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3D Edge Bundling for Geographical Data Visualization

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Abstract
Visualization of graphs containing many nodes and edges efficiently is quite challenging since representations generally suffer from visual clutter induced by the large amount of edge crossings and node-edge overlaps. That problem becomes even more important when nodes positions are fixed, such as in geography were nodes positions are set according to geographical coordinates. Edge bundling techniques can help to solve this issue by visually merging edges along common routes but it can also help to reveal high-level edge patterns in the network and therefore to understand its overall organization. In this paper, we present a generalization of [18] to reduce the clutter in a 3D representation by routing edges into bundles as well as a GPU-based rendering method to emphasize bundles densities while preserving edge color. To visualize geographical networks in the context of the globe, we also provide a new technique allowing to bundle edges around and not across it.

1 Introduction
International air interconnections, as well as theirs analysis, are becoming more and more dense and complex. Complexity of air traffic networks drives the need for visual analysis techniques which aim at solving three main issues:

- Emphasize major trends in air traffic and highlight most important airports.
- Determine interconnected but also interdependent regions.
- Show worldwide air traffic organizational schemes.

To answer these questions, an intuitive modeling of such a network consists in using a graph where nodes represent airports and edges interconnections between these airports. International air traffic visualization raises a very strong constraint, namely geographical positioning of airports. Indeed, when dealing with international air traffic, nodes positions cannot be changed as they bring some information. This makes unusable classical approaches where nodes positions are computed by a drawing algorithm to emphasize central airports and/or important patterns. In that case, information discovery becomes difficult as edge crossings and node-edge overlaps clutter the representation. Reducing the clutter in such data representation is therefore of utmost importance to identify relationships and high-level edge patterns of the network.

In the past, clutter reduction had been achieved using three main techniques: compound graph visualization, edge routing and edge bundling. In a compound graph visualization (e.g [20, 1, 2]), the original network is abstracted by collapsing clusters into metanodes and the result is then displayed on the screen. This technique reduces the cluttering of the representation as inter-cluster edges are merged into metaedges. However, the compound visualization is not suitable for geographical data visualization as nodes positions cannot be changed and therefore as clusters may overlap.

To increase the readability of a graph representation, the graph drawing community offers techniques to reduce the number of edge crossings and node-edge overlaps by routing edges (e.g. [8, 10, 24, 11]). Among these techniques, one can find the confluent drawing method (e.g [8]) but also heuristics based on the visibility graph and shortest path edge routing (e.g [10, 24, 11]). These approaches efficiently reduce edge clutter by either reducing edge crossings or avoiding node-edge overlaps. However they do not help the user to identify high level edge patterns and therefore to understand the overall organization of the network.

Recently, edge bundling techniques [19, 15, 4, 7, 16, 18] are of increasing interest in the graph visualization community. Under the spotlight by Holten [15], this technique routes edges into bundles in order to uncover high level edge patterns and to emphasize relationships in a 2D representation of the network.

In this paper, we focus on a novel approach to generate 3D edge-bundled representations of graphs, this approach generalizes the work of Lambert et al. [18]. We introduce an intuitive edge bundling algorithm which efficiently reduces edge clutter in graphs drawings. Our method discretizes the space into regions. Boundaries of these regions are used as roads to route edges. The main contribution of this paper is therefore a new 3D edge bundling
technique that avoids node-edge overlaps. We also present GPU-based rendering method which enables users to perceive bundle densities while preserving edge color.

The remainder of this paper is structured as follows. Section 2 reviews related work on edge clutter reduction methods and techniques to enhance edge bundles visualization. In section 3, we present the main steps of our method and several implementation issues. Section 4 refers to rendering techniques necessitated by edge bundling visualization. We then present some results on 2000 and 2004 international air traffic in section 5. Finally, we draw a conclusion and give directions for future work.

2 Related work

As mentioned above, we focus in this paper on a 3D representation of edges whose extremities have fixed positions. In this section, we present existing methods for edge clutter reduction but also techniques for enhancing edge bundles visualization. For a general overview of clutter reduction techniques and not only edge clutter reduction techniques, we recommend the survey of Ellis and Dix [12].

