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A New Statistical Similarity Measure for Change Detection in Multitemporal SAR Images and its Extension to Multiscale Change Analysis

Jordi Inglada, Grégoire Mercier

Abstract—In this paper, we present a new similarity measure for automatic change detection in multitemporal SAR images. This measure is based on the evolution of the local statistics of the image between two dates. The local statistics are estimated by using a cumulant-based series expansion which approximates the probability density functions in the neighborhood of each pixel in the image. The degree of evolution of the local statistics is measured using the Kullback-Leibler divergence. An analytical expression for this detector is given, allowing a simple computation which depends on the 4 first statistical moments of the pixels inside the analysis window only.

The proposed change indicator is compared to the classical mean ratio detector and also to other model-based approaches. Tests on simulated and real data show that our detector outperforms all the others.

The fast computation of the proposed detector allows a multiscale approach in change detection for operational use. The so-called multiscale change profile (MCP) is introduced to yield change information on a wide range of scales and to better characterize the appropriate scale. Two simple yet useful examples of applications show that the MCP allows the design of change indicators which provide better results than a monoscale analysis.

Index Terms—Change detection; multitemporal SAR images; Kullback-Leibler divergence; Edgeworth series expansion; multiscale change profile (MCP).

I. INTRODUCTION

REMOTE sensing imagery is a precious tool for rapid mapping applications. In this context, one of the main uses of remote sensing is the detection of changes occurring after a natural or anthropic disaster. Since they are abrupt and seldom predictable, these events cannot be well temporally sampled – in the Shannon sense – by the polar orbit satellites which provide the medium, high and very high resolution imagery needed for an accurate analysis of the land cover. Therefore, rapid mapping is often produced by detecting the changes between an acquisition after the event and available archive data.

This change detection procedure is made difficult due to the time constraints imposed by the emergency context. Indeed, the first available acquisition after the event has to be used whatever its modality which is more likely to be a radar image due to weather and daylight constraints.

The kind of changes produced by the event of interest are often difficult to model. The same kind of event – a flood – can have different signatures depending on where it happens – high density built-up areas, agricultural areas, etc. – and on the characteristics of the sensor. Also, the changes of interest are all mixed up with normal changes, which can be the majority if the time gap between the two acquisitions is too long.

All these issues present us with a very difficult problem: detecting abrupt unmodeled transitions in a temporal series with only two dates.

From this position of the problem, one can make the straightforward deduction that pixel-wise comparison between the two images will not be robust enough.

In the case of radar acquisitions, the standard detector is based on the ratio of local means [3]. This detector is robust to speckle noise, but it is limited to the comparison of first order statistics. The classical model for SAR intensity introduced by Ulaby et al. [4] assumes that the texture is a zero-mean multiplicative contribution. Therefore, changes taking place at the texture level which preserve the mean value will not be detected by the mean ratio detector. One can thus assume a miss-detection behavior of the detectors using only the mean pixel values. This remark invites a more accurate analysis of the local statistics of the images to be compared. Bujor et al. [5] did very interesting work by analyzing the interest of higher order statistics for change detection in SAR images. They concluded that the ratio of means was useful for step changes and that the second and third order log-cumulants were useful for progressive changes appearing in consecutive images in multi-temporal series. Since higher order statistics seem to be helpful, one may want to compare the local probability density functions (pdfs) of the neighborhood of the homologous pixels of the pair of images used for the change detection.

Of course, this assumes that the pdfs are known, and that there exists a robust way to compare them. The estimation of pdfs can be made with different approaches, but the straightforward histogram method should be avoided due to the need a high number of samples for the estimation. Indeed, small analysis window sizes are required to yield high resolution change maps. In this paper, we will present several approaches for this estimation by using only a small number of samples for the local statistics estimation, up to order 4.

Once the pdfs are estimated, their comparison can also be performed using different criteria. Information theory shows that a good measure is the Kullback-Leibler divergence, also called information gain. We will use a symmetrical version of this measure and show that it is superior to the classical

1In the case where a sequence of several images is to be processed, the approaches presented in [1], [2] may be applied.
detector when the pdfs are correctly estimated.

Therefore, these measures will be based on the comparison of local neighborhoods where an analysis window for the computation of the local estimation of probabilities is used. The problem which arises here is the one of choice of window size. Since we are facing unmodeled changes, we cannot choose the window size to fit the size of the expected changes. An inappropriate window size can produce miss- and over-detections:

- when using a small window for a correlation analysis, no detection will be performed in a homogeneous area, which was globally changed to another homogeneous area;
- on the contrary, when using a larger window size, change areas have to be of larger size or strong in intensity (relatively to the measure) to be detected. In these cases, it will produce a coarse resolution change map.

One way to overcome this problem is by applying a multiscale change detection analysis.

Scale is to be understood in its geographic meaning, which is the spatial extent of the study area. It does not refer to the cartographic meaning of scale (the larger the scale the more detailed the information) [6]. For an interesting discussion on scale issues in remote sensing see [7].

Image processing techniques for multiscale analysis often use the cartographic meaning and apply low-pass filtering and possibly sub-sampling. For change detection analysis, this filtering and sub-sampling can be justified in the case where the images are not perfectly registered [8]. In other cases we think that it is better to use all the available information, that is, maximizing the number of available samples by using increasing window sizes. Nevertheless, pyramidal multiscale decompositions can also be useful in the case of phenomena characterizations (see [9] for example).

