composites

The reinforcement of ceramic materials with long ceramic fibres leads to low density and refractory materials of high damage tolerance. Therefore they should be an appropriate substitute for metal alloys in advanced engines (turbines) and waste treatment energy plants [366]. Ceramic fibres can also be directly incorporated in metal matrices to increase their high temperature mechanical properties [366]. These are often hard to measure and an optical non-destructive technique such as $\mu$RE will prove very useful in this regard. One of the peculiarities observed in ceramic fibres prepared from polymeric precursors is that there is no accumulation of impurities at the grain boundaries. Due to the lack of such usual diffusion

---

$^{32}$ $S^\varepsilon$ is sometimes referred to as the Raman Frequency Gauge Factor (RFGF).
$^{33}$ $\varepsilon$ and $\sigma$ are positive for tensile solicitations.
regulators, abnormal grain growth is therefore very common and responsible for mechanical degradation [1]. A close relationship has been proven, for instance, between the micro-hardness and short-range ordering in sol-gel prepared nano-crystalline oxides [447] and some authors have already pointed out that the overall mechanical ability of fibres is governed by their microstructure [448-450]. The expertise of the fibre manufacturers consists in postponing the onset of crystallization and grain growth. The RMC difference between the reference single crystals and embedded nanoparticles under the same macroscopic stress can tell a lot about the fibre structure (Figure 21). Thus, $S_\varepsilon$ is -4.2 cm$^{-1}$/% (~ -1 cm$^{-1}$/GPa with $E=420$ GPa [370]) for SiC LO mode in the Hi-S fibre [379], which is lower than in SiC single crystals axially strained along [100] (-1.5 cm$^{-1}$/GPa) or [001] (-3.0 cm$^{-1}$/GPa) directions [379]. In such a quasi-stoichiometric SiC fibre, the carbon sensitivity is almost nil.

![Figure 21](image)


Equation (50), which derived from Eq. (43), assumed small bond deformation. Yet, the RMCs are measured up to the breaking point. For actual fibres, a better description of $S_\varepsilon$ is given with second or third order polynomial laws [451-453] and $S_\varepsilon^{\text{Compression}} < S_\varepsilon^{\text{Tension}}$ [389,453-455]. Yet, the $S_\varepsilon^{\text{Compression}}/S_\varepsilon^{\text{Tension}}$ ratio gets close to one in stiff materials (high Young’s modulus) containing (iono)-covalent bonds and isotropic 3D-bonded inorganic structures. Such materials do indeed have a lower sensitivity to flaws than chain-like structures (where flaws open under tension and close under compression). Thus, the difference between $S_\varepsilon^{\gamma/\sigma_{\text{compression}}}$ and $S_\varepsilon^{\gamma/\sigma_{\text{tension}}}$ is lower in graphitic carbon fibres than in linear chain-based fibres (PPTA, PBZT). Pitch fibres have better aligned and closer graphene planes than PAN fibres. They also have more "reversible" $S_\varepsilon$ coefficients [392,417]. Micro-Raman Extensometry (µRE) was most specifically applied to model polymer matrix systems reinforced with PAN [390,416,417,455-464] and Pitch [415,453] carbon fibres, aramid fibres [390,414,418,448,465-470], polyethylene fibres [471] or carbon nanotubes [472]. The matrix was then sufficiently transparent for *in situ* analysis of the embedded reinforcement material.
The $S^e$ calibrations and in-situ measurement of Raman spectra could be used to generate strain profiles $\varepsilon_f(l)$ along the fibre, from which other properties like (longitudinal) residual strain ($\varepsilon_f(l)$ in the lack of external stress)\cite{415,453,456,470,471}, interfacial shear stress $\tau_{ci}$ (Figure 22 and Ref. [459]), stress concentration factors \cite{455,457-459,461,463,469}, Ineffective Lengths$^{34}$ (IL) [459], the interfacial fracture energy $G_i$ [463] or the Coulombian friction coefficient (the proportionality factor between $\sigma_{radial}$ and $\tau_{ci}$) [416] can be derived.