2.1 Edge Clutter reduction

Most of the previous work focused on clutter reduction in 2D representation of the graph. Even if some of the following techniques can be adapted to take the third dimension into account, Balzer and Deussen presented in [4] the only technique (to the best of our knowledge) for clutter reduction in a 3D representation. 

**Edge routing:** One of the first attempts to reduce clutter in graphs drawings was made by the graph drawing community. Indeed, to increase the readability of a graph representation, one can try to reduce the number of edge crossings but also to avoid node-edge overlaps (to use non-point-size nodes for instance). In [10], Dobkin et al. give a novel method using visibility graphs and shortest-path edge routing to remove node-edge overlaps. The technique was ported to tangent visibility graphs by [24]. Finally, Dwyer and Nachmanson [11] give a fast heuristic to compute an approximation of the visibility graph to reduce the time complexity of the approach and therefore to support large graph edge routing. These approaches efficiently reduce edge clutter by avoiding node-edge overlaps, however they do not help the user to identify high-level edge patterns.

**Interactive techniques:** Wong et al. give in [23, 22] interaction techniques to remove clutter around the user’s focii. Edges close to one of the focii are pushed away in a fisheye-like manner while preserving nodes positions. The representation is locally uncluttered around each focus, but this technique does not reduce the clutter of the entire representation. Therefore, it does not help in understanding the overall organization of the network.

**Edge bundling:** Phan et al. present in [19], a flow map layout technique based on geometrical node clustering. Edges are routed along the hierarchy tree branches. This idea has also been used by Holten in [15] to enhance relationship in hierarchical (and relational) data. Balzer and Deussen [4] present a multilevel compound visualization technique similar to [15] to render an hierarchical clustering in a 3D visualization. Then the transparency of each implicit surface and the bundling “factor” are dynamically updated according to the distance to the viewpoint resulting in a smooth animation when zooming in or out on a focus cluster. The main drawback of these methods is that edges are routed using a hierarchy tree which can be restrictive in the general case.

In [13], Gansner and Koren give an improved circular layout algorithm where edges are routed either on the outer face of the circle or in its inner face. Edges routed inside the circle are bundled using an edge clustering algorithm that tries to optimize area utilization. Another edge clustering method is given by Cui et al. [7]. In this paper they propose a geometric approach to create bundles of edges. The main idea is to build a control mesh based on user interaction or a Delaunay triangulation. The mesh is then used to compute regions where edges should be merged. The merging of edges is done according to a clustering algorithm based on the orientation of edges. Finally, Holten and van Wijk introduced in [16] a force-directed heuristic to bundle edges and therefore, to unclutter a representation of a graph where nodes positions are fixed. In this heuristic, dummy nodes are inserted to split edges into segments. A similarity measure between edges is computed to determine which of them should interact. Dummy nodes of any two interacting edges are linked by inserting dummy edges. Bundles are obtained by running a force-directed algorithm preserving positions of the original nodes.

Recently, Lambert et al. [18] presented a novel approach for bundling edges in order to unclutter 2D drawing but also reveal high-level edge patterns. The technique is based on plane discretization and shortest path edge routing. In this paper, we present a generalization of this technique to 3D representation of graphs.

2.2 Enhancing edge-bundled graph visualizations

**Smoothing curves:** The main feature common to each edge-bundled graph visualizations is the drawing of edges as curves. Indeed, rendering graph edges as curves makes the task of following them easier and gives a more visually appealing graph drawing. In [15], Holten renders bundled edges piecewise with cubic B-splines. In [25], Zhou et al. use others models of splines to render bundled edges which are Bézier curves and Catmull-Rom splines. Another method used by Holten et al. [16] and by Cui et al. [7]
is to apply a smoothing technique on the edges drawn as polylines to morph them into curves.

**Coloring edges:** Another mean of enhancing edge-bundled graph visualization is to use colors and opacities to encode information. In [7], edge colors are mapped to the orientations of the original links. The same technique is used in [15] with the difference that an edge direction is encoded by an interpolated color gradient running from a fixed color for the source to a fixed color for the target. In [15], edge opacities are mapped to their length, long curves being more translucent than short ones, preventing short curves to become obscured by long ones. In [7], the opacity of each segment of a polyline representing an edge is mapped to the density of lines overlapping it.