Therefore, the main point of the problem is how to choose the largest window size which robustly detects the changes but which is small enough to preserve the resolution of the final map without miss-detections.

We propose to use multiscale change profiles, which are defined as the change indicator for each pixel in the image as a function of the analyzing window size. The computation of the change detection for each window size can be very time consuming. We present here a method for the computation of these profiles which allows the change indicator at scale \( n \) to be computed from the value obtained at scale \( n - 1 \) plus a correction term which takes into account the addition of new samples only. Analytical expressions are given for three different change indicators.

This paper proposes three main contributions:

1) an Information Theory-based similarity measure which uses full local statistics;
2) the use of cumulant-based series expansions of similarity measures, which allow a robust and fast computation by using a small number of samples;
3) the concept of multiscale change profile and its fast implementation using recurrence evaluations.

The overall performance of the detection system will depend on both the quality of the change image and the quality of the thresholding. In this work, we choose to focus on the generation of an indicator of change for each pixel in the image. For interesting approaches in the field of unsupervised change image thresholding, the reader can refer to the works of Bruzzone and Fernández Prieto [10], [11], Bruzzone and Serpico [12] and Bazi et al. [13]. The reader may note that some of these approaches need a statistical modelling of the detectors’ response, which is not presented here.

The change indicator can also be useful by itself. Indeed, often the end user of a change map wants not only the binary information, given after thresholding, but also an indicator of the intensity of the change and eventually a confidence level. In order to evaluate the quality of a change image independently of the choice of the thresholding algorithm, the evolution of the detection probability, \( P_{\text{det}} \) as a function of the false alarm
probability, \( P_x \), may be evaluated in the case where a set of
constant thresholds are applied to the whole image. These are
the so-called Receiver Operating Characteristics (ROC) and
the plots of \( P_{\text{det}}(P_x) \) are called the ROC plots.

III. DISTANCE BETWEEN PROBABILITY DENSITIES

The main difficulty in the multitemporal analysis of SAR
images is the presence of speckle noise. When moving away
from interferometric configurations, the speckle is different
from one image to the other and it can induce a high number
of false alarms in the change detection procedure. Because
of the multiplicative nature of speckle, the classical approach
in SAR remote sensing involves using the ratio of the local
means in the neighborhood of each pair of co-located pixels.
The Mean Ratio Detector, MRD, is usually implemented as
the following normalized quantity:

\[
 r_{\text{MRD}} = 1 - \min \left\{ \frac{\mu_X}{\mu_Y}, \frac{\mu_Y}{\mu_X} \right\}, \tag{1}
\]

where \( \mu_X \) and \( \mu_Y \) stand for the local mean values of the
images before and after the event of interest. The logarithm of eq. (1)
may also be used. Nevertheless, this operation does not modify
the performance of the detector in terms of ROC even if
the contrast of the image of change indicator is modified.
However, the logarithm is used since it modifies the initial
pdf of the image of change indicator and then facilitates the
development of Bayesian thresholding approaches [13].

This detector assumes that a change in the scene will appear
as a modification of the local mean value of the image. If the
change preserves the mean value but modifies the local texture,
it will not be detected.

The change detection algorithm proposed in this paper ex-
tends the MRD by analyzing the modification of the statistics
of each pixel’s neighborhood between the two acquisition
dates. A pixel will be considered as having changed if its
statistical distribution changes from one image to the other.
In order to quantify this change, a measure, which maps the
two estimated statistical distributions (one for each date at a
colocated area) into a scalar change index is required. Several
approaches could be taken into consideration: the mean square
error between the two distributions, the norm of a vector of
moments, etc. We have chosen to use a measure derived from
Information Theory called the Kullback-Leibler divergence
[14].

A. Kullback-Leibler divergence

Let \( P_X \) and \( P_Y \) be two probability laws of the random
variables \( X \) and \( Y \). The Kullback-Leibler divergence from \( Y \)
to \( X \), in the case where these two laws have the densities \( f_X \)
and \( f_Y \), is given by:

\[
 K(Y|X) = \int \log \frac{f_X(x)}{f_Y(x)} f_X(x) dx. \tag{2}
\]

The measure \( \log f_X(x)/f_Y(x) \) can be thought of as the information
on \( x \) for discrimination between hypothesis \( H_K \) and \( H_F \) if
hypothesis \( H_K \) is associated with pdf \( f_X(x) \), and \( H_F \) with
\( f_Y(x) \). Therefore, the Kullback-Leibler divergence \( K(Y|X) \) can
be understood as the mean information for discrimination
between \( H_K \) and \( H_F \) per observation. This divergence appears
be an appropriate tool to detect changes when we consider
that changes on the ground induce different shapes of the local
pdf.

Since the Kullback-Leibler divergence can be understood as
the entropy of \( P_X \) relative to \( P_Y \), it is also called information
gain. It can easily be proved that \( K(Y|X) \geq 0 \); \( K(Y|X) \) vanishes
only when the two laws are identical. \( K(Y|X) \) can be used as a
measure of the divergence from \( P_Y \) to \( P_X \). This measure is not
symmetric as it stands: \( K(Y|X) \neq K(X|Y) \), but a symmetric
version may be defined by writing:

\[
 D(X,Y) = D(Y,X) = K(Y|X) + K(X|Y) \tag{3}
\]

that will be called the Kullback-Leibler distance (KLD).