![Diagram of Fibre-Matrix sliding](image)

Figure 22: Diagram of Fibre-Matrix sliding. The deformations of the fibre and matrix when a stress $\Delta \sigma$ is applied to the composite are in the ratio of the Young's Moduli ($\Delta \sigma = E_f \times \Delta \varepsilon_f = E_m \times \Delta \varepsilon_m$). Hence the interfacial shear stress $\tau_{ci}$ between the fibre and the matrix [459].

The key points for getting reliable µRE results are an accurate determination of $S^e$ (Figure 20) and taking into account that stress is not the only possible reason for peak shifts. Fibre/matrix inter-diffusion and laser-induced heating$^{35}$ produce chemical and thermal shifts, which are accounted for in the following expression$^{36}$ \cite{91,379}:

$$\Delta \sigma = \frac{E_f \times \left(\nu_{in\,situ} - \nu_{in\,0}\right) + \left(\nu_{fiber\,as-received} - \nu_{fiber\,extracted\,from\,the\,composite}\right) + P_l \times (S^p_{reference} - S^p_{sample})}{100 \times S^e_{fibre}}$$ (52)

In Eq. (52), $S^p$ measures the (quasi-)linear dependence of the wavenumber on the laser power $P_l$. The spatial resolution of µRE makes it easy to study the effect of a fibre environment (neighbouring fibres or cracks, fibre sizing, humidity, etc) on stress \cite{455,457-460,466,469,470}. The results fulfil relatively well the predictions of micromechanical models such as Cox's (axial stress for elastic fibre and matrix, the so-called "shear-lag" model) \cite{414,416}, Piggott's (applies after fibre/matrix decohesion and for matrix creeping) \cite{414,418,466,474}, the friction model of Kelly and Tyson \cite{416,460,474} or that of Cook and Gordon (stress concentration in the vicinity of cracks) \cite{466}.

The applicability of µRE to low transparency (ceramic matrix \cite{91,374,475}) or intrinsically opaque (inter-metallic matrix [476]) coupons has recently been demonstrated, despite their high consolidation temperatures (fibre/matrix inter-diffusions might complicate the study). Given the much higher Young's modulus of such matrices with respect to resins, Ineffective Lengths (ILs) are small enough (a few µm only instead of hundreds [459]) for a cross-section

$^{34}$ The length over which stress builds up from zero (at a fibre tip or a matrix crack) to its maximum value.

$^{35}$ Thermal expansion has the same effect on bond lengths (hence on $\nu$) as a tensile stress [473].

$^{36}$ This equation neglects the statistical wavenumber dispersion in the reference and supposes wavenumbers are corrected for any instability of the Raman spectrometer.
analysis to give results close to those obtained with longitudinal probing [91,390,393,475,476]. Yang and Young studied $\varepsilon_f(l)$ in model single fibre NLM/pyrex [474,477,478] and NLM/SiC [479] composites. Bollet et al. measured the influence of micro-cracking in SiC/glass-ceramic composites [480]. Pezzotti also used µRE to study cracking in "monolithic" ceramics [481]. Chollon and Takahashi studied a C/C composite [482]. Colomban and co-workers measured residual stress in C$_f$/mullite [475], NLM/mullite [475] and Hi-Nicalon/mullite [374,483] composites.

