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Adaptable Mobile Transactions and Environment Awareness

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ABSTRACT. Mobile environments are characterized by high variability (e.g. variable bandwidth, disconnections, different communication prices) as well as by limited mobile host resources. Such characteristics lead to high rates of transaction failures and unpredictable execution costs. This paper introduces an Adaptable Mobile Transaction model (AMT) that allows defining transactions with several execution alternatives associated to a particular context. The principal goal is to adapt transaction execution to context variations. An analytical study shows that using AMTs increases commit probabilities and that it is possible to choose the way transactions will be executed according to their costs. In addition, the middleware TransMobi is proposed. It manages environment awareness and implements the AMT model with suitable protocols.

RÉSUMÉ. Les environnements mobiles sont caractérisés par une grande variabilité (bande passante variable, déconnexions, prix de communication différents, etc.) ainsi que par des unités mobiles à ressources limitées. Ces caractéristiques entraînent un nombre important de défaillances transactionnels et des coûts d’exécution imprévus. Cet article introduit un modèle de transactions mobiles adaptables (AMT) permettant de définir des transactions avec plusieurs alternatives d’exécution. Le principal objectif est d’adapter l’exécution des transactions aux variations du contexte. Une étude analytique montre que les AMT augmentent la probabilité de validation et qu’il est possible de choisir le type d’exécution en fonction de son coût. Nous proposons également l’intergiciel TransMobi gérant la perception de l’environnement et implantant le modèle AMT à l’aide de protocoles appropriés.

KEYWORDS: Mobile transactions, ACID properties, environment awareness.

MOTS-CLÉS : Transactions mobiles, propriétés ACID, perception de l’environnement.

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1. Introduction

The omnipresence of mobile devices such as cell phones, PDAs, smartcards, sensors and laptops, together with the development of different kinds of networks (local, wireless, ad-hoc, etc.) lead to a true mutation in the use, design and development of future information systems. Our work is related to the topics of ubiquitous and pervasive computing where technological improvements allow users to access data and perform transactions from any type of terminal and from anywhere using a wired or a wireless network. Applications that we have in mind cover a wide area. They might be personal ones, where clients want to access public data (e.g. weather forecast, stock exchange, road traffic) or professional ones, where mobility is inherent (e.g. mobile vendors/clients, health services, mobile offices, transport). We consider that mobile and fixed hosts can be clients or servers.

We consider a mobile computing environment with a network consisting of fixed and mobile hosts (FH, MH), see Figure 1. MHs could be of different nature ranging from PDAs to personal computers. Shared data are distributed over several database servers running, generally, on FHs. MH may run database management system (DBMS) modules and may provide some services to other hosts. While in motion, an MH may retain its network connection through a wireless interface supported by some FHs which act as Base Stations (BS). The geographical area covered by a BS is a cell. Each MH communicates with the BS covering its current cell. The process during which an MH enters into a new cell is called hand-off.

We make no specific assumptions about the database model (relational, object) but we place ourselves in a multidatabase environment assuming that data are managed by autonomous and possible heterogeneous DBMSs.

Applications in mobile environments are confronted to particular characteristics and limitations imposed by hardware such as: low and variable bandwidth, frequent disconnections, high communication prices, variable hardware configuration (due to plug-in components), limited display, battery autonomy, processing power and data
storage. These limitations/variations lead to a lot of potential failure modes that affect data management process (e.g. queries, replication, caching, transactions, etc.).

In this paper, we are particularly interested on mobile transaction management. Focusing on this notion, we adopt a quite general definition: a mobile transaction is a transaction where at least one mobile host takes part in its execution. Mobile transactions are considered as long lived ones because of the probability of disconnections.

As an example, let us introduce an e-shopping application that allows people to browse products in an e-mall, to select, to book and to buy items. We assume also that secured e-payment is available based on credit cards or e-money. Application execution – as a set of transactions – will not be the same if they are launched from a (fixed) terminal office, from a PDA while traveling in a train or from home using a laptop. Thus, under this context:

– transactions may succeed but with different execution times (bandwidth capacity is highly variable) and communication prices (prices vary among wireless network providers/technologies/time-access);
– energy consumption is affected by low bandwidth (more battery is consumed);
– failures may occur due to unexpected disconnections or battery breakdown.

In traditional environments, application designers do not care about host and network characteristics. Nevertheless, in mobile applications we claim the necessity of being environment aware to overcome the infrastructure variability and to react to variations satisfying application and user requirements.

Several works concerning mobile transactions have been introduced (e.g. [DUN 97, YEO 94, DIR 00]). In the analysis made in [SER 03b], we found out that the majority of these proposals are particular solutions oriented to specific application context. Moreover, most of these works do not take into account the importance of mobile environment variability and therefore environment awareness.

The contribution of this paper is twofold, we propose an Adaptable Mobile Transaction (AMT) model and the middleware TransMobi to support it. The general idea of the AMT model is to define mobile transactions (\( T_{AMT} \)) with several execution alternatives associated to a particular mobile environment state. When a \( T_{AMT} \) transaction is launched, the appropriate execution alternative is initiated depending on the current mobile environment. We argue that adapting transaction executions improves commit rate, execution costs, response times and application availability, in short, the application’s quality of service. We made an analytical study that shows how the AMT model increases transaction commit probability according to expected costs. The middleware TransMobi coordinates the execution of \( T_{AMTS} \) and manages the variations of the mobile environment state (e.g. bandwidth rate, communication price, MH disconnections, MH available energy, etc.). It uses suitable protocols to guarantee AMT properties. Among these protocols we propose (CO2PC) a Combination of an Optimistic approach and 2PC [GRA 78] to ensure semantic atomicity.