In order to estimate the KLD, the pdfs of the two variables to
be compared have to be known. As stated in the introduction,
the processing of high resolution change maps requires analy-
ssis windows of small size, which makes impossible the use
of local histogram estimations. In the following sections, we
will introduce several approaches which allow the estimation
of the pdfs by using a limited number of samples only. This
requires some a priori information on the data which can be
introduced by using models of local statistics.

B. Gaussian KLD

As seen in section III, the classical detector of eq. (1) uses
first order statistics only. Yet, second order statistics are often
used for SAR image processing. For instance, many speckle
reduction filters [15], [16], [17] are based on the contrast
coefficient \( \sigma^2_X/\mu_X^2 \), that is, the ratio between the variance
and the square of the mean value. If the local statistics have to be
compared up to the second order, the local random variables,
\( X \) and \( Y \) may be assumed to be normally distributed (i.e. of
Gaussian law). Then, the pdf of \( P_X \) can be written as:

\[
 f_X(x) = G(x;\mu_X,\sigma_X) = \frac{1}{\sqrt{2\pi\sigma^2_X}} e^{-\frac{(x-\mu_X)^2}{2\sigma^2_X}}. \tag{4}
\]

An analogous expression holds for \( f_Y(x) \).

Fig. 2(b) shows the Gaussian approximation of the proba-
bility distribution of a small region of interest (Fig. 2(a))
extracted from a SAR image.

If this Gaussian model is used in eq. (3), it yields the
Gaussian Kullback-Leibler detector (GKLD):

\[
 r_{\text{GKLD}} = \frac{\sigma^2_Y + \sigma^2_X + (\mu_X - \mu_Y)^2 (\sigma^2_X + \sigma^2_Y)}{2\sigma^2_X \sigma^2_Y} - 1. \tag{5}
\]

It can be seen that even in the case of identical mean values,
this detector is able to underline the shading of textures which
is linked to the local variance evolution.

Nevertheless, the reader should note that the Gaussian
model should not be used since SAR intensity values are
always positive. However, this example has been given as a
simple case of a parametric model which takes into ac-
count second order statistics. Since some Gaussianity may
be introduced into the data when resampling and filtering the
images during the pre-processing step, the Gaussian model may nevertheless be justified.

C. KLD using the Pearson system

The drawback of the GKLD is that SAR intensity statistics are not normally distributed, and the use of a bad model can induce bad performance of the detector, whatever the accuracy of the parameter estimation. In the absence of texture, the radar intensity follows a Gamma distribution:

\[ f_X(x) = \frac{1}{\Gamma(L)} \left( \frac{L}{\sigma_X} \right)^L e^{-\frac{Lx}{\sigma_X}} x^{L-1}. \]

(6)

The Gamma distribution is characterized by the following parameters: \( L \) is the number of looks and \( \sigma_X \), the square-root of the intensity SAR image. \( \Gamma(\cdot) \) is the Gamma function.

In the presence of texture, the local statistics can deviate from the Gamma distribution. For instance, if the texture is represented by a point on the first 4 statistical moments. Any distribution can therefore be induced bad performance of the detector, whatever the accuracy of the parameter estimation. The drawback of the GKLD is that SAR intensity statistics are not normally distributed, and the use of a bad model can cause bad performance of the detector, whatever the accuracy of the parameter estimation. The difference of eight types of distributions among which the Gaussian and the Gamma distributions known as the Pearson system [19]. It is composed of eight types of distributions among which the Gaussian and the Gamma distributions.

\[ X \sim \text{Gamma}(\mu_X, \beta_X) \]

where \( \mu_X \) is the centered moment of order \( i \) of variable \( X \).

More generally, it is now accepted that the statistics of SAR images can be well modeled by the family of probability distributions known as the Pearson system [19]. It is composed of eight types of distributions among which the Gaussian and the Gamma distributions may be found. The Pearson system is very easy to use since the type of distribution can be inferred from the following parameters:

\[ \beta_{X,i} = \frac{\mu_{X,i}^2}{\mu_{X,2}} \quad \text{and} \quad \beta_{X,2} = \frac{\mu_{X,4}}{\mu_{X,2}^2}, \]

where \( \mu_{X,i} \) is the centered moment of order \( i \) of variable \( X \).

That means that any distribution from the Pearson system can be assessed from a given set of samples by computing the first 4 statistical moments. Any distribution can therefore be represented by a point on the \( (\beta_{X,1}, \beta_{X,2}) \) plane. For instance, the Gaussian distribution is located at \( (\beta_{X,1}, \beta_{X,2}) = (0, 3) \), and the Gamma distributions lie on the \( \beta_{X,2} = \frac{3}{2} \beta_{X,1} + 3 \) line. Details about the theory of the Pearson system can be found in [20].

Figure 2(c) shows an example of distribution estimation. The Pearson approximation fits the data better than the Gaussian one (Fig. 2(b)). The example shown corresponds to a Beta distribution of the first type with parameters \( \beta_1 = 2.51 \times 10^{-6}, \beta_2 = 1.87 \).