5.3.► In-situ Analysis of a C$_f$/epoxy Composite

Nine $\mu$m diameter PAN-based low crystallinity IM7 carbon fibres (Hexcel Fibres, USA) were used for the unidirectional reinforcement of an epoxy matrix processed by radical-polymerisation under $\gamma$ irradiation. The resulting composite ($\gamma$-pol) was nearly opaque, rather unfavourable conditions for a µRE study. These notwithstanding, $\gamma$-pol was submitted to a constant tensile strain of 1% and the spectra could be recorded through a few tens of micrometers of the matrix material, starting from the tip of an isolated fibre chosen in a fibre-poor region (Figure 23-a). This ~300 $\mu$m-long segment was longer than the usual IL in polymer matrices (~200 $\mu$m [391,457,459]), which was mandatory to observe full fibre-matrix interaction. The results of the spectra fitting are illustrated in Figure 23-b. D and G bands (see §4.3) have very similar wavenumber variations, with a few singular points. These might result from the local environment (presence of cracks or neighbouring fibres), as expected from the conclusions of van den Heuvel et. al. [457]. The jumps in opposite directions for D and G wavenumbers support an attribution to stresses of different nature (axial vs. radial). It is indeed a well established fact that graphite planes preferentially orientate along the longitudinal direction of high-performance carbon fibres [484,485]. G wavenumber should thus be representative of the axial loading of the fibre. As for D band, it corresponds to defective graphene, possibly the C$_{sp}^2$-C$_{sp}^3$ bonds forming where graphite nanocrystals transform into amorphous carbon. Such bonds located at the surface and in-between the graphite planes would be expected to be less specifically sensitive to the loading direction. G wavenumbers have been converted into an axial compressive stress ($\sigma_f$) in Figure 23-c and the resulting data were fitted according to the following model [366]:

\[
\sigma_f = \sigma_{\text{max}} \left( 1 - \cosh \left( \frac{\beta}{2} \frac{x}{l} \right) \right) \left( \frac{1}{\cosh \left( \frac{\beta l}{2} \right)} \right)^{-3.7}
\]

\[\beta \sim 0.03 \frac{\mu m}{l} \]

\[
\beta = \frac{1}{r} \frac{E_m}{(1+\nu_m)E_f} \ln \left( \frac{r_m}{r} \right)
\]

Equation (53)

x is the position along the fibre of length l and radius r, $\sigma_{\text{max}}$ is the maximum stress, $\nu_m$ is the matrix Poisson's ratio and $E_f$ and $E_m$ are the fibre and matrix Young's moduli. As for $r_m$, it corresponds to the effective matrix thickness responsible for the fibre stress. A value $\beta \sim 0.03 \mu m^{-1}$ gave the best fit and the variation in Figure 23-c shows the axial compression rises from the tips along a characteristic IL ~100 $\mu$m.
In this section, we will demonstrate how the local information accessed by RS through very simple spectra fittings correlates with "macroscopic" parameters such as Young's modulus, tensile strength and micro-hardness. The reason why such a correlation exists is the common dependence of the Raman signal and the mechanical behaviour on the micro/nanostructure of materials.

5.3.1. → Comparison of Raman Spectra with Micro-Indentation Results

Strong correlations between Raman and microhardness data have been reported by Gogotsi et al. for semiconductors, quartz and carbon [134,487] and by Amer et al. for “diamond-like carbon” [488]. Figure 24 illustrates how "mechanical changes" (Figure 24-c) are similarly related to a change in the Raman spectrum of either carbon or SiC (Figure 24-a&b) in a SCS-
6 fibre. The variations in Berkovich's micro-hardness (µH; three-sided diamond tip) and Young's modulus were measured by Mann and co-workers [490] and we highlighted different zones with vertical dots. From core to periphery, they correspond to:

I) The 32 µm-diameter carbon core consisting of graphitic units 1 to 5 nm in size [476].

II) A 1.5 µm-thick layer of pyrolytic carbon (grains are 25-50 nm in size). It has been identified as the weakest part of the fibre because its graphitic planes are parallel to the fibre axis [490].

III) A zone in which carbon coexists with SiC and evolves over 30 µm towards a highly disordered carbon.

IV) A zone where only SiC is detected (C-C bonds abundance ≤ 0.1%). The TO and LO peak widening and the increase of the background level reveal stacking faults are all the more frequent as thickness increases [476]. In spite of this, the mechanical properties are constant, which suggests they are governed by free carbon in insertion.

V) The interfacial carbon deposit (thickness 3µm).