This paper is organized as follows: Section 2 presents the adaptable mobile transaction model and Section 3 gives an analytical study of its performances. Section 4...
introduces the TransMobi middleware. Section 5 discusses related work and Section 6 concludes this article.

2. Adaptability for Mobile Transactions

2.1. Overview

Traditionally, transactions are defined independently of execution infrastructure. This approach is well suited for centralized and distributed systems where the execution characteristics have acceptable, predictable and controlled state variations. As the mobile environment is highly variable, transaction execution can be unpredictable.

We consider that in order to optimize resources, both transaction design and management should be made taking into account environment awareness. Our proposal is done along these lines. For each mobile transaction, application programmers give execution alternatives suitable to a particular environment context. For instance, a transaction distributed over a fixed and a mobile host will be launched if a good connection is available, whereas, a local execution will be preferable if there is no connection or if only a very low bandwidth is available.

To allow context aware transaction executions we propose an Adaptable Mobile Transaction (AMT) model. This model offers concepts to design mobile transactions \( T_{AMT} \). Generally speaking, a \( T_{AMT} \) is composed of at least one execution alternative involving one or several mobile or fixed hosts. Execution alternatives may be semantically equivalent. The successful execution of one of them, represents a correct execution of the \( T_{AMT} \). A \( T_{AMT} \) also contains environment descriptors which express the state of the mobile environment required to execute each alternative. When a \( T_{AMT} \) is launched, the mobile environment state is checked and the appropriate execution alternative is chosen – only one alternative must be active by \( T_{AMT} \). If the environment state does not allow the execution of any alternative, the execution of the \( T_{AMT} \) may be deferred. As soon as an acceptable environment state will be detected, an execution alternative will be triggered.

2.2. Mobile Environment Awareness

Mobile environments include the wireless network (WN), MHs involved in mobile transactions and MH locations. Several dimensions – connection state, bandwidth-rate or communication price – characterize the state of a mobile environment. As said before, the variability of such environment may affect transaction execution and impact resources consumption. Environment descriptors introduced here reflect the execution context and its potential state variations. Thus, transaction designers who know the application characteristics and requirements for quality of service, specify different execution alternatives and the required execution context for each of them.\footnote{This might put the burden on the application designer. Future work should be oriented to develop computer aided environments for application developers.}

The set of relevant dimensions is specific to the application environment. It depends on the available mobile network, used MHs or user habits. For instance,
Table 1. Mobile environment characteristics.

<table>
<thead>
<tr>
<th>Dimension</th>
<th>States</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>WN</td>
<td>connection-state = connected, disconnected</td>
<td></td>
</tr>
<tr>
<td></td>
<td>bandwidth-rate = high, medium, low</td>
<td>kbytes/s</td>
</tr>
<tr>
<td></td>
<td>communication-price = free, cheap, expensive</td>
<td>Euros/time</td>
</tr>
<tr>
<td>MH</td>
<td>available-battery = full, half, low</td>
<td>hh:mm:ss</td>
</tr>
<tr>
<td></td>
<td>available-cache = full, half, low</td>
<td>kbytes</td>
</tr>
<tr>
<td></td>
<td>available-persistent-memory = full, half, low</td>
<td>kbytes</td>
</tr>
<tr>
<td></td>
<td>processing-capacity = high, medium, low</td>
<td>mhz/s</td>
</tr>
<tr>
<td></td>
<td>estimated-connection-time = t</td>
<td>hh:mm:ss</td>
</tr>
</tbody>
</table>

network bandwidth is important under packet-switched networks (e.g. UMTS) and not under circuit-switched ones (e.g. GSM) where bandwidth is guaranteed if the connection is available. Also, communication price is not relevant under WLAN networks but may be crucial in other environments. In addition, user-defined dimensions can be introduced, for instance, specific “quality” of data.

The basic set of dimensions we consider is introduced in Table 1. To simplify, States are divided in levels of quality – high, medium, low – nevertheless, they can be defined according to each specific dimension.

Environment descriptors (ED) indicate dimensions and states as follows.

**Definition 1** An Environment Descriptor \( ED = \{ \text{dimension}=\text{state(s)} \} \) contains a set of dimensions with their respective states at a given instant.

For instance, to execute an alternative involving large data transfer, the required environment state may be:

**Example 1** \( ED = \{ \text{connection-state} = \text{connected}, \text{bandwidth-rate} = \text{high}, \text{communication-price} = \text{free, cheap} \} \).

Notice that several hosts may be involved in a transaction. In that case, \( ED \) may or may not specify the required state for each involved host.

