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Evaluation of Pointing Performance on Screen Edges

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ABSTRACT
Pointing on screen edges is a frequent task in our everyday use of computers. Screen edges can help stop cursor movements, requiring less precise movements from the user. Thus, pointing at elements located on the edges should be faster than pointing in the central screen area. This article presents two experiments to better understand the foundations of "edge pointing". The first study assesses several factors both on completion time and on users’ mouse movements. The results highlight some weaknesses in the current design of desktop environments (such as the cursor shape) and reveal that movement direction plays an important role in users’ performance. The second study quantifies the gain of edge pointing by comparing it with other models such as regular pointing and crossing. The results not only show that the gain can be up to 44%, but also reveal that movement angle has an effect on performance for all tested models. This leads to a generalization of the 2D Index of Difficulty of Accot and Zhai that takes movement direction into account to predict pointing time using Fitts’ law.

Categories and Subject Descriptors
H.5.2 [Information Systems]: Information Interfaces and Presentation (e.g., HCI) – User Interfaces, Input Devices and Strategies

Keywords
Edge pointing, Screen Edges, Fitts’ Law, performance modelling

General Terms
Human Factors, Experimentation, Performance

1. INTRODUCTION
Common graphical desktop environments display a number of interactive widgets along the physical edges of the screen. Microsoft Windows\textsuperscript{\textcopyright} and several X Window environments, e.g., GNOME and KDE, feature a task bar. This task bar contains buttons to navigate among application windows, and shortcuts to the files and applications used most often. It is also used to display notification icons, current time, sound controls or system status. Mac OS X\textsuperscript{\textcopyright} displays the menus of the foreground application and some notification icons in a menu bar that is always at the top of the screen. It also features a dock holding icons to quickly launch frequently used files and applications. Users can change the task bar or dock location but the system constrains them to one of the four physical edges of the screen (three for Mac OS X because of the menu bar).

Placing widgets along the edges makes it easier for users to organize their workspace, i.e., their windows and icons, in the central area of the screen without occluding these widgets. However, it also maximizes the distance between the working area and these “edge widgets”. Since Fitts’ law \cite{fitts1954}, predicts that the larger the distance between the cursor and a target, the longer the time to reach that target, edge widgets may impede pointing performance.

While pointing in the central screen area has been extensively studied and Fitts’ law has been shown to hold in most cases, e.g. \cite{fitts1954, beaudouin2005}, the situation with targets located on screen edges may be different. A typical pointing movement is composed of two main phases: an acceleration phase at the beginning of the movement and a deceleration phase at the end of the movement to stop the cursor within the target bounds \cite{beaudouin-lafon2006}. Figure 1(left) shows the typical profile of the speed curve for pointing at a “regular” target. When pointing at an edge target, however, users can take advantage of the physical boundary to stop the movement. They only have to stay within the bounds of the target along the direction collinear to the edge, while maintaining a high speed (prone to overshooting) along the main movement direction. Figure 1(right) shows the expected speed curve when pointing at a target on a screen edge. Accordingly, edge pointing should be faster than “regular” pointing. The intuition that pointing at edge widgets should be faster has already been noted, e.g., \cite{beaudouin-lafon2006}, Chapter 4, or \cite{beaudouin-lafon2004}, but, to the best of our knowledge, it has never been empirically tested. Thus, we do not know if users can perceive the potential advantage and actually use edges in practice.

![speed-time diagram](image)

**Figure 1:** Speed curves for regular pointing (left) and for edge pointing (right).
In this article, we present two experiments to better understand edge pointing and help interface designers in their desktop layout choices. The first experiment identifies the relevant factors involved in an edge pointing task and measures their effects on mouse movements and pointing performance. Results show that some factors such as cursor shape or movement direction have an impact on completion time and the use of edges. The second experiment quantifies the gain of using edges by comparing edge pointing with regular pointing and crossing [1]. It shows that movement angle has a strong effect on performance in all three cases and that differences between models increase with angle. We then propose a generalization of the 2D Index of Difficulty of Accot and Zhai [2] that captures the relation between pointing difficulty and movement direction to provide better predictions of pointing performance.

2. RELATED WORK

Regular pointing has been extensively studied and providing a full review of the literature is beyond the scope of this article. Since we are interested in identifying relevant factors that influence completion time of an edge pointing task, we give an overview of factors that have already been tested in regular pointing and the main findings of these studies.