**Perceiving bundles density:** Recent work on edge-bundled graph visualizations addresses the issue of estimating the quantity of edges merged together. In [16], a GPU-based method is used to compute the amount of overdraw for each pixel of the produced graph visualization. That value is then used to map pixels colors with a user defined gradient colorscale after the minimum and maximum value of overdraw have been retrieved. A similar technique is used in [18] where the overdraw densities are mapped to heights and rendered with a bump mapping technique making dense bundles appear higher than sparse ones. That technique allows users to perceive bundles densities while preserving edges colors.

### 3 Routing edges in a 3D space

#### 3.1 Technique overview

Our technique generalizes the idea presented in [18] and therefore uses an edge routing algorithm to bundle edges. Pipeline shown in figure 1 summarizes the different steps of our method. In this example, the original network is embedded in a 2D plane, nevertheless this figure illustrates the main idea of our technique. First of all, we discretize the space into regions according to nodes positions. Boundaries of these regions define a grid that is then used to compute the shortest routes for each edge of the original network. Like highways attract more drivers than little roads, we use frequent routes to bundle edges.

**Grid computation:** The first step of our method consists in building a grid graph used to compute the shortest routes of each original edge (i.e. edge of the original network). This is achieved by discretizing the space into cells or regions using nodes positions. In following, we investigate several approaches to create the grid graph.

Our first attempt was to build a regular 3D grid to discretize the 3D space. However, using such a discretization method forces us to create really large grid graphs to obtain a granularity thin enough to bundle edges even in highly dense regions of the network. To solve that problem, one can build a multi-resolution grid using for instance an octree [17] or 3D Voronoi diagram (for a survey on Voronoi diagrams, the reader can refer to [3]). In an octree, the space is decomposed in height parts until it contains at most one element. Such approach is efficient in term of computation since its time complexity is $O(|V| \cdot \log(|V|))$.

However, using such grid to route edges raises two main issues: the shortest paths computational cost (as the size of the generated grid is large), and the quality of the result (as such grid promotes horizontal and vertical routes).

In [18], Lambert et al. propose to use an hybrid algorithm based on both quad trees and Voronoi diagrams. We follow this principle by using a combination of octree and 3D Voronoi diagram.

**Edge routing:** The second step of the method consists in routing edges of the original graph on the grid graph built in the previous step. One can use a shortest paths algorithm, such as the so called Dijkstra’s algorithm [9], to achieve that operation. However, that method cannot guar-
antee that the edges will follow common routes, and therefore, that the edges will be bundled. To create bundles, we use the metaphor of real life roads. The principle is to make attractive regular roads if highly used (i.e. if many edges are routed along these roads). We reproduce that effect by computing all the shortest paths between linked nodes of the original graph twice. During the first computation, the weight of an edge is set to the euclidean distance between its extremities. Then, according to the number of shortest paths passing through an edge of our grid, we adjust the weight of each edge. Reducing the weight of an edge is equivalent to transform it into a highway since following that edge allow to go faster from one point to another. Recomputing the shortest paths creates bundles as the new matrix distance in our graph promotes the use of highly frequent edges.

3.2 Routing edges on the globe

One of the possible applications of our method is the visualization of international air interconnections in the context of the globe. In that case, we need to adapt our method to route edge around the globe and not across it. We thus have to guarantee that for each edge of the original network, there exists at least one route on the grid graph not crossing the globe. This is achieved by a preprocessing step adding dummy nodes before computing the grid graph (see figure 2). Dummy nodes are first added outside the globe in regular and spherical manner (see figure 2.(b)) to ensure that the 3D Voronoï diagram will contain for each site (node of the original network) a finite cell with boundaries (at least) partially outside the globe. However, adding these dummy nodes is not sufficient to guarantee that no edge of the grid will cross the globe. To overcome that problem we also add dummy nodes inside the globe on sphere having a smaller radius than the globe. By setting the radius of the internal and the external spheres of dummy nodes correctly, we can guarantee that there exists at least one route for each original edge on the grid graph not crossing the globe.

The space discretization step of our algorithm is then applied, creating cells inside but also outside the globe. To speed up the edge routing step and to forbid routes crossing the globe, we remove all nodes (resp. edges) of the generated grid graph inside (resp. crossing) the globe.