2.3. The AMT Model

This model allows to describe mobile transactions having one or more execution alternatives \( E_{A_{k}} \), each of them is associated to an \( ED_{k} \). \( E_{A_{k}} \)s may take the form of any of the following execution types: the mobile transaction (1) is initiated by an MH and entirely executed on FHs, (2) is initiated by an MH/FH and entirely executed on an MH, (3) execution is distributed among MHs and FHs, and (4) execution is distributed among several MHs. So, a wide variety of mobile transactions is addressed.

An \( E_{A_{k}} \) contains a set of component transactions \( (t_{ki}) \) which must respect ACID properties. They can be traditional flat, distributed or close nested transactions. Compensating transactions may be associated to component transactions. They will be executed in case of failures. An \( E_{A_{k}} \) may be aborted if a component transaction
aborts or if the mobile environment changes and the new state does not satisfy its
environment descriptor. The EAs and the T_{AMT} are coordination units, data access
is made only by component transactions. Making the analogy with multidatabases,
component transactions are local transactions participating into global transactions.

Next, we present a semi-formal definition of the AMT model. A formal specification
in ACTA [CHR 90] is presented in [SER 03a].

**Definition 2** An adaptable mobile transaction is a \( T_{AMT} = (E_A) \) where:
- \( (E_A) \), \( k > 0 \), is a list of execution alternatives for \( T_{AMT} \) where \( E_A \) has
  higher priority than \( E_A_{k+1} \).
- \( E_A \) = \( (E_D, E_P) \), an execution alternative has an execution plan \( E_P \) to be
  executed if the actual mobile environment satisfies the environment descriptor \( E_D \).
- \( E_D \) describes the environment state for the suitable execution of \( E_P \).
- \( E_P \) = \{ \( (t_{ki}, ct_{kt}, HostId) \) \}, is a set of triplets introducing a component trans-
  action, its compensating one and the host where they have to be executed.

Let \( RD \) be a relationship dependence over \( E_P \), such that:
\[ \forall (t_{ki}, ct_{kt}, HostId_x) \in E_P; (t_{kl}, ct_{kt}, HostId_y) \in E_P; \]
\[ (t_{ki}, ct_{kt}, HostId_x) RD (t_{kl}, ct_{kt}, HostId_y); \]

HostId indicates a database and the MH/FH responsible for the execution. Such
host must execute only one component transaction per execution alternative. In \( RD \),
we consider parallel or sequential execution dependencies.

Compensating transactions \( (ct_{kt}) \) are semantically equivalent to physical rollbacks
and are defined to undo already committed component transactions. They recover
semantically the database and avoid cascading aborts. Defining a \( ct_{kt} \) to compensate
a \( t_{ki} \) is not always possible, thus, \( ct_{kt} \) will not always appear in \( E_P \).

**AMT example**

To continue with the example introduced in Section 1, consider an MH client with
storage capacity, and an e-mail with two servers on the wired network: CatalogS and
PurchaseS. The first site allows to query the store catalog whereas the second one
takes purchase orders and payments.

We define the \( T_{AMT, shopping} \) with the following component transactions:
- GetCatalog allows clients to get a catalog;
- SelectItems allows clients to select items from a local copy of the catalog;
- Order-Pay allows clients to send the purchase order and payment to the store;
- AutoPay allows clients to pay on the MH (with e-money) without contacting
  other host;
- Order allows clients to send a purchase order (no payment included);
- Select-AutoPay = SelectItems + AutoPay
Table 2. **TAMTshopping example.**

<table>
<thead>
<tr>
<th>$E_{A_k}$</th>
<th>$E_{D_k}$</th>
<th>$F_{IA}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k=1$</td>
<td>catalog-state=upToDate</td>
<td>(SelectItems, MH), (Order-Pay, PurchaseS)</td>
</tr>
<tr>
<td>$k=2$</td>
<td>(connection-state=connected, bandwidth-rate=high, medium, communication-price=cheap), (SelectItems, MH), (Order-Pay, PurchaseS)</td>
<td></td>
</tr>
<tr>
<td>$k=3$</td>
<td>(connection-state=connected, bandwidth-rate=low, catalog-state=missing)</td>
<td>(GetCatalog, CatalogS), (Select-AutoPay, MH), (Order, PurchaseS)</td>
</tr>
</tbody>
</table>

In Table 2, **TAMTshopping** proposes three execution alternatives to be triggered according to the environment state. In this example, wireless network dimensions that determine the choice of an alternative are: connection availability, bandwidth and communication price. The presence of the catalog on the MH is an application defined dimension. It takes the states missing (the catalog is not available on the MH) present (a version, probably out of date or incomplete, is on the MH) or upToDate (an up to date version is on the MH). Dimensions not appearing in environment descriptors are not considered as relevant for the context application.

In this example, the priorities between $E_{A_k}$s are determined by the communication cost. Executing $E_{A_1}$ is cheaper than executing $E_{A_2}$. In $E_{A_1}$ the MH has an up to date catalog, this allows saving communication messages. $E_{A_1}$ may be launched even in disconnected mode and Order-Pay can be deferred until reconnection. $E_{A_2}$ will be launched provided that the communication quality is acceptable. $E_{A_3}$ is executed even under bad communication rates. The advantage of this alternative is that Select-AutoPay can be made in disconnected mode because the payment is in the MH. Order will be launched at reconnection.

Defining compensating transactions for this example is easy. They would mainly include operations to cancel orders and refundings.