The most common way of studying pointing is to measure movement time (MT) according to Fitts’ Index of Difficulty (ID) on a one-dimensional pointing task [9]. Fitts’ ID is a function of the ratio of two other factors: the distance to the target (D) and the width of the target (W):

\[ MT = a + b \cdot ID, \quad \text{where} \quad ID = \log_2 \left( \frac{D}{W} + 1 \right) \]

This law means that the larger and the closer the target, the shorter the time required to point at it. Numerous studies have validated this model, see [14] for a review.

Over the past fifteen years, a number of studies have attempted to refine this model by taking into account other factors that might influence pointing performance in a realistic two dimensional environment. Since many targets are rectangular, a number of models of 2D pointing have been proposed. For example, MacKenzie and Buxton compared several models [15] and found that \( ID_W \) and \( ID_{min} \) were the most promising, with \( ID_{min} \) providing slightly better predictions:

\[ ID_W = \log_2 \left( \frac{D}{W} + 1 \right) \quad (1) \]
\[ ID_{min} = \log_2 \left( \frac{D}{\min(W,H)} + 1 \right) \quad (2) \]

Accot and Zhai [2] criticized the similar importance attributed to target width and height in these models. They proposed a more complex model, noted \( ID_{ac} \) in this article, that assigns a specific role to each of these two dimensions, and showed that it provides better predictions. They define target width as the side collinear to the movement direction, i.e., the amplitude constraint, and target height as the side orthogonal to the movement direction, i.e., the directional constraint. Each of these dimensions makes its own contribution to the task difficulty. In their study, \( p = 2 \), \( \omega = 1 \) and \( \eta = \frac{1}{2} \) were the best values for the three free parameters:

\[ ID_{ac} = \log_2 \left( \omega \left( \frac{D}{W} \right)^p + \eta \left( \frac{D}{H} \right)^{\frac{1}{2}} + 1 \right) \quad (3) \]

Regarding movement direction, the ISO9241-9 standard for evaluating pointing devices [12] recommends to lay out targets in a circular pattern and to impose a specific order of appearance that forces participants to perform movements in every direction to obtain results that are valid whatever the movement direction. However, some studies have attempted to isolate and measure the effect of movement angle on completion time. Mackenzie and Buxton [15] used three different angles (0, 45 and 90 degrees) and found that moves along the horizontal and vertical axes were about the same while moves along the diagonal axis took 4% longer. Grossman and Balakrishnan [10] tested angles 0, 22.5, 45, 67.5 and 90 degrees and found that users were the fastest in horizontal movements. To our knowledge, the studies that have tested a wider range of angles have not given more fine-grained results. For example, Whisenand and Emurian [20] found that diagonal movements were slower than straight movements and that horizontal movements were the fastest. Hancock and Boot [11] and Boritz et al. [7] also tested angles all around the cursor with both left and right-handed users and found that movements to the right were the fastest with the right hand for right-handed users and a symmetric result for left-handed users.

Finally, a few studies have measured the effect of other factors such as target feedback or cursor shape. Akamatsu et al. [3] compared five different sensory feedback conditions (no feedback, auditory, colour, tactile, and a combination of the three). They found that feedback of any type decreases the final positioning time (between entering the target an selecting it) but has no significant effect on overall completion time. Regarding cursor shape, Po et al. [17] compared a circle cursor and four arrow cursors (upper-left, upper-right, lower-left and lower-right) and showed that (i) an arrow cursor is more efficient when it is oriented in the direction of movement and that (ii) a circle cursor is the most efficient on average and its performance is independent of the movement angle.

3. STUDY 1: RELEVANT FACTORS

The goal of Experiment 1 was to measure the effect of variables involved in an edge pointing task. First, since it is a pointing task, we tested the effect of two common variables: Index of Difficulty (ID) and movement angle. Second, we tested the effect of variables that can help users feel the edges. While interacting with a direct input device such as a stylus provides a physical feedback of screen edges, indirect input devices such as a mouse, which are commonly used with desktop interfaces, do not have this property. Let us see what happens in today’s standard desktop interfaces.