The Pearson-based Kullback-Leibler Detector (PKLD) was originally introduced in [21]. It does not have a unique analytic expression, since 8 different types of distribution may be hold. Therefore, 64 different possibilities for the couples of pdf exist. Once the couple of pdfs is identified, the detection can be performed by numerical integration:

\[ r_{PKLD}(X, Y) = \int \left[ \log \left( \frac{f_X(x; \beta_{X,1}, \beta_{X,2})}{f_Y(x; \beta_{Y,1}, \beta_{Y,2})} \right) f_X(x; \beta_{X,1}, \beta_{X,2}) + \log \left( \frac{f_Y(x; \beta_{Y,1}, \beta_{Y,2})}{f_X(x; \beta_{X,1}, \beta_{X,2})} \right) f_Y(x; \beta_{Y,1}, \beta_{Y,2}) \right] dx. \]

(8)

The correct way to proceed to use the Pearson system is to choose a pdf using the estimated moments and then estimate the parameters of the distribution by maximum likelihood. While this can improve the results of the pdf estimation, the effect is not noticeable in terms of the estimation of the change indicator. This approach was not used in the experiments in order to reduce the computation cost.

The reader should note that in the case of single-look high resolution SAR data (better than 10 m) other statistical models may be more appropriate, mainly on urban areas. Nicolas et al. have proposed a new model based on the log-statistics and a set of pdfs coming from the Fisher system of distributions [22], [23]. It has been applied to high resolution SAR images on dense urban areas with promising results [24], [25].

D. Cumulant-based KL approximation

Instead of considering a parameterization of a given density, or set of densities, it may be of interest to describe the shape of the distribution. Such a description is based on quantitative terms that may approximate the pdf itself. The cumulants themselves do not provide such a pdf estimation directly but are necessary to describe its shape: for example, third order \( (\kappa_3) \) is linked to the symmetry (i.e. skewness), while the fourth \( (\kappa_4) \) is linked to the flatness (i.e. kurtosis). The density is then estimated through a series expansion. In fact, the cumulant generating function is used for such an estimation. By definition, the cumulant generating function \( \mathcal{K}_X(\cdot) \) of a random variable \( X \) is defined by:

\[ \mathcal{K}_X(\omega) = \ln \mathcal{M}_X(\omega) = \sum_n \kappa_{X,n} \frac{\omega^n}{n!} \]

with \( \mathcal{M}_X(\cdot) \) being the moment generating function defined by:

\[ \mathcal{M}_X(\omega) = \int e^{\omega x} f_X(x) dx = \int \left( 1 + \omega x + \frac{\omega^2}{2!} x^2 + \cdots \right) f_X(x) dx. \]

For the case of the four first order cumulants, the following expressions hold [26, p.8]:

\[ \begin{align*}
\kappa_{X,1} &= \mu_{X,1} \\
\kappa_{X,2} &= \mu_{X,2} - \mu_{X,1}^2 \\
\kappa_{X,3} &= \mu_{X,3} - 3 \mu_{X,2} \mu_{X,1} + 2 \mu_{X,1}^3 \\
\kappa_{X,4} &= \mu_{X,4} - 4 \mu_{X,3} \mu_{X,1} - 3 \mu_{X,2}^2 + 2 \mu_{X,2} \mu_{X,2} \mu_{X,1} - 6 \mu_{X,1}^4.
\end{align*} \]

(9)

Let us assume that the density to be approximated is not too far [27] from a Gaussian pdf (denoted as \( G_X \) to underline the fact that it has the same mean and variance as \( X \), that is, with a shape similar to the Gaussian distribution. The difference between \( \mathcal{K}_X(\cdot) \) and \( \mathcal{K}_{G_X}(\cdot) \), can be written in terms of the
difference of the cumulants $\kappa_{X,n} - \kappa_{G,n}$. By inversion, the density may be expressed by a formal Taylor-like series:

$$f_X(x) = G_X(x) + c_1 \frac{d G_X}{dx} x + c_2 \frac{d^2 G_X}{dx^2} x^2 + \cdots$$

Since a Gaussian density is used, it yields

$$f_X(x) = \sum_{r=0}^{\infty} c_r H_r(x) G_X(x),$$

with $H_r(x)$ known as the Chebyshev-Hermite polynomial of order $r$ [27]. When choosing a Gaussian law so that its first and second cumulants agree with those of $X$, the number of terms of the series expansion is greatly reduced. This is the so-called Edgeworth series expansion. Its expression, when truncated to order 6, is the following:

$$f_X(x) = \left( 1 + \frac{\kappa_X^2}{6} H_3(x) + \frac{\kappa_X^4}{24} \frac{1}{G_X} H_4(x) + \frac{\kappa_X^6}{120} \frac{1}{G_X^2} H_5(x) \right) G_X(x).$$

It can be thought of as a model of the form $X = X_G + X'$ where $X_G$ is a random variable with Gaussian density with same mean and variance as $X$, and $X'$, a standardized version of $X$ [28] with:

$$X' = (X - \kappa_{X,1}) \kappa_{X,2}^{-1/2}.$$  

Fig. 2(d) shows an example of such an approximation of a histogram.