### 2.4. **AMT Properties**

A $T_{AMT}$ can be considered at three different levels: the $T_{AMT}$ itself, the execution alternatives and the component transactions. For the last ones we assume that ACID properties are guaranteed, nevertheless, as we will see latter, durability is conditioned by the success of the corresponding execution alternative.

An execution alternative (actually the associated $E_{P_k}$) is a kind of sagas [GAR 87] containing a set of transactions which execution may be distributed among mobile and fixed hosts. The $RD$ defined inside the alternative describes the possibility of a parallel or sequential execution of component transactions. Integrity constraints can be defined and verified at $t_{k_i}$ level, under the responsibility of the underlying DBMS. Global data integrity constraints are not considered but value dependencies between $t_{k_i}$s (of the same $E_{A_k}$) are allowed.
 Atomicity and isolation for $E A_k$

Considering the restrictions of mobile environments, the AMT model relaxes atomicity by adopting semantic atomicity [GAR 83] (as in sagas).

Definition 3 $E A_k$ preserves semantic atomicity if either:

- All $t_{ki}$s defined in $E A_k$ commit.
- All $t_{ki}$s defined in $E A_k$ are compensated or rolled back.

The goal is to avoid blocking participant hosts and to allow MH disconnections. This is obtained with local commits where partial results are shared before the $E A_k$ commits. The durability of locally committed transactions is conditioned to the commit of the $E A_k$. In case of abortion, compensating transactions are used.

To address critical applications with non-compensatable transactions, resources are blocked. Thus, when transactions terminate, resources are retained until a global decision ($E A_k$ commits/aborts) is made. Hence, compensating transactions are not needed. If no participant commit locally, compensating transactions will be unnecessary and traditional atomicity is obtained.

Since dependency values between $t_{ki}$s of the same $E A_k$ are allowed, a correct global ordering must be ensured. That is because concurrent execution of several alternatives might introduce indirect interference between value dependent transactions. The criterion used to control the correctness of concurrent execution alternatives is global serializability. Global serializability states that transactions of each $E A_k$ must have the same relative serialization order in their corresponding underlying DBMS.

Even though a global serializable order is preserved, semantic consistency [GAR 83] is provided – due to semantic atomicity.

 Atomicity and Isolation for $T_{AMT}$

We mentioned in Section 2.3 that $E A_k$s defined in a $T_{AMT}$ may be semantically equivalent. A $T_{AMT}$ is correctly executed if one of its $E A_k$s is successfully executed. This results in Semi-atomicity [ZHA 94] which is guaranteed for $T_{AMT}$s as follows.

Definition 4 AMT preserves semi-atomicity if either:

Table 3. Summary of AMT properties.
– All \(t_{ki}\) defined in \(EA_k\) commit and all attempted \(t_{ki}\)s, of another alternative \(EA_i\) in the same \(T_{AMT}\), are aborted or have their effects compensated.
– No partial effects of component transactions of the \(T_{AMT}\) remain permanent in the underlying DBMSs.

Serializability of \(T_{AMT}\)s is offered through the serializability of execution alternatives. Regarding the durability property, once the corresponding \(EA_k\) commits (and consequently the \(T_{AMT}\)), durability of component transactions is provided by the underlying DBMS. Table 3 summarizes properties at all levels (\(t_{ki}, EA_k, T_{AMT}\)). Section 4 introduces appropriate protocols to ensure these properties.

### 3. Impact of Environment Awareness: Analytical Study

This section provides an analytical study of the capabilities allowed by the AMT model. In Section 3.1, we use a probabilistic model to analyze several execution alternatives one by one — separated of the AMT model. For each of them, we evaluate its initiation probability and its execution cost. Section 3.2 highlights the benefits expected from environment awareness and AMT adaptable facilities. It is shown that the \(T_{AMT}\) initiation probability is always greater than the initiation probability of one alternative. In addition, it is shown how the AMT model allows the designer to define the best \(T_{AMT}\) according to the required quality of service: low cost without complete guarantee of success or at the opposite success any time at any cost. The \(T_{AMT}\) shopping example (introduced in Section 2.3) is used all along this section to illustrate the analytical study. A short concluding discussion is proposed in Section 3.3.

#### 3.1. Analytical Study of an Execution Alternative

**Mobile Environment Model**

As mentioned in previous sections, a mobile environment state can be seen as a set of dimensions. An \(EA_k\) is initiated only if the environment state satisfies the acceptable states for each dimension.

**Example 2** The environment descriptors used by \(T_{AMT}\) shopping include the following dimensions and states:

<table>
<thead>
<tr>
<th>Dimension</th>
<th>States</th>
</tr>
</thead>
<tbody>
<tr>
<td>Connection State</td>
<td>Connected, Unlinked</td>
</tr>
<tr>
<td>Bandwidth Rate</td>
<td>High, Medium, Low</td>
</tr>
<tr>
<td>Communication Price</td>
<td>Cheap, Expensive</td>
</tr>
<tr>
<td>Catalog State</td>
<td>Up-to-date, Present, Missing</td>
</tr>
</tbody>
</table>

**Definition 5** Let \(p_{ij}\) be the probability of dimension \(i\) to be in state \(j\).

In the resulting matrix \(P = (p_{ij})\), \(\forall i, \sum_j p_{ij} = 1\). Next example shows that this matrix depends on the considered mobile environment.
Example 3 An example of the matrix probability of an environment like the one introduced in the example 2 could be:

\[ P = (p_{ij}) = \begin{bmatrix}
0.8 & 0 & 0.2 \\
0.7 & 0.2 & 0.1 \\
0 & 0.4 & 0.6 \\
0.2 & 0.3 & 0.5
\end{bmatrix} \]

Here, the probability of being connected is given by \( p_{11} \), the probability of having an up-to-date catalog is given by \( p_{41} \) and so on. \( p_{31} \) has 0 probability because in the considered environment, communication is never free.