**Figure 24:** Reprinted from J. Eur. Ceram. Soc., 21[9], G. Gouadec and Ph. Colomban, Non-destructive mechanical characterization of SiC fibres by Raman spectroscopy, pp 1249-1259, 2001, with permission from Elsevier - a) Raman detection of carbon (intensities of D, G and D' peaks are added) and SiC (intensities of TO and LO peaks are added) as a function of the position along the fibre radius (λ_{laser}=632.8nm). 100% corresponds to the maximum intensity.

---

37 This is a 140 µm-diameter fibre used for metal-matrix reinforcement [366]. It has a high heterogeneity along the radius, due to a preparation by CVD of SiC (and carbon), on a carbon core [489].
detected for each phase - b) Bandwidths obtained after spectra fitting for D carbon peak ($\lambda_{\text{laser}}=632.8\text{nm}$) and SiC TO modes (three separate scans; $\lambda=514.5\text{nm}$) - c) Young's modulus and "Berkovich's hardness" (data from Mann et al [490]).

5.3.2. Comparison of Raman Spectra with Fibre Strength

Figure 25 shows the correlation of the strength measured on NLM [371] and Hi-Nicalon [384] SiC fibres annealed at different temperatures (up to about 1500°C) with their Raman spectra recorded at room-temperature. The linearity suggests that the macroscopic (strength measurement) and microscopic (Raman spectrum) responses to stress have the same dependence on grain size. A strength reduction resulting from grain boundary creeping is ruled out since it would not alter the Raman spectra. Two atmospheres were tested for the NLM grade. The mechanical failure is postponed in a reducing atmosphere but this does not seem to modify the "micro-macro" mechanical correlation.

![Figure 25: Raman shift and linewidth of carbon D mode ($\lambda=514.5\text{nm}$) plotted as a function of tensile strengths found in Berger et al. [384] or Kumagawa et al. [371] for heat treated SiC fibres. Reprinted from J. Eur. Ceram. Soc., 21[9], G. Gouadec and Ph. Colomban, Non-destructive mechanical characterization of SiC fibres by Raman spectroscopy, pp 1249-1259, 2001, with permission from Elsevier.](image)

5.3.3. Young Modulus and "Raman microextensometry"

At the macroscopic scale, fibres present the same tendency as their bonds to strengthen in compression and soften in tension [454]. Hooke's law being nothing but the macroscopic manifestation of bond stiffness, one may indeed expect to find a relationship linking $E$ to $k_b$ (introduced in Eq. (37)) via $S^2$.

The simplest expression modelling a "realistic" bond potential $V(l_b)$ would be the following:

$$V(l_b) = \frac{k_b}{2} (l_b - l_{0})^2 + \frac{k'_b}{6} (l_b - l_{0})^3; \; k' < 0 \tag{54}$$

With this form, the quasi-harmonic approximation (Eq. (37) and (38)) leads to:

$$\nu(l_b) \propto \sqrt{k_b \times \left(1 + \frac{k'_b}{k_b} \times (l_b - l_{0})\right)} \tag{55}$$
$k_b'$ is expected to be much smaller than $k_b$ so, as long as $l_b$ remains close to $l_0$ (small strain assumption), a Taylor expansion is justified:

$$
\nu(l_b) \sim \sqrt{k_b} \cdot \frac{k_b'}{\sqrt{k_b}} \times (l_b - l_0)
$$

(56)

$$
\nu(l_b) - \nu(l_0) \sim \frac{k_b'}{\sqrt{k_b}} \times (l_b - l_0)
$$

(57)

Upon comparison with Eq. (50), this is equivalent to:

$$
S_b^\varepsilon = \frac{k_b' l_0}{100 \sqrt{k_b}} < 0
$$

(58)

Here again, we find that the energy shift for a strained bond can be expected to be proportional to the bond deformation. Besides, in such isotropic structures as most Nanophased fibres are, the "bond compression model" predicts a Young's modulus in the following form [491]:

$$
E = \sum_{\text{bonds}} \frac{l_b^2 k_b}{9}
$$

(59)

**Figure 26**: Absolute value of the Raman Mechanical Coefficient (RMC) of carbon G band plotted versus the inverse of Young's modulus square root. Reprinted from J. Eur. Ceram. Soc., 21[9], G. Gouadec and Ph. Colomban, Non-destructive mechanical characterization of SiC fibres by Raman spectroscopy, pp 1249-1259, 2001, with permission from Elsevier.