The Edgeworth series expansion of the two pdfs $f_X$ and $f_Y$ may be introduced into the Kullback-Leibler divergence (eq. (2)). It yields an approximation of the Kullback-Leibler divergence by Edgeworth series, truncated at a given order. In [29], such an approximation has been truncated to order 4 by using the equality $f_X = f_X G_X/g_Y$, where $G_X$ (resp. $G_Y$) is a Gaussian density of same mean and variance as $f_X$ (resp. $f_Y$). Then,

$$KL_{\text{Edgeworth}}(X, Y) =$$

$$\frac{1}{2} \frac{\kappa_X^2}{\kappa_Y^2} \left( \log \frac{\kappa_Y^2}{\kappa_X^2} - 1 + \frac{1}{\kappa_Y^2} \left( \kappa_{X,1} - \kappa_{Y,1} + 1/2 \kappa_{Y,2} \right)^2 \right)$$

$$+ \frac{1}{6} \kappa_X^2 \frac{a_1}{\kappa_Y^2} + \frac{1}{24} \kappa_Y^4 \frac{a_2}{\kappa_Y^2} + \frac{1}{72} \kappa_Y^6 \frac{a_3}{\kappa_Y^2}$$

$$- \frac{1}{12} \frac{\kappa_X^2}{\kappa_Y^2} \left( c_0 - 6 \frac{c_4}{\kappa_Y^2} + 9 \frac{c_2}{\kappa_Y^2} \right)$$

$$- 10 \kappa_Y^6 \frac{\kappa_{Y,3}}{\kappa_Y^2} \left( \kappa_{X,1} - \kappa_{Y,1} \right) \kappa_{Y,2} (X - \kappa_{Y,1}) \kappa_{Y,2}^{-1/2}.$$  

where

$$a_1 = c_3 - 3 \alpha \frac{\kappa_Y^2}{\kappa_Y^2},$$

$$a_2 = c_4 - 6 \alpha \frac{\kappa_Y^2}{\kappa_Y^2} + \frac{3}{4} \kappa_Y^2,$$

$$a_3 = c_6 - 15 \alpha \frac{\kappa_Y^2}{\kappa_Y^2} + 45 \alpha \frac{\kappa_Y^4}{\kappa_Y^2} + 15 \kappa_Y^6,$$

$$c_0 = \kappa_{X,1} - \kappa_{Y,1}$$

$$c_2 = \alpha^2 + \beta^2,$$

$$c_4 = \alpha^4 + 6 \alpha^2 \beta^2 + 3 \beta^4,$$

$$c_6 = \alpha^6 + 15 \alpha^4 \beta^2 + 45 \alpha^2 \beta^4 + 15 \beta^6,$$

$$\alpha = \frac{\kappa_{X,1}}{\kappa_{Y,1}},$$

$$\beta = \frac{\kappa_{X,2}}{\kappa_{Y,2}}.$$  

Finally, the cumulant-based Kullback-Leibler detector (CKLD) between two observations $X$ and $Y$ is written as:

$$r_{\text{CKLD}} = KL_{\text{Edgeworth}}(X, Y) + KL_{\text{Edgeworth}}(Y, X).$$  

The reader should note the fact that, like for the Pearson-based detector, despite the apparent complexity of the formulas, and thanks to eq. (9), only the moments up to order 4 have to be computed.

 IV. MULTISCALE CHANGE PROFILE

Scale plays a strategic role in image analysis and more especially in change detection applications. In section I, it has been shown how an inappropriate scale of analysis can produce miss- or over-detections. In [30], Bovolo and Bruzzone, stress the fact that the scale of analysis is a key parameter for better discrimination between change and no change areas. Such a point of view is implemented by a wavelet transform of the log-ratio estimated with a window of a user-defined size.

Instead of applying a multiscale analysis of the change image, the purpose here is to produce a set of change indicators estimated at various scales. We will call it multiscale change profile (MCP).

As stated in the introduction, the multiscale term refers here to the size of the analyzing window. The MCP will therefore involve computing the change indicator for a pixel by using neighborhoods of increasing sizes. The so-called profile corresponds to the sequence of change measures as a function of scale. We will restrict our formulation to the case of the CKLD. Given the fact that this detector needs the estimation of scale. We will restrict our formulation to the case of the CKLD. Given the fact that this detector needs the estimation of the statistical moments of the samples inside the analyzing window, we are interested in finding an approach which avoids the computation from scratch of the moments at every scale.

A. Optimized computation of the MCP

Let us consider the following problem: how to update the moments when an $N + 1$th observation $x_{N+1}$ is added to a set of $N$ observations $\{x_1, x_2, \ldots, x_N\}$ already processed. When
considering raw moments of order \( r \), the formulation comes easily as:

\[
\tilde{\mu}_r[N+1] = \frac{N}{N+1} \tilde{\mu}_r[N] + \frac{1}{N+1} x_{N+1}^r.
\]

\( \tilde{\mu}_r[N] \) (resp. \( \tilde{\mu}_r[N+1] \)) stands for the raw moment of order \( r \) estimated with \( N \) samples (resp. \( N+1 \) samples). Since the analyzing window may contain textured areas, the mean value itself may be modified by the increase in the number of samples. Therefore, by using simple binomial properties, it can be shown that central moments may be characterized by:

\[
\mu_{1,[N]} = \frac{1}{N} s_{1,[N]},
\]

\[
\mu_{r,[N]} = \frac{1}{N} \sum_{t=0}^{r} \binom{r}{t} (-\mu_{1,[N]})^{r-t} s_{r,[N]},
\]

where the notation \( s_{r,[N]} = \sum_{i=1}^{N} x_i^r \) has been used.