Environment Description Matrix

Definition 6 For each \( EA_k = (ED_k, EP_k) \) we denote by \( \Delta^k \) the boolean matrix where:

\[
\delta^k_{ij} = \begin{cases} 
1 & \text{if the state } j \text{ of dimension } i \text{ is acceptable for } EA_k \\
0 & \text{otherwise}
\end{cases}
\]

Example 4 The \( \Delta^k \) matrix for the three proposed alternatives of \( T_{AMT\text{shopping}} \) (see Table 2) are:

\[
\Delta^1 = \begin{bmatrix}
1 & 0 & 1 \\
1 & 0 & 1 \\
0 & 1 & 0 \\
1 & 0 & 1
\end{bmatrix} \quad \Delta^2 = \begin{bmatrix}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{bmatrix} \quad \Delta^3 = \begin{bmatrix}
1 & 0 & 0 \\
0 & 1 & 1 \\
0 & 0 & 1
\end{bmatrix}
\]

If a dimension \( i \) does not appear in \( ED_k \), any state is suitable: if \( i \notin ED_k \) then \( \forall j, \delta^k_{ij} = 1 \). \( \Delta^3 \) and \( \Delta^2 \) illustrate this case.

Cost Matrix

Definition 7 Let \( C^k \) be the matrix where \( c^k_{ij} \) is the cost of the \( EP_k \) execution in state \( j \) of dimension \( i \).

\( c^k_{ij} \) must be defined by the designer according to application needs in cost improvement. Example 5 shows some particular definitions of cost.

Example 5 For the \( T_{AMT\text{shopping}} \) one could identify the memory utilization as a cost associated to the dimension catalog-state or the CPU consumption as a cost associated to the dimension connection-state (since in disconnected mode more operations are done on the MH). Let us focus on communication price and battery utilization respectively associated to dimension communication-price and bandwidth-rate (bandwidth limitations increase battery consumption). The considered wireless network is UMTS which uses a packet-switched communication where bandwidth rate goes from 144 kbps (vehicular mobility), 384 kbps (pedestrian mobility) to 2 mbps for indoor traffic. These bandwidth rates correspond to high, medium and low states. Communication price depends on the size of transmitted data (packets). For instance, the execution of \( EP_1 \) requires three wireless logical messages. First, a transaction request (kind of login), then the purchase order (component transaction Order-Pay) and finally, a message is received by the MH to confirm the order (acknowledgment). The execution of \( EP_2 \) and \( EP_3 \) requires an extra message to ask for the catalog which is received through another message (GetCatalog).
Three different sizes of messages may be identified: small messages (login, ack and ask for catalogue), medium ones (for Order-Pay and Order) and large ones (for GetCatalog). Let us assume that small, medium and large messages are composed respectively of 1, 10 and 20 packets. So, if the execution plan of $EA_k$ sends $n_s$ small, $n_m$ medium and $n_l$ large messages then $n_p$ is the number of packets sent or received by the MH during the $EP_k$ execution, $n_p = n_s + 10n_m + 20n_l$.

To evaluate communication cost (communication price and battery consumption), we assume that:

- Sending a single packet in the state cheap (resp. expensive) costs 1 unit of price (resp. 2 units).
- If bandwidth is high (resp. medium, low) sending/receiving a single packet uses 0.1% (resp. 0.2%, 0.4%) of the battery capacity. In this case, the cost associated to the dimension bandwidth-rate is the battery consumption.

Under these assumptions we have:

$$C_k = \begin{bmatrix} 0 & 0.1n_p & 0 \\ 0 & 0.2n_p & 0 \\ 0 & 0.4n_p & 0 \\ 0 & 2n_p & 0 \end{bmatrix}$$

where $c_{kj}^k$ is the battery consumption of the $EP_k$ execution when the bandwidth-rate is in state $j$. $c_{kj}^k$ is the price of the $EP_k$ execution when the communication-cost is in state $j$. In $TA_MT$ shopping, $n_p = 12$ for $EP_1$ and $n_p = 33$ for $EP_2$ and $EP_3$, so:

$$c^1 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1.2 & 2.4 & 4.8 \end{bmatrix}$$

$$c^2 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 3.3 & 6.6 & 13.2 \end{bmatrix}$$

Mean Cost of an $EA_k$

The execution plan of $EA_k$ is launched by the system when the mobile environment is in the state $j$ of the dimension $i$ with the probability:

$$\frac{\delta^k_{ij}p_{ij}}{\sum_j \delta^k_{ij}p_{ij}}$$

So, the mean cost due to dimension $i$ of the $EP_k$ execution is given by:

$$c^k_i = \frac{\sum_j \delta^k_{ij}c_{ij}^k p_{ij}}{\sum_j \delta^k_{ij} p_{ij}}$$