3.3 Optimizations

One the main advantages of the edge routing technique to bundle edges is that some optimizations can be done to improve computation time.

As mentioned in section 3, we use the so called Dijkstra’s algorithm [9]. A straightforward optimization consists in not computing shortest paths between all pairs of nodes but only between each edge extremities of the original graph edge. Moreover with a slight modification of the Dijkstra algorithm, we can stop the computation of paths when all candidate nodes (in the Dijkstra’s priority queue) are at a distance greater than all the neighbors of our source node. The second optimization consists in reducing the number of calls to the Dijkstra’s algorithm. More precisely, it consists in minimizing the number of nodes to treat in order to consider each edge of the graph. That problem is also known as the vertex cover problem [14] and had been proved as been NP-complete. However, it is possible to compute a minimum (but not minimal) vertex cover of a graph. Finally, our method run a shortest paths algorithm for each of our vertex cover set and can therefore be parallelized by computing several shortest paths simultaneously. However, there are several critical sections that one needs to address. To remove some critical sections (due to the parallelization) but also generate a set of tasks with more homogeneous sizes, we use a preprocessing step that creates sets of nodes that do not conflict with each other.

These improvements do not change the theoretical complexity but it can significantly reduce execution time.
4 Rendering bundling on the sphere

Visualizing edge-bundled graphs leverage two main issues. First, edges can have a quite high number of bends after the edge routing process of our technique. Consequently, following an edge from its source node to its target node can be quite challenging when rendering edges as polylines. Second, the density of edges that have been merged into a bundle is not easily seen in the drawing. The following sections introduce the rendering techniques we applied to solve these issues.

4.1 Smoothing the edges with curves

Once the bundling process has been performed on the graph, edges become polylines due to the routing phase which adds bends to them. When rendering the edge-bundled graph layout, these bends induce a “zigzag” effect on the edges making them hard to follow. In order to smooth edges, we offer the possibility of rendering them as curves in our visualization system using edge bends as curves control points. Several kinds of parametric curves are proposed including Bézier curves, Catmull-Rom splines and cubic B-splines. Moreover, edges going to the same region of the graph and sharing successive bends remain merged, giving a nicer impression of flows between different areas of the graph. Due to the high computational cost of rendering curves with a large number of control points, especially Bézier curves, we have developed a GPU-based implementation based on dedicated vertex shaders. It allows us to draw a large number of curves defined by an arbitrary number of control points in real time, giving us the ability to smoothly interact with the graph drawing.

4.2 Edge splatting

In order to distinguish dense bundles from sparse ones, we proposed in [18] an edge splatting technique to visually enhance them. Our method is inspired from the GraphSplatting technique introduced by van Liere et al. in [21]. In that work, the authors represent a graph as a 2D continuous scalar field and calculate a splat field. Our edge splatting rendering pipeline is based on a combination of common image processing and computer graphics technique and each stage entirely runs on the GPU. In a similar way than the GraphSplatting technique, the idea is to compute a splat field encoding continuous variations in the density of merged edges. That splat field can then be displayed on screen in a various ways. We chose to render it as a height map for preserving edges colors. A per-pixel shading technique is used mapping splatting values to heights giving the impression than strong bundles appears higher than weak ones. Our original edge splatting technique was restrained to graph embedded in a 2D-plane so we adapted our rendering pipeline in order to handle graph with nodes positioned on a sphere surface. The remaining summarizes the different steps of our edge splatting rendering pipeline.

The first stage of the pipeline is to compute the number of edges crossing each pixel of the drawing. As in [16], that operation can be done by performing an offscreen rendering of the graph edges in an accumulation buffer. Due to the fact that the graph layout is mapped on a sphere, we have to restrain the pixel overdraw computation to edges routed on the visible face of that sphere.

Next stage is the splat field computation. The resulting output of the previous stage is a field of discrete values encoding edges density per pixel. The goal of that stage is to transform it into a continuous scalar field. That process can be performed by convoluting the discrete density values field with a Gaussian kernel defined by a radius \( r \) and a standard deviation \( \sigma \). The larger the kernel radius and standard deviation, the more the splat field is smoothed.