For fibers with a single (or dominant) type of bonds, $k_b$ and $k_b'$ have unique values and, according to equations (58) and (59), $S_b^\varepsilon$ must then be proportional to $E^{-1/2}$. The same will apply to $S_G^\varepsilon$ (see discussion of Eq. (49) and (50)). Figure 26 plots $S_G^\varepsilon$ coefficient measured in different carbon and "first generation" SiC fibres as a function of Young's modulus square root. The proportion and the distribution of the carbon and SiC phases differ in the fibres and,
yet, a global classification is possible. Note that a direct proportionality between $S^\varepsilon$ and $E$ has been reported in the literature but these results were based on a narrower exploration of Young Modulus, limited to aramid [448,468,492], polyethylene [493] or carbon [454] fibres. Deviations from the linear trend in Figure 26 can be explained with the following arguments:

i)- A few of the $S^\varepsilon$ values appearing in Figure 26 were measured under compression and they are not necessarily comparable with those obtained through tensile straining. Indeed, $S^\varepsilon$ coefficients suppose a linear dependence of Raman wavenumbers on the macroscopic deformation but a general relationship would rather be quadratic [451]:

$$\Delta \nu = a \Delta \varepsilon + b (\Delta \varepsilon)^2$$

(60)

$S^\varepsilon$ is thus subject to change when passing from tensile to compressive stress. There is almost no effect (b ~0) for isotropic structures like SiC fibres with strong covalent bonds in all directions but Melanitis et al. found $a/b\sim 5$ (only !) in "PAN-based" carbon fibres [452].

ii)- Not all $S^\varepsilon$ values in Figure 26 were obtained with the same laser line. Yet, carbon is a resonant species and both the spectrum and the penetration depth therefore depend on the wavelength. Most papers on Raman extensometry of carbon have neglected this aspect of the problem.

iii)- The reasoning that drove to Figure 26 neglected $k_b$ and $k_b'$ distribution in the material. This simplification is probably acceptable in carbon fibres but certainly not in SiC fibres (Tyranno and NLM grades), where C-C and C-SiC bonds coexist. For that matter, 2nd and 3rd generation SiC fibres have such a specific behaviour that they were not even included in Figure 26. In such fibres with small amorphous or crystalline particles, C-C bonds are largely outnumbered by Si-C and inter-particles bonds. $E_{\text{fibre}}$ (macroscopic scale) can no longer be considered as the counterpart of $S^{\varepsilon/\sigma}_{\text{particles}}$ (bond scale) [376].

**Figure 27**: Comparison of the strain dependency of the crystalline and amorphous low frequency Raman contributions (left hand scale) with the stress-strain tensile curve (right hand scale) for PET fibres. Reprinted from Engineering Fracture Mechanics, 73[16], Ph. Colomban et al., Micro-Raman study of the fatigue and fracture behaviour of single PA66 fibres: Comparison with single PET and PP fibres, pp 2463-2475, 2006, with permission from Elsevier.
Figure 27 shows that the variations of Young Modulus (the slope on the strain-stress curve) in a semi-crystalline polymer such as PET can be correlated with the Raman shifts of the low frequency contributions corresponding to the amorphous and crystalline substructures (see Figure 5). In PET fibres, most of the stress is obviously transferred to the amorphous matrix, whereas nano-crystallites are only slightly compressed by a Poisson's effect in the amorphous matrix. In Polyamide fibres, both the amorphous and crystalline moieties accommodate the stress because the nanostructure puts them "in series". Wavenumber-strain curves then start with a plateau that corresponds to the disentanglement of the polymer chains (visco-elastic regime) and wavenumbers start downshifting as soon as "knots" block this process (elastic regime) [170,171,173,494].