The standard arrow cursor, which points toward the upper left, leads to a situation where only one pixel (the tip of the arrow) is (barely) visible when the cursor is located at the very bottom or right edge of the screen (Figure 3c). This could reduce the potential gain of using edges since users have to perform a visual search to make sure that they are on the right target (and possibly additional movements to locate the cursor). This probably explains why, in such situations, additional feedback is added to the target under the cursor. For example, on Windows XP, the task bar icon under the cursor is slightly highlighted. On the contrary, Macintosh menus, which are always located at the top of the screen do not provide any additional feedback (until the mouse is clicked) since the cursor remains completely visible even when moved as far up as possible (Figure 2b).

In this experiment, we considered three factors specific to edge pointing. First, we considered targets on the top (North) and bottom (South) edges. While the task bar and the Mac OS X dock can
be on the left or right edges as well, we omit these cases to simplify the design and leave them for future work. The important point is that we have a condition where the arrow cursor almost disappears (South) and one where it is always visible (North). The second factor is target feedback: either targets are highlighted when the cursor is over them, or they are not. The third factor is the cursor type. We tested the traditional arrow cursor as well as a circle cursor. The circle cursor is symmetric and its hotspot is at its center. It remains visible whichever edge it is pushed against (Figure 3). This factor will help assess whether the observed effects of Angle and Edge are due to the arrow cursor orientation.

3.1 Apparatus
The experiment was run on a 2.66 GHz bi-processor PC running Linux with a Nvidia Quadro FX 1000 graphics card connected to a 1680 × 1050 LCD display (99 × 98 dots per inch). We used a standard optical mouse with the default linear X Window acceleration. Our program was implemented in Java using the Touchstone run platform [13] and the SwingStates Toolkit [4].

3.2 Subjects
Twelve unpaid adult volunteers (11 male, 1 female), from 24 to 34 year-old (average 27.92, median 27), all right-handed, served in the experiment.

3.3 Task and Experiment design
Our experiment was a 2 × 2 × 2 × 7 within-participant design. The following list summarizes the factors we tested:

- 2 Cursor conditions: arrow and circle,
- 2 Feedback conditions: highlight and none,
- 2 Edge conditions: top edge or bottom edge,
- 4 Width conditions: 20, 50, 100 and 200 pixels,
- 7 Angle conditions: -90, -60, -30, 0, 30, 60 and 90 degrees.

We used different angles and target widths to study edge pointing in a realistic context of use. -90, -60, -30, 0, 30 and 60 degrees cover a good range of situations when the user is working at arbitrary screen locations. We also included -90 and 90 degrees to represent the frequent situation where a user moves the cursor horizontally to switch among window icons in a task bar or to explore different menus in the menu bar. For target widths, 20 pixels is roughly the size of a notification item while 50, 100 and 200 pixels represents a range of sizes for icons in the task bar or menus in the Mac OS X menu bar. To limit the number of trials, we used a fixed distance of 500 pixels and a fixed height of 20 pixels for the target (which is the typical height for a menu item or an icon in the task bar). Figure 4 illustrates the simple task participants had to perform: first click on a circular starting point and then click on the target. The next trial started only when the participant had clicked the target, i.e. every trial had to end successfully even if it included clicks outside the target.

We grouped trials into blocks according to the Cursor × Feedback condition, each block containing the 56 combinations Edge × Width × Angle. To counterbalance the presentation order of Cursor × Feedback blocks, we used a Latin Square to compute 4 presentation orders per participant, resulting in a design containing 4 trial replications per participant. Each participant thus executed 16 blocks. Each block was divided into two series, one per Edge condition. We divided our participants into two groups of six participants. Participants in the first group performed these series in the order top then bottom while participants in the second group performed them in the order bottom then top. Within a series, participants had to perform 28 trials per Width × Angle condition, presented in a random order (4 × 7 = 28 trials). Thus, the total number of logged trials in our experiment was: 16 blocks × 2 series × 28 trials × 12 participants = 10752 trials. Before starting the experiment, participants were instructed to point as fast and as accurately as possible and had to perform a series of trials with a sample of all the conditions they would face during the experiment.

Our software collected three main measures: completion time, number of “errors” (clicks outside the target) and click position.

3.4 Predictions
Before running the experiment, we made the following predictions:

$H_1$: circle cursor is more efficient than arrow cursor for Edge = bottom because of the visibility problem caused by arrow cursor.

$H_2$: Feedback = highlight is more efficient than Feedback = none especially in condition Cursor = arrow × Edge = bottom. Feedback should help users quickly perceive that they are in the target, making them more confident and avoiding a costly visual search for cursor location.