Hence, when considering a new sample \( x_{N+1} \), each moment may be updated directly by using updates of \( s_{1,[N+1]} \) and then \( s_{r,[N+1]} \) for increasing values of order \( r \). The Edgeworth series is also updated by transforming moments to cumulants (by using eq. (9)) to be introduced in eq. (10) and then in eq. (11).

Fig. 2 shows an example of a pdf estimation on a homogeneous area (shown in fig. 2(a)) when the window increases from \( 9 \times 9 \) to \( 17 \times 17 \). In fact, the availability of updating the estimation of the distance between distributions from windows of any size without re-processing the overall data is the most interesting point for multiscale change detection purposes. This on-line multiscale moment estimation is the key for the operational use of the MCP concept.

For example, the computation of \( r_{CKLD} \) with windows of size ranging from \( 5 \times 5 \) pixels to \( 51 \times 51 \) pixels (22 different window sizes) takes only 42\% additional time with respect to the computation of a single detection with a window of median size of \( 29 \times 29 \) pixels (300 s. versus 210 s. for a \( 800 \times 400 \) pixel image).
B. MCP exploitation

The MCP computation produces a multichannel image (one scale per channel) whose pixels have to be transformed into scalar values in order to provide a change indicator. In order to exploit the information available at all scales, two approaches may be investigated. The first one consists in choosing the best scale for each image pixel. The second one consists in fusing the information available at all scales in order to provide a single change value.

The development of an optimal approach for the exploitation of the MCP may be application dependent. Indeed, multiscale fusion approaches could be tuned to a particular type of change – shape, nature, etc. In this section, two simple yet useful choices will be proposed which yield an improvement in comparison to the performance of a single scale detection.

1) In order to choose the best scale, we will choose the one which produces the highest KLD value. This assumes that this scale is the one that is associated with the largest window inside a homogeneous area with respect to the classes change and no change.

2) The fusion of the multiscale information will be performed by using Principal Component Analysis (PCA). The first principal component of the MCP multichannel image will be considered as the change indicator. This corresponds to a linear combination of all scales which maximizes the contrast of the final image.

V. EXPERIMENTS WITH SIMULATED DATA

A. Data set description

Simulations have been performed to better understand the behavior of the detectors relatively to a given kind of change and a given size of the change area. Since this study focuses on change detection on radar images, a speckle simulation is performed from a map of ground reflectivity. The simulated changes are applied on a small area, drawn as a circle, located in the center of the initial image.

The simulation procedure is based on the radar image formation mechanism. Each pixel is simulated with a given amplitude (coming from a SPOT, NIR band image, normalized to $[0, 1]$) and thousands phases coming from independent uniform generations in $[0, 2\pi]$ to characterize elementary wave scatterers. Taking the square of the modulus of each pixel yields a 1-look intensity image. A 4-look intensity image is obtained by averaging and subsampling two adjacent pixels along lines and rows.

Each simulation of change is applied to the initial image by using a change circle of given size taken from $\{5, 10, 15, 20\}$. Once the speckle simulation is performed (independently from one image to another), the speckled-changed images are mosaicked on a $2 \times 2$ grid as shown on fig. 4(b).

B. Simulation of changes

Three kinds of change were considered:

1) Offset change: fig. 4(c). The initial image is modified by applying an offset value (i.e. a shift) to the initial data. This is a very simple type of change which seldom occurs in reality, but is useful to characterize the behavior of the detectors.

2) Gaussian change: fig. 4(d). The initial image is modified by applying a zero mean gaussian additive noise to the initial data. This corresponds to a change in the state of the surface – field, vegetation. This is the main type of change that one can encounter in medium resolution SAR images.

3) Deterministic change: fig. 4(e). The initial image is modified by pasting values copied from another area of the image itself. This type of change can occur when there is a land-use change, anthropic activities, etc.

C. Results

1) Mono-scale detection: the results of the different detectors for a fixed analysis window size are analyzed.

Figure 5 shows the ROC plots for the case where the change consists in a shift of the reflectivity value (fig. 4(c)). In this case, all 4 detectors are able to detect the changes with high accuracy. There is a slight difference in performance between the pair CKLD - GKLD and the pair PKLD - MRD, but it is difficult to infer general behavior from this result. To draw a preliminary conclusion, for a simple change such as a reflectivity shift, the mean value criterion is efficient enough for good discrimination in the changes, even on speckled images.

Figure 6 shows the ROC plots in the case of a Gaussian change. The change is simulated by the addition of a Gaussian noise to the reflectivity (before speckle simulation). In this
case, the mean value of the observed pixels remains approximately the same. It is difficult for this kind of change to be observed by a human operator. However, it is more likely to occur when modifications affect the surface without changing its nature. In this case, even if all the detectors show bad performance, in comparison to the offset case, the MRD and the PKLD are far below the GKLD and CKLD. The bad performance of the MRD is easy to understand, since the zero-mean Gaussian noise added to the reflectivity slightly changes the observed mean value. For the PKLD, it can be argued that the type of law in the Pearson system is not very different from the initial case and the main difference is seen through the mean value, thus obtaining the same performance as the MRD. On the contrary, the GKLD assumes a simpler model consisting in the mean value, thus obtaining the same performance as the PKLD. For the PKLD, it can be argued that the mean Gaussian noise added to the reflectivity slightly changes the performance of the MRD is easy to understand, since the zero-mean Gaussian noise added to the reflectivity slightly changes the observed mean value. For the PKLD, it can be argued that the type of law in the Pearson system is not very different from the initial case and the main difference is seen through the mean value, thus obtaining the same performance as the MRD. On the contrary, the GKLD assumes a simpler model consisting in the mean value, thus obtaining the same performance as the PKLD.