The final stage performs the splat field rendering using a classical shading technique called bump mapping. Bump mapping is a computer graphics technique introduced by Blinn [6] allowing a rendered surface to appear more realistic without modifying geometry. It adds a per-pixel shading that makes the surface appears bumpy, by changing the surface normals. These modified normals are computed from a heightmap generated by mapping the splatting values to a black to white color scale. A dedicated fragment shader compute for each pixel the heightmap derivatives in horizontal and vertical directions using a gradient operator, like the Sobel or Prewitt filter, and construct the associated normals from these. Once the normal map associated with the splat field has been generated, bump mapped rendering can be performed. Because we want to perform bump mapping on a sphere surface and not on a flat one, we add an extra process to our original pipeline. Its goal is to compute for each pixel of the sphere’s visible face the transformation of the light vector and the eye vectors into tangent space. That space is locally tangent to the surface and is used to compute the final colors of the pixels in a bump mapping context. That process is performed by rendering a sphere in an offscreen buffer, whose center and radius are the same as the graph layout, with tangent space informations attached to each vertex of the mesh. A dedicated shader program then transforms the light and eye vectors provided as parameters into tangent space and stores the results in two floating point textures. The final bump mapped drawing is then generated by another shader program reading the modified normals from the normal map texture, the transformed light and eye vectors from the two previous generated textures, and performing a per-pixel illumination using Blinn-Phong [5]. The final colors of the pixels are computed from the lighting properties and another texture called the diffuse map. In our case, the diffuse map corresponds to the original edge colors. To perform a global il-
Figure 3: (a) 2000 international air interconnections network, containing 1524 airports and 16397 flights, embedded on the globe; (b) Result when applying the 3D edge routing method and using spline curves; (c) Result when routing edge around the globe and using cubic b-spline curves and bump mapping; (d) 2004 international air interconnections network, containing 1501 airports and 12360 flights, embedded on the globe; (e) Result when applying the 3D edge routing method and using cubic b-spline curves and bump mapping; (f) Zoomed view.

We experimented our algorithm on the international air interconnection networks of year 2000 and year 2004 (see figure 3). Figures 3.(a) and (d) show the original layout of both air traffic networks when nodes are laid out according to their latitudes and longitudes. An edge color is computed according to the geographical regions its extremities belong to (for instance, european flight are represented by red edges while north american ones are in dark green). These representations are difficult to understand due to the visual complexity of such networks and to occlusion problems raised by 3D visualization. Using our 3D edge bundling technique (see figure 3.(b)) reduces the clutter of the representation. One can already see some of the major trends, such as really dense intra european and north american networks. However as the number of possible routes for each original edge is large, edges are not bundled enough and the representation still suffers from occlusion problems.

Figures 3.(c) and .(e) show the result we obtained when routing the edges around the globe and not across it. To increase the readability of that drawing, we added a texture to render the continents and seas. These drawings had been computed in 90 seconds for the 2000 air traffic network and 84 seconds for the 2004 air traffic network 1. When looking closer to the results one can notice that edges colors in each bundle are more or less uniform, meaning that

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1Computation time obtained with an Intel Core Duo 2.4 GHz processor with 4GB RAM.
edges bundled together are linking the same geographical regions. For instance, figure 3.(f) is a zoomed view on the 2004 air traffic network, one can see that all edges between Europe and North America were bundled together in the light brown bundles. In these figures, one can see major trends, such as the central positioning of Europe within both networks or that Africa is mainly related to European and middle east countries. Our technique clearly improves the readability of these representations and help to reveal high-level edge patterns.

Conclusions

In this paper, we have presented a 3D edge bundling technique based on edge routing. This technique allows to reduce clutter of a 3D representation but also reveals high-level edge patterns. We have also introduced the needed modifications to bundle the edges on the sphere in order support visualization geographical networks, such as the international air traffic networks, in the context of the globe.

To facilitate edge bundle density perception, we presented a GPU-based rendering method that allows a fast enough rendering to support smooth exploration. That method is an extension of the bump-mapping technique of [18] which allows to preserve edge colors in order to encode another information.

An interesting direction for future work is to explore different methods to build the grid graph such as a grid supporting non-uniform nodes sizes or avoiding regions of the representation. Another direction is to adapt our method to surfaces having other topologies. Finally we plan to speed up the rendering by minimizing the number of bends. This bends simplification should also guarantee that no node-edge overlap is created.

References