$H_3$: As in regular pointing, the larger the target, the shorter the completion time. Since we use a single target height and hypothesize

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1Note that we do not use the same Latin Square for each participant so as to ensure that within a group of 6 participants, the $4! = 24$ possible orders are presented.
that participants will use edges to stop their movement, completion time should be a linear function of \( ID_e = \log_2(1 + \frac{D}{\text{width}}) \). Contrary to Accot and Zhai [2] who defined width and height according to movement angle, we consider that target width is always the length of the target side collinear to the screen edge.

### 3.5 Results

We collected a total of 10752 trials. 690 of them included clicks outside the target (error rate = 6.41%). We did not remove these trials for our analyses since participants had to end each task successfully (errors are thus included in task completion time as a penalty).

There was a significant learning effect: Block number has a significant effect on completion time \((F_{31,341} = 2.4, p < 0.001)\) and completion time decreases according to Block number. This should not affect the validity of our analyses since our counterbalancing strategy ensured that each condition appeared in every position across participants. This is supported by an analysis of variance that did not reveal an effect of presentation order on completion time: the interaction effect Block number × Cursor × Feedback on completion time is not significant.

![Figure 5: Mean time as a function of \( ID_e \) by Edge × Cursor](image)

Analysis of variance did not reveal a significant effect of \( ID_e \) on task completion time but revealed a strong interaction effect of \( Edge \) × \( Cursor \) on task completion time \((F_{1,11} = 65.2, p < 0.0001)\). Tukey post hoc tests showed that \( bottom \times circle \) is significantly faster than \( bottom \times arrow \) (a difference in mean of 40 ± 6 ms representing a speed up of 6.5%) and that \( top \times arrow \) is significantly faster than \( top \times circle \) (a difference in mean of 19 ± 6 ms representing a speed up of 3.4%). We found no significant difference between \( bottom \times circle \) and \( top \times circle \). These results support hypothesis \( H_1 \). \( H_3 \) is also supported since we observed a significant simple effect of \( ID_e \) on task completion time \((F_{3,33} = 262.8, p < 0.0001)\). Figure 5 illustrates these results.

Hypothesis \( H_2 \) however is rejected since there was no significant effect of Feedback on task completion time (nor any significant interaction effect of Feedback with any other factor on completion time). Analyses of the number of errors revealed that Feedback has a significant effect on number of errors \((F_{1,11} = 20.1, p = 0.0009)\) with participants making significantly more errors in the Feedback=highlight condition (6.5%) than in the Feedback=none condition (5.1%). It seems that providing feedback by highlighting the object under the cursor is more disturbing than helpful in our experimental task. This is consistent with Akamatsu et al. [3] who observed no significant effect of feedback on completion time. We also observed a significant effect of \( ID_e \) on number of errors \((F_{3,33} = 12.8, p < 0.0001)\). This is not surprising since clicking in a small target requires more precision than clicking in a large one. A linear regression of completion time as a function of \( ID_e \), \( MT = 208 + 114.ID_e \), shows a high correlation with an adjusted \( r^2 = 0.992 \) (we consider here 4 mean completion times per \( ID_e \)).

![Figure 6: Mean time (left) and mean number of clicks along the edge (right) by Angle × Cursor](image)

Our analyses showed that movement direction is an important factor for edge pointing. First, participants were faster at pointing upward than downward since we observed a significant effect of \( Edge \) on task completion time \((F_{1,11} = 45.8, p < 0.0001)\). Second, performance varies according to the movement angle: \( Angle \) has a significant effect on task completion time for both edges \((F_{6,66} = 11.8, p < 0.0001 \text{ for } Edge = \text{bottom} \text{ and } F_{6,66} = 4.1, p < 0.0014 \text{ for } Edge = \text{top})\). This is probably because it is easier to use edges to stop when the movement is orthogonal to the edge, i.e. when \( Angle \) is close to 0. Comparing the mean completion time and the mean number of times users stopped on an edge according to the angle of movement supports this interpretation (Figure 6): participants stop more often on an edge for angles close to 0. Note that these results differ from those on regular pointing, in which users are faster in horizontal movements than in vertical ones \([10][15][20]\).