2) Analysis of the MCPs: some collected multiscale change profiles, obtained by applying $r_{CKLD}$ of eq. (12) to our data set are analyzed. Four different profiles are presented. They are extracted from a change area of the simulated data set for the case of a deterministic texture change and a radius of 10 pixels. These profiles are labeled as follows: Far for the case where the analysis window is located 30 pixels from the center of the change area; Outside border for a distance of 15 pixels; Inside border for a distance of 7 pixels and Inside centered for a distance of 0 pixel. Fig. 8(a) presents a diagram explaining how the profiles are extracted with respect to the change area and fig. 8(b) presents the profiles themselves.

The Far profile shows low values for small window sizes, and these values increase as the window size increases and it begins to include pixels from the change area. The values decrease for large window sizes, since the window stops including new change pixels while including no change pixels present in all directions. The Outside border profile has a similar behaviour, but the CKLD values are high for small scales since the pixel is nearer to the change area. The Inside border profile shows higher values for the change indicator for small window sizes. Finally, the Inside centered profile shows very high values of the detector for a large interval of window sizes. It is worth noting that the CKLD values are nearly the same for all detectors for the largest window sizes, since, at this scale, all detectors include the same proportion of change and no change pixels.

3) MCP exploitation: in this section, the interest of the use of the MCP is illustrated with respect to the selection of a fixed scale of analysis, (i.e. a fixed window size). The MCP allows the best scale to be selected for each pixel location in the images. Here the maximum of the profile is used as a means to select the appropriate scale.

The maximum of the MCP and 2 different scales, $5 \times 5$ and $17 \times 17$ are compared. The small window size is used in order to detect small changes, but its main drawback is that the false alarms may increase in the presence of noise. The larger window size gives a lower false alarm rate since the noise is averaged, and therefore its effect is reduced. But small changes can also be averaged and therefore the detection probability
may be lowered. Also, false alarms may be increased in the neighborhood of the change areas.

The results of the comparison are presented in figures 9, 10 and 11. As expected, small windows are able to give high detection rates. In the case of radiometric shift, the false alarm rates are low, for a given detection probability, since the type of change is easily detected by computing the mean value over a few pixels only. However, when more complex changes occur (figures 10 and 11), the false alarm rate is very high at a given detection probability. Another interesting effect can be observed in figures 9 and 11, where for the large window sizes, the false alarm rate increases without an increase in the detection probability. This is due to the fact that when the window is too large for the small changes and not as large as the larger changes (see the mask in fig. 4(b)), the new detections induce false alarms only in the neighborhood of the small changes.

In addition, the MCP gives results which do not suffer from these drawbacks without the constraint of choosing a window size without prior information on the size of the changes in the images.

VI. EXPERIMENTS WITH REAL DATA

This section shows an example of applications of these algorithms to a real case. A pair of Radarsat images, acquired before and after the eruption of the Nyiragongo volcano (D.R. of Congo) which occurred in January 2002, were used. Fig. 12 shows the two images to be compared and a change map produced using ground measures. The images have a ground resolution of 10 m and cover an area of 4 km by 8 km. The images were ortho-rectified by IGN-F, the French National Geographic Institute, to a UTM35S projection, which was the same as the one used for the reference map. No filtering or calibration was applied to the data.
8 bit conversion was performed using a $3\sigma$ thresholding followed by a linear intensity rescaling. It is worth noting that the image resampling applied in the ortho-registration step modifies the local statistics of the image. Indeed, the image resampling implies local image interpolation which is based on approximate interpolators. A bicubic interpolation was used in this case. This type of filter has a smoothing effect which depends on the local shift [31]. Because of these radiometric artifacts introduced during the geometric pre-processing, the theoretical models for SAR statistics may not hold locally. The area at the bottom right hand corner of the ground truth mask corresponds to an area where a severe mis-registration exists due to the lack of a proper digital terrain model. Finally, one has to take into account the fact that the ground truth is not perfect and that all results presented in this section should be analyzed rather in a relative manner – one detector with respect to another – rather than in an absolute one – absolute value of detection probabilities.

A. Change indicator

The comparisons between the result coming from the classical image intensity ratio and the method proposed in this paper are shown in fig. 13. Fig. 14 gives the ROC plots using the ground truth of fig. 12(c). It shows that the use of KL approximation by the Edgeworth series outperforms any other methods such as model-based (Gaussian-based or Pearson-based) KL distance, or the ratio measure. As stated in the introduction, a miss-detection behaviour of this detector can be observed because it uses the mean pixel values only. It is interesting to underline the fact that the ratio criterion is not always worse than pdf-based criteria. In fact, a density model has to fit the data in order to yield pertinent results.

For a detection probability below 0.3, it is more interesting to use the ratio criterion instead of a model-based one (by using Gaussian or Pearson assumption) in this example, even if a better change detection could have been expected by using Gaussian or Gamma laws coming from local analysis of the two Radarsat images.