5.4. ► CNTs used as Nanometric Stress Gauges

On account of their very small dimension, the direct determination of CNTs Young’s modulus is difficult. Most experimental values were obtained through manipulations with an AFM tip (see table 4 in Ref. [495]) but Lourie and Wagner demonstrated that an indirect measurement was possible using RS on "quenched" matrix-embedded nanotubes [496]. Using a "concentric cylinders" modelling of each CNT and the surrounding matrix, they calculated the axial tube stress due to cooling by $\Delta T$ degrees and established nanotubes Young's modulus $E_{NT}$:

$$E_{NT} = \left[ \frac{\Delta \alpha \Delta T}{\varepsilon_{NT}} - 1 \right] \left[ \frac{1 - f_{NT}}{f_{NT}} \right] E_m$$  \hspace{1cm} (61)

$\Delta \alpha$ is the difference in thermal expansion, $f_{NT}$ is the volume fraction of nanotubes, $E_m$ the Young’s modulus of the matrix and $\varepsilon_{NT}$ is the compressive strain. The latter was measured by the strain dependency of D$^*$ Raman band of SWCNTs, which allowed Young's modulus determination. Conversely, some authors filled composites matrices with nanotubes and used them to sense fibre stress in polymers [472,497,498].
Gwénaël Gouadec (born in 1973) is Associate Professor at Pierre & Marie Curie (Paris VI) University where he teaches Physical Chemistry. He took an Engineering degree in Materials Science from the University of Rennes in 1996 and served his French National Duty period at ONERA, the French Aeronautics and Space Research Centre, developing Sol-Gel interphases for Al₂O₃/Al₂O₃ Composites. In 2001, he got a Ph.D on the "Physical and Chemical Characterization of Aerospace Ceramic Matrix Composites by Raman (micro)-Spectroscopy". In 2002, he was appointed post-doctoral fellow at the University of Alabama at Birmingham. His Research project on the nano-compressibility of carbon micro-ballons was funded by Los Alamos National Laboratory (LANL). In 2003, Dr. Gouadec joined the Laboratoire de Dynamique Interaction et Réactivité (LADIR). He now specializes in the Raman spectroscopy of nanocrystalline and amorphous domains found in fibres reinforcing Polymer and Ceramic Matrix Composites (PMC/CMC).

Philippe Colomban (born in 1952) is the Head of the "Laboratoire de Dynamique, Interaction et Réactivité", a CNRS and Pierre & Marie Curie (Paris VI) University joint laboratory. He got is Engineering degree from Sèvres "Ecole Nationale Supérieure de Céramique Industrielle" in 1975 and a Ph. D. degree from Paris VI University in 1979. In 1975, Dr. Colomban was at Thomson-CSF (now Thalès) Central Laboratory one of the first to develop Sol-Gel routes for advanced ceramics (PLZT optically clear ferroelectric ceramics). In 1976 he was appointed as CNRS Research Associate at the "Ecole Nationale Supérieure de Chimie de Paris" and studied superionic conductors structure and ion mobility. In 1980 he created the Solid State Chemistry Group at the "Ecole Polytechnique", focusing on Nasicon solid electrolytes, proton conductors and Sol-Gel ceramics and became a Consultant for the French Science and Technology Minister. From 1989 to 1993 Dr. Colomban took charge of the new projects at the Materials Department of ONERA, the French Aeronautics and Space Research Establishment (Sol-Gel routes, Oxide-oxide ceramic-matrix composites, microwave absorbing materials and Functionally-Graded composites…). From 1994 to present, as a CNRS Senior Scientist, his research specialized in the use of Raman, IR and neutron spectroscopies for in situ stress and phase distribution imaging (in composites, solid state devices, fuel cells, synthetic and natural fibres) and the identification of the technologies used for the fabrication of ancient ceramics and glasses. Philippe Colomban was an invited speaker at International Conferences in many different topics. His publications comprise more than 300 original papers and reviews, and five patents. He is a board member of Composite Part B Journal, Editor of Taoci (the series of the French Oriental Ceramic Society) and received the Société Française de Chimie (SFC) "Solid State Chemistry Award" in 1984.
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