We also observed an \( Angle \) × \( Cursor \) interaction effect on completion time \((F_{6,66} = 6.2, p < 0.0001 \text{ for } Edge = \text{bottom} \text{ and } F_{6,66} = 2.7, p = 0.0202 \text{ for } Edge = \text{top})\). This interaction effect seems stronger for \( Edge = \text{bottom} \) probably because this edge suffers from the cursor visibility problem. Finally, there was a significant \( Angle \times ID_e \) interaction effect \((F_{18,198} = 3.7, p < 0.0001 \text{ for } Edge = \text{bottom} \text{ and } F_{18,198} = 4.1, p < 0.0001 \text{ for } Edge = \text{top})\). The comparison of mean completion times across \( Angle \times ID_e \) conditions revealed that performance is less sensitive to angle for easy pointing tasks, i.e., low IDs, than for difficult ones.

This first experiment revealed that edge pointing exhibits some differences with previous results on regular pointing, especially regarding the effect of movement angle. This is a motivation to further study edge pointing in order to better understand its underlying model and compare it with other models for target selection.
4. STUDY 2: PERFORMANCE GAIN
The goal of Experiment 2 is to identify a model for edge pointing. Our approach consists in comparing edge pointing with well-known models such as regular pointing or crossing, as well as a model that has not been studied yet, i.e., pointing a Semi-Infinite target, and that we hypothesize to be close to edge pointing.

4.1 Candidates for a model

Regular Pointing. In this model, based on Fitts’ law, the user has to stop within the bounds of a finite target and click to select it. Edge pointing follows this model if users do not use edges to stop their movement.

Crossing+Click. Crossing was introduced by Accot and Zhai [1]: a target is a segment, and selection consists in overshooting the target with the pen down. Accot and Zhai showed that crossing a segment whose width is $W$ can be more efficient than pointing a target of width $W$. Crossing follows Fitts’ law but has lower empirical coefficients ($a$ and $b$) when the segment is orthogonal to the movement direction. Crossing and edge pointing share the following property: the user does not have to perform the last part of the movement which consists in precisely stopping within the target. While crossing seems a good candidate to model edge pointing, crossing does not require a click to select the target (the selection is completed as soon as the user has crossed the segment). Therefore, we compare a variant of crossing that we call Crossing+Click which consists in first crossing the target and then clicking to actually select it. A pilot experiment revealed that it was hard for participants to know which target side they had to cross and to be sure that they had actually crossed it when the target was on the edge. Thus, in this experiment, we used a black line to indicate which side to cross (Figure 7a) and the target was highlighted as soon as it had been crossed.

Semi-Infinite Pointing. A close look at current implementations of edge pointing in standard desktop environments shows that mouse movements along the x-axis are still taken into account once the top or bottom of the display is reached. We therefore introduce semi-infinite pointing. Figure 7 illustrates the difference with crossing. If a target is selected by crossing, only the position on the x-axis at crossing time is taken into account. This means that if the cursor has a diagonal trajectory and its speed would make it stop further along the edge, the part of the movement beyond the edge is ignored. On the contrary, if a target is selected by edge pointing, it is the x-position of the cursor when the click occurs that is taken into account to determine which target is selected. Therefore, in an edge pointing task, targets can be seen as semi-infinite, i.e., they are not bounded along the orthogonal direction of the edge. As mentioned earlier, pointing at targets with various $W/H$ ratios has already been studied but only on a limited set of angles (0, 45 and 90 degrees in [15] and 90 degrees in [2]). Each study yielded a formula ($ID_{min}$ and $ID_{eq}$) that does not include the angle of movement.

We hypothesize that edge pointing is close to pointing a semi-infinite target, i.e., pointing a target with a $W/H$ ratio close to zero, and that both models ($ID_{min}$ and $ID_{eq}$) do not capture this configuration properly since Experiment 1 has revealed a significant effect of angle of movement on movement time in edge pointing.

4.2 Task and Experiment design

We used the same hardware and software as in Experiment 1. Eight participants, all having already completed Experiment 1, also served in Experiment 2. The task also consisted in selecting a target but under different model conditions (Figure 8).

To limit the length of the experiment and focus on the study of the underlying model, we did not include Feedback and Cursor as factors in this experiment. Participants had to perform target acquisition tasks with a circle cursor and no feedback. This allowed us to study a wider range of ID. Our experiment was a $4 \times 2 \times 3 \times 2 \times 7$ within-participant design with the following factors:

- 4 Model: Pointing, Crossing, Semi-Infinite and Edging,
- 2 Edge: top edge or bottom edge,
- 3 Width: 35, 70 and 140 pixels,
- 2 Distance: 300 and 600 pixels,
- 7 Angle: -90, -60, -30, 0, 30, 60 and 90 degrees.