Example 6 With previous $P$, $\Delta^k$ and $C^k$ we can compute:

$$c_3^3 = \frac{13.2 \times 0.1}{0.1} = 13.2%$$

$$c_3^3 = \frac{33 \times 0.4 + 66 \times 0.6}{0.4 + 0.6} = 52.8$$

This means that the average of battery consumption of $EA_3$ is 13.2% with an average price of $c_3^3 = 52.8$ units, whereas $c_2^3 = 1.8\%$, $c_3^3 = 19.2$ units and $c_2^3 = 4.03\%$, $c_3^3 = 33$ units.

3. Eventually, it could be interesting to distinguish between sending or receiving messages.
Definition 8 Let $q^k$ be the probability for $EA_k$ of being selected for execution. $q^k$ will be called the $EA_k$ initiation probability. Since the probability that dimension $i$ has an acceptable state for $EA_k$ is given by $\sum_j \delta_{ij}^k p_{ij}$, we have:

$$q^k = \prod_i \left( \sum_j \delta_{ij}^k p_{ij} \right)$$

So the execution plan of an $EA_k$ has a chance to be initiated ($q^k > 0$) iff $\forall i, \exists j$ such that $\delta_{ij}^k = 1$.

Comparing EAs

Example 7 In order to study EAs in different types of environment, performances indices are studied in regard to the probability of the bandwidth to be low ($p_{23}$):

$$P = \begin{bmatrix} 0.8 & 0.2 \\ (1 - p_{23})/2 & (1 - p_{23})/2 \\ 0.2 & 0.6 \\ 0.4 & 0.5 \end{bmatrix}$$

Fig. 2 shows the $EA_k$ initiation probability and Fig. 3 the battery consumption associated to each $EA_k$ in $T_{AMT}$. It can be seen that if the bandwidth is often low (e.g. $p_{23} = 0.8$) then $EA_3$ is the alternative with the highest battery consumption whereas it has the best initiation probability. $q^1$ is constant because it does not depend on the bandwidth but only on the probability for the catalog to be uptodate.

3.2. Analytical Study of a $T_{AMT}$

As mentioned in Section 2, mobile environment awareness allows the system to choose an $EA_k$ if the environment state corresponds to the associated $ED_k$. $EA_k$ has higher priority than $EA_{k+1}$; this allows us to assume without lost of generality that:

Property 1 If a state of the environment is suitable for an $EA_k$ it should not be suitable for an $EA_{k'}$ of the same $T_{AMT}$. That is: $\forall (k, k'), k \neq k', \exists i$ such that $\forall j, \delta_{ij}^k \neq \delta_{ij}^{k'}$.
Adaptable Mobile Transactions

**$T_{\text{AMT}}$ Initiation Probability**

**Definition 9** Let $q_{\text{AMT}}$ be the $T_{\text{AMT}}$ initiation probability. Thanks to property 1, we have: $q_{\text{AMT}} = \sum_k q^k$.

**Mean Cost of a $T_{\text{AMT}}$**

**Definition 10** Let $c_i$ be the mean cost (associated to dimension i) of the execution of $T_{\text{AMT}}$. Under the assumption that the environment is stable during the execution, $EA_k$ is initiated with the probability $q^k$ so the cost of the whole $T_{\text{AMT}}$ is $c_i^k$ with the probability $q^k$, hence:

$$c_i = \frac{\sum_k c_i^k q^k}{\sum_k q^k}$$

As an example, we study the mean battery consumption and the initiation probability of $T_{\text{AMT} \text{shopping}}$ in regards to the probability of the bandwidth to be low ($p_{23}$).

Fig. 2 shows that the $T_{\text{AMT} \text{shopping}}$ initiation probability never reaches 1. This is due to the fact that for certain states no alternative is defined. For instance, if the MH is disconnected with a missing catalog $T_{\text{AMT} \text{shopping}}$ cannot be initiated. This figure also shows that the initiation probability of a single $EA_k$ is smaller than the initiation probability of the whole $T_{\text{AMT} \text{shopping}}$.

Fig. 3 shows that the mean battery consumption of the $T_{\text{AMT} \text{shopping}}$ increases with the probability of the bandwidth to be low is going up. This is due to the fact that $EA_3$ initiation probability is bigger than the one of $EA_2$ (see Fig. 2).

Fig. 4 shows performance parameters for $T_{\text{AMT} \text{shopping}}$ and a variant without $EA_3$. This new transaction is called $T_{\text{AMT} \text{12}}$. It can be seen that $T_{\text{AMT} \text{shopping}}$ has a better initiation probability whereas $T_{\text{AMT} \text{12}}$ has a better mean battery consumption.

**3.3. Discussion**

This section showed that compared to non-adaptable approaches, adaptability in transaction execution improves performances and allows choosing the way the transaction will be executed according to execution costs. Without environment awareness, a transaction is defined in a standard way (the execution plan is fixed). The system will try to execute this transaction whatever the state of the environment is. If the current state does not allow the execution, the transaction will fail even if another execution alternative could have been successful. In the same way, the environment state may lead to a costly execution without considering cheaper alternatives. Allowing the system to choose the execution plan in regards to the current environment state is a way to ensure better performances.