This point confirms that it is more interesting, for operational use, to consider a more flexible pdf approximation by using the Edgeworth series instead of a pdf parameterization. The cumulant-based approximation may give equivalent results to the Pearson-based approximation if the estimated cumulants correspond to a pdf belonging to the Pearson system of distributions, even though it may be less appropriate in the case of heavy tailed distributions (single look data). If cumulants of orders 3 and 4 vanish, the Edgeworth series is equivalent to a Gaussian model. If the variance of $X$ and $Y$ are equivalent, the Edgeworth series yields the same behavior as the ratio measure. However, when the local observations $X$ and $Y$ to be compared do not fit an a priori model, the Edgeworth series becomes a more suitable tool.

Fig. 15 draws the minimum distance of ROC curves to the point $(P_d = 1, P_{fa} = 0)$. It is an interesting point of view to evaluate the threshold to be applied to obtain the best trade-off between detection and false alarms. The best value of the threshold is to be found at the minimum of the curves.

Fig. 15 shows that this minimum is lower – and therefore, more interesting – for the Edgeworth series than for the Pearson measure or the ratio detector.

When no ground truth is available, the end-user has no a priori knowledge to set the value of the threshold. In this case the Pearson measure seems to be better since a trivial value of zero could be used (i.e. pixels with values greater to 0 may be considered as a change). Unfortunately, simulations and comparisons with other sets of images have shown that this trivial threshold is very sensitive to noise and fluctuates. The same observations about sensitivity hold for the ratio measure. On the contrary, the cumulant-based measure takes its minimum for a wider range of values. Therefore, a threshold chosen a priori from the interval $[40, 50]$ gives an almost optimal change map for all cases.
B. Multiscale change indicators

As stated in section IV-B, our goal here is not to find the optimal way of exploiting the MCP, but only to show the interest of the concept with simple examples. The results presented here use an MCP with window sizes ranging from 29 × 29 to 51 × 51.

In order to select the appropriate analysis window for each pixel in the image, we will choose the maximum of the MCP. The resulting change image is shown in fig. 16(a). Fig. 17(a) presents the histogram of the sizes of the selected analysis windows when using the maximum of the MCP. It is interesting to observe that there is a high variability of window sizes, meaning that no trivial choice exists, like for instance choosing the largest window in order to increase the number of samples. Nevertheless, two peaks may be observed in the histogram. The first maximum gives the limit of the resolution of the detector and corresponds to areas near the borders of the change and no change classes. The second one corresponds to homogeneous areas where the window size could continue increasing. Fig. 17(b) shows the map of the selected scales. The histogram bounds of fig. 17(a) are linearly mapped to the minimum and maximum values of the image. It is interesting to note that large windows are used inside the change and no change areas and that small window sizes are selected near the boundaries of these areas.

The ROC plots of fig. 18 show that this simple strategy improves the results with respect to the case where the 35 × 35 window was used.

As an approach to multiscale fusion, we propose here to use the first principal component of the stack of multiscale detection images. The obtained change image is presented in fig. 16(b). The ROC plot of fig. 18 shows that this approach also provides better performance than the monoscale detector.

VII. DISCUSSION AND CONCLUSION

In this paper a new similarity measure between images has been introduced in the context of multitemporal SAR
image change detection. This measure is based on the use of the cumulant-based series expansion of the local image statistics combined with the Kullback-Leibler divergence. The concept of multiscale change profile has been developed and a fast and efficient implementation has been proposed. Finally, two simple approaches for the production of change images containing multiscale information have been presented. The first one is based on the selection of the scale which gives the highest change indicator, and the second one uses the first principal component of the multiscale change image stack.

The proposed similarity measure has been compared to the classical ratio of local means, and also to other Kullback-Leibler detectors which use parametric models (Gaussian- or Pearson-based). The experiments have been carried out on simulated and real data for which a reference change map was available.

The proposed original cumulant-based detector has been shown to have a more robust behavior than other detectors in terms of receiving operator characteristics. The two simple yet useful schemes for the exploitation of the multiscale change profile provide better performance than the monoscale detector.

The main advantages of the proposed approach are the following: our detector needs only the computation of the first 4 statistical moments and can deal with a great variety of pdfs; the multiscale change profile provides change information over a wide range of scales at very low computation cost.

Some improvements could be done in order to use this approach with single-look images, where the heavy tailed distributions may need other statistical models. The use of Gamma distributions instead of Gaussian for the series expansion seems to be a good starting point.

Some questions still remain open about the use of multiscale change profiles. Indeed, it would be interesting to analyze if we could establish a classification of the profiles and thereby derive useful information, not only about the scale of the change, but also about its type. This task could be carried out by visual inspection, but automatic clustering techniques, like for instance the Self Organising Map [32] could be used. The parametric modeling of the profiles by projection on an orthogonal basis could be envisaged.
Another issue remaining is the automatic thresholding of the change images. Whether it be for the case of a single scale, or for the case of a multiscale analysis, the statistics of the change indicators could be used in order to propose adaptive Bayesian thresholding techniques, as done in [13].

Finally, direct classification of multiscale profiles by using Support Vector Machines seems an appropriate choice for the production of binary change maps in the case of supervised change indicators could be used in order to propose adaptive change images. Whether it be for the case of a single scale, INGLADA AND MERCIER: THE MULTI-SCALE CHANGE PROFILE: A STATISTICAL SIMILARITY MEASURE FOR CHANGE DETECTION 13

References


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