The trials were grouped into 12 blocks, 4 Model conditions repeated 3 times. Each Model block was divided into two sub-blocks, one per Edge condition and each of these sub-blocks contained 3 Width × 2 Distance × 7 Angle = 42 trials. The target height was 320 pixels in the Semi-Infinite condition while it was 20 pixels in all other conditions. To counterbalance the presentation order of conditions, we created 4 groups of 2 participants and computed 12 presentation orders for the Model condition using three Latin Squares. We concatenated 3 orders to compose a sequence of 12 blocks so we obtained 4 sequences, one per group of two participants. Within a group, one participant saw this sequence with sub-blocks in the order Edge = bottom then Edge = top while the other participant saw this sequence with sub-blocks in the order Edge = top then Edge = bottom. Finally, the 42 trials of a Model block were presented in a random order. To summarize, the total number of logged trials in our experiment was: 12 blocks × 2 sub-blocks × 42 trials × 8 participants = 8064 trials. As in Experiment 1, participants were instructed to acquire the target as fast and as accurately as possible and had to perform a series of trials with a sample of all the conditions before starting the experiment.
4.3 Results
Before analyzing the results, we first checked that participants did not use the physical edge of the screen in the Semi-Infinite condition in order to avoid a confound with the Edging condition. The cursor reached the edge in only 0.34% of the trials and 99% of mouse clicks occurred within the first 250 pixels of the 320-pixel target.

Learning effect and error rate (6.05%) were similar to the ones observed in Experiment 1. Here again, our design counterbalanced learning effects since we did not observe a significant interaction effect of Block number × Model on completion time.

Analysis of variance revealed a significant effect of Model (F₃,2₁ = 141.3, p < 0.0001) and IDₑ (F₃,2₁ = 440.3, p < 0.0001) on task completion time. We also observed a significant Model × IDₑ interaction effect on task completion time (F₉,₆₃ = 28.7, p < 0.0001). Figure 9 illustrates these results: performance comparison among conditions depends on IDₑ. First, Tukey post hoc tests showed that Crossing+Click is significantly faster than Pointing for easy tasks (i.e. IDₑ = 1.65) and significantly slower than Pointing for difficult tasks (i.e. IDₑ = 4.18). This result is consistent with Accot and Zhai [1]. Second, the difference between Pointing and Edging is larger for easy tasks than for difficult ones: Tukey post hoc tests showed that Edging is significantly faster than Pointing for all IDₑ values, but the difference between mean completion times is 36.8% for IDₑ = 1.65 while it is only 6.8% for IDₑ = 4.18. Focusing our analyses on the Edging and Semi-Infinite conditions, we still observe a significant effect of Model (F₁,₇ = 19.4, p = 0.0031) and IDₑ, but no Model × IDₑ interaction effect (F₃,₂₁ = 2.6, p = 0.0803) on completion time. Tukey post hoc tests showed that Semi-Infinite is significantly faster than Edging with a difference in mean of 26 ± 6 ms, this difference being almost similar across IDₑ.

In summary, Edging and Semi-Infinite seem to follow a similar underlying model for IDₑ and only differ by a small constant. Pointing and Crossing seem to follow different models.

Contrary to Experiment 1, we found no significant effect of Edge

3 A finer analysis considering Width and Distance separately showed that this interaction effect was mainly an effect of Width.
4 And no significant Model × Width and Model × Distance interaction effects when we consider Width and Distance separately.

An analysis of variance also revealed a significant Model × Angle interaction effect (F₁₈,₂₈ = 19.7, p < 0.0001) on completion time as illustrated in Figure 10. First, Pointing is faster for horizontal movements than for vertical movements, while Crossing+Click is faster for vertical movements than for horizontal movements. These results are consistent with the ones reported in previous work: [10] [20] showed that pointing is faster for horizontal movements than the two other angles they tested and [1] showed that crossing an orthogonal goal is faster than crossing a collinear goal in a continuous movement. Second, differences between Pointing and both Edging and Semi-Infinite are higher for vertical movements (i.e. Angle close to zero). For instance, Tukey post hoc tests showed that Edging is significantly faster than Pointing for Angle = 0 (a speedup of 34.0%) while there is no significant difference for Angle = ±90. This is probably due to the “virtual” target height in the Edging condition that offers a lower amplitude constraint for angles close to 0 than for angles close to 90 or -90. The histogram in Figure 11 supports this interpretation: it plots...
the “virtual” y-coordinate\(^7\) of the cursor at target selection time according to Angle in the Edging condition and shows that participants stopped their movement further away for angles close to 0 (i.e. vertical movements).