With $n$ different execution plans, environment awareness and AMT facilities allow to choose among $n!$ different $T_{\text{AMT}}$ (each one including $n$ alternatives) depending upon the user optimization criteria, e.g. minimal costs or execution time. The definition of the $T_{\text{AMT}}$ that provides best initiation probability does not depends on the number of defined $EA_k$s but on the capacity to overcome environment variations.
To ensure a better quality of service with $T_{AMT}$ execution, specific tools based on this analytical model could be used to define optimized $T_{AMTS}$.

Environment awareness allows to define the $T_{AMT}$ that fits the best to the quality of service required by the application, for instance, a trade-off between reducing costs and relaxing quality of service can be done.

4. TransMobi Middleware

We designed the TransMobi middleware which supports adaptable mobile transactions ($T_{AMT}$). This section presents the architecture of TransMobi, its functionalities, the environment awareness and the protocols to ensure the AMT properties.

4.1. Overview and Architecture

As a middleware between application code and existing DBMSs, TransMobi coordinates the execution of $T_{AMTS}$, see Fig. 5a. We assume the existence of DBMS functionalities on fixed and mobile hosts. TransMobi relies on them for the execution – ensuring ACID properties – of component and compensating transactions. To preserve DBMS autonomy, TransMobi uses standard interfaces.

TransMobi has the client/agent/server architecture showed in Fig 5b. A TMClient acts as an intermediate between the mobile application and underlying DBMS. It may run on FHs, called fixed TMClients or on mobile hosts, called mobile TMClients. Among others a TMClient manages MH awareness.

Figure 5. TransMobi global architecture.

4. Preliminary ideas on a Mobile Transaction Service (MTS) were introduced in [SER 02].

5. Products like FastObjects j2 [Fas ] or Oracle9i Lite [Ora ] provide ACID properties.
Table 4. Event types for environment awareness.

TransMobi Agents (TMAgent) are on BSs\(^6\) or on some FHs able to communicate with MHs. TMAgents play a particularly important role, they (1) facilitate the interaction between mobile and fixed hosts acting as a representative (e.g. storing communication messages addressed to disconnected MHs, keeping track of particular MH information), (2) store transactional coordination information (e.g. transaction state, commit process), (3) follow MH moves (in case of hand-off, the old TMAgent sends the related MH information to the new TMAgent), and in particular, (4) manage network awareness.

A TMServer does some kind of global control, for instance, it maintains a global serializability graph. Furthermore, it interacts with database servers requesting for transaction execution on behalf of mobile applications. Besides transaction execution, servers may provide replication and reconciliation features, but it is not our objective to address these issues here.

Generally speaking, \(T_{AMT}\) application requests are intercepted by a TMClient. It chooses the best \(EA_k\) to be initialized according to the mobile environment state and distributes the \(t_{k,s}\) to the appropriate hosts. Distribution is made according to relationship dependences over \(EP_k\) (see Section 2.3). Mobile TMClients send the \(EA_k\) to their TMAgent which takes in charge the distribution. Value dependent component transactions are executed sequentially, independent ones can be executed concurrently.

4.2. Adaptability and Environment Awareness

TransMobi takes advantage of the adaptability potential of the AMT model. TMClients take in charge the comparison of the actual mobile environment state with environment descriptors. Comparison is made in the order defined by the \(EA_k\) list.

The environment state concerns the wireless network, MHs and location. A mobile TMClient knows its state (see Table 1) and perceives the WN one. For fixed TM Clients the state of the mobile environment is provided by TMAgents which perceive the WN

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6. Wireless network providers, generally, do not allow to install software on BSs, we believe that this will change in the future.
state. An MH may publish its state completely or partially. It may include physical characteristics but also particular processing functions and available data.

Environment awareness can be implemented with events. Table 4 defines the event types that reflect the variations of the considered mobile environment. Related information can be attached to events. Notifications are made in pull and push manners. This approach facilitates immediate and deferred triggering of $T_{AMTS}$.

TransMobi uses an event service (Events component in Fig. 5b). Such a service produces environment events from information supplied by environment monitors of different types and levels (e.g. operating system or communication layer). Some events are easy to generate, for instance, the $e$-bandwidth-rate-changes can be estimated by using knowledge of the active wireless interface (determined from active wireless card) or by obtaining the link latency and connection throughput. The $e$-connection event can be obtained by using the environment monitors $mhnicp$ or $pumicp$ proposed in modules of the Columbia Mobile IP [IOA 91]. There are events like $e$-communication-price-changes which may be obtained from a kind of environment profile where information related to contracts with wireless network providers are stocked.

4.3. TransMobi Protocols

This section presents the protocols to provide the properties of the AMT model (see Section 2.4), particularly, semantic atomicity and global serializability. Thanks to the assumptions made by the AMT model – each $T_{AMT}$ has only one $EA_k$ active – the commit/abort of $EA_k$ ensures semi-atomicity.