In summary, Edging and Semi-Infinite seem to follow a similar underlying model for Angle while Pointing seems to follow a different one. This result also supports our hypothesis regarding the similarity between the underlying models of Edging and Semi-Infinite.

5. DISCUSSION

The first important finding of this study is that users do take advantage of edges to facilitate target acquisition. Our analyses reveal that acquiring a target on an edge is similar to acquiring a target with a very large height: completion times for both tasks follow a similar function in terms of ID\(_x\) (Figure 9) and Angle (Figure 10).

The second important finding is that pointing at a target on an edge is quite different from pointing at the same target in the middle of the screen. First, the relationship between movement time and ID\(_x\) is different for the two conditions: while in both cases it is an increasing function of ID\(_x\), differences between regular pointing and edge pointing are much larger for low ID\(_x\) values than for high ones (Figure 9). Second, the relationship between movement time and movement direction is different: for edge pointing, movement time seems to be a linear increasing function of the absolute value of Angle while for edge pointing, it seems to be a linear decreasing function of the absolute value of Angle. This results in performance differences between regular pointing and edge pointing between +33 ± 49 ms (i.e. 4.4% of movement time) and −278 ± 20 ms (i.e. 44.6% of movement time).

As far as we know, the only model that takes movement direction into account is ID\(_W\) \(= \text{eq. 1}\), which was introduced with ID\(_{min}\) \(= \text{eq. 2}\) by Mackenzie and Buxton \(\textbf{[15]}\). In their study, ID\(_W\) was shown to be less accurate than ID\(_{min}\). Accot and Zhai \(\text{[2]}\) raised issues with both models and introduced ID\(_{ref}\) \(= \text{eq. 3}\). The table below reports the linear regressions of completion times as a function of ID using each of these models (we consider the 42 mean completion times per condition Angle \(\times\) Distance \(\times\) Width for a given Model\(^6\)):

<table>
<thead>
<tr>
<th>Model</th>
<th>MT (= a + b\ ID_W)</th>
<th>MT (= a + b\ ID_{min})</th>
<th>MT (= a + b\ ID_{ref})</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>a</td>
<td>b</td>
<td>r(^2)</td>
</tr>
<tr>
<td>Edging</td>
<td>205</td>
<td>127</td>
<td>0.80</td>
</tr>
<tr>
<td>Semi-Infinite</td>
<td>178</td>
<td>129</td>
<td>0.80</td>
</tr>
<tr>
<td>Pointing</td>
<td>233</td>
<td>106</td>
<td>0.73</td>
</tr>
</tbody>
</table>

Since ID\(_W\) contains three free parameters, we tested different combinations for \(\omega \in [0.10] \times \eta \in [0.10] \times p \in [0.12]\) with a step of 0.1 for \(\omega\) and \(\eta\). Since the simple values \(\omega = \eta = p = 1\), corresponding to ID\(_W\) = \(\text{log}_2(p + f(|\text{Angle}|) / \text{min}(W, H) + 1)\), did not provide noticeably worse correlation coefficients, we use these values in the table.

Once again, these results support the hypothesis that Edging and Semi-Infinite follow the same underlying model but differ from traditional Pointing. The correlation coefficients however are not as good as for regular pointing, calling for a more detailed analysis.

\(^5\)Even though the cursor is graphically blocked on the edge, we recorded input events directly from the mouse to compute the “virtual” off-screen location at target selection time.

\(^6\)For Edging and Semi-Infinite, we approximate “infinite” height to 250 pixels, i.e. the height of the area that contains 99% of mouse clicks in the Semi-Infinite condition (see Section 4.3).

Let us come back to the notions of amplitude and directional constraints defined by Accot and Zhai \(\text{[2]}\). The Amplitude constraint is the interval within which the user must stop along the movement direction while the Directional constraint is the interval within which the user must stop along the direction orthogonal to the movement. In their study, Accot and Zhai only evaluated non-diagonal movements, so these constraints were simple functions of target width and target height. Figure 12 suggests that taking movement direction into account should help describe the task more accurately. We propose to introduce movement direction in the ID\(_{ref}\) model based on two ideas mentioned by Accot and Zhai \(\text{[2]}\): (i) satisfying an amplitude constraint takes more time than satisfying a directional constraint and (ii) the shortest side must dominate the ID.

To this end, we add a term that emphasizes the contribution of the shortest side to the ID, and we make this term a function of |Angle|. Figures 10 and 12 show that the larger the difference between the orientation of the shortest side and movement direction, the smaller the amplitude constraint. In the Edging and Semi-Infinite conditions (where \(W\) is the shortest side), this difference is an increasing function of |Angle| while in the Pointing condition (where \(H\) is the shortest side), this difference is a decreasing function of |Angle|. We therefore propose the following model where the |Angle| term captures the relationship between orientation of the shortest side and movement direction:

\[
\text{ID}_{\text{Angle}} = \log_2\left(\frac{D}{W} + \frac{D}{H} \times f(|\text{Angle}|) \times \frac{D}{\text{min}(W, H)} + 1\right)
\]

\(f(|\text{Angle}|) = 0.6 \times \sin(|\text{Angle}|)\) for Edging and Semi-Infinite \(f(|\text{Angle}|) = 0.6 \times \cos(|\text{Angle}|)\) for Pointing

The table below and Figure 13 show that ID\(_{\text{Angle}}\) provides much better predictions than the other models studied above:

<table>
<thead>
<tr>
<th>Model</th>
<th>MT (= a + b\ ID_{\text{Angle}})</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>a</td>
</tr>
<tr>
<td>Edging</td>
<td>−57</td>
</tr>
<tr>
<td>Semi-Infinite</td>
<td>−82</td>
</tr>
<tr>
<td>Pointing</td>
<td>−335</td>
</tr>
</tbody>
</table>

To select the functions \(f(|\text{Angle}|)\), we balanced a trade-off between simplicity and prediction accuracy after systematically considering the following functions: \(x \times |\text{Angle}|\) for Edging and Semi-Infinite and \((x \times |\text{Angle}|) - x \times \sin(|\text{Angle}|)\) for Edging and Semi-Infinite and \((x \times |\text{Angle}|) - x \times \cos(|\text{Angle}|)\) for Pointing, with \(x \in [0, 10]\) with a precision of 0.05.
6. CONCLUSION AND FUTURE WORK

We have presented an empirical study to better understand pointing at targets on screen edges. We have also proposed an analysis of the differences between regular pointing and edge pointing and shown that the angle of movement affects the amplitude constraint for a rectangular target. In order to account for these differences with Fitts’ law, we have extended Accot and Zhai’s definition of index of difficulty (ID) for bivariate pointing. While our model provides better predictions in the study presented here, its validity must be further tested by considering larger sets of target heights and edge orientations, i.e., left and right as well as top and bottom.

Having assessed the effect of various factors on edge pointing performance and compared different pointing models, we can draw the following recommendations to improve current desktop environments. First, the cursor should always be visible even when located on a screen edge. We have shown that a circular cursor shape does improve performance but that target highlighting does not. Other alternatives worth exploring in future work include displaying a small halo around the cursor when it is on the edge or having virtual edges within a few pixels of the physical edges so that the cursor does not move to the physical edge and stays visible. Second, we encourage the use of edges for placing a widget if this does not significantly affect its average distance to the cursor in a typical context of use. The edge creates a “semi-infinite” target that can be acquired up to 44% faster than a regular target at the same distance in the central screen area. Third, we found that movements orthogonal to a given edge, i.e., with a zero angle, afford better performance. Designers should therefore lay out frequently used “edge widgets” close to the center of the edge. Note, however, that we have not tested the special case of corners, which are probably even faster to acquire than edge widgets.

Another research direction for this work is to explore whether “virtual” edges, such as the borders of a window, that would block the cursor under certain conditions, could also improve selection time in specific situations. Obviously, it is important to clearly identify when and how to activate and deactivate such virtual edges so that the user can easily access the rest of the screen. One idea would be to activate the virtual edges while transient graphical components, e.g., a pop up menu, are displayed.

7. ACKNOWLEDGEMENTS

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8. REFERENCES