4.3.1. Semantic Atomicity

**CO2PC Protocol**

Our objective is to provide semantic atomicity for execution alternatives by allowing participants to perform either optimistic local commit (locally committed results are shared) or non-optimistic commit. We attempt to increase the flexibility of participants (particularly MHs), thus compensable transactions can be committed locally in an optimistic manner, whereas non-compensable ones have to wait for the global $EA_k$ decision.

We propose CO2PC, a Combination of an Optimistic approach and 2PC [GRA 78]. CO2PC works as follows: all participants send a vote (commit/abort) to the coordinator which takes the global decision and sends it to all participants. An unanimous vote for commit leads to a commit decision, otherwise the decision is abort.

Participants are TMClients or TMServers working with a local DBMS. The CO2PC coordinator must be a participant FH. If there is no FH participant then a TMAgent will play this role. MH should not be coordinator because they are subject to frequent disconnections and have restrained resources for logging and communication.

A participant making optimistic commit (called $opt$-participant) executes its $t_{ki}$ and commits/aborts it unilaterally. Then, it sends its vote to the coordinator. If the
Figure 6. CO2PC example.

global decision is commit, opt-participants are done; if it is abort they have to launch compensating transactions. Fig. 6 shows CO2PC with one opt-participant (MH B).

A participant making non-optimistic commit (called non-opt-participant) executes the 2PC protocol locally. The TMClient (or TMServer) acts as coordinator for this 2PC and the unique participant is the underlying DBMS. In Fig. 6, MH A and FH C are non-opt-participants. The TMClient/TMServer initiate the 2PC with their respective DBMSs (prepare message). Each DBMS sends its vote to the TMClient/TMServer which forwards it to the CO2PC coordinator. If the vote is abort, the participant aborts the transaction unilaterally, otherwise it enters a prepared state. When the decision of the CO2PC coordinator arrives to participants, the corresponding commit/abort is executed on the underlying DBMS. Notice that the 2PC part of the protocol is made on the same host and does not require messages through the wireless network. Fig. 6 shows that only vote and decision messages are transmitted over the wireless network (2 messages per participant).

In order to tolerate MH disconnections, to limit undefined blocking and to break eventual deadlocks, CO2PC uses timers. A timeout is assigned to each $t_{ki}$ and to $EA_k$s. Commits must be done before timeouts expire. Timeouts could be renegotiated for instance, when an MH disconnection period is known in advance. When a participant votes commit, it deactivates its timer and has to wait for the global decision. If the $EA_k$ timeout expires before the coordinator has all votes, the $EA_k$ is aborted or compensated (consequently the TAMT).

2PC is used by CO2PC because – for non-compensable transactions – resources must be retained until a global commit/abort. 2PC provides this state, besides it ensures atomicity, produces recoverable systems, avoids cascading aborts (when it is combined with two-phase locking) and its interface is widely implemented.

Notice that 2PC is not used for the global coordination of $T_{AMT}$ atomicity. 2PC is not the best choice for mobile environments because it requires a high rate of messages (four per participant) and it blocks the entire global transaction for an undefined period of time, until a global decision is made. This is particularly constraining in the mobile context. Moreover, light MHs may not support the 2PC interface or may not have enough resources to spend on it. Thus, trying to address several kind of transactions

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7. A non-compensable transaction cannot be executed on a DBMS not supporting 2PC.
To provide recovery, CO2PC records its progressing steps in the coordinator and participant logs. Since failures and disconnections can occur at any moment, logging information should be forced to be written (i.e. flushed into a stable storage) before sending messages. For MHs, CO2PC information will be logged in the TMClient log as well as in the corresponding TMAgent. Physical storage of MH is not considered stable because MHs are subject to lost, damages and undefined disconnections.

Table 5 shows information to be logged by the participants and the coordinator. In order to preserve DBMS heterogeneity, we make no assumptions about the recovery policy used by underlying DBMS. To preserve autonomy, recovery information (e.g. logs) is not required.

Once compensating transactions are initiated they should complete successfully. This characteristic is called persistence of compensation [GAR 87] and is ensured by resubmitting compensating transactions until they commit. If persistence of compensation is guaranteed there is no need to use an atomic commit protocol to obtain the atomicity of the set of $ct_{ki}$s of an $EA_k$. $ct_{ki}$s of sequentially executed $tk_i$S are executed in the reverse commit order. Other $ct_{ki}$s can be executed concurrently.

### 4.3.2. Global Serializability

Concurrency control algorithms synchronize concurrent transactions by ordering their conflicting operations such that a serialization order can be maintained. At a global level ($EA_k$), determining conflicts is not easy, particularly when DBMSs do not share local management information. Two global transactions without direct conflicts may however conflict if there exists local transactions that do not belong to $EA_k$s - such conflicts may affect the consistency of value dependent component transactions. These indirect conflicts are known at global level only if DBMS autonomy is relaxed. In our context, DBMS autonomy is respected. To provide global serializability two conditions should hold. (1) local DBMS should produce serializable and recoverable schedules. (2) each local DBMS should maintain the subtransactions relative order determined at global level.

Thanks to the assumptions that we made (underlying DBMSs preserve ACID properties), the first condition holds. To guarantee the second condition, we propose to use the Optimistic Ticket Method (OTM) [GEO 93]. Several reasons motivate our choice:

<table>
<thead>
<tr>
<th>Hosts</th>
<th>Log information</th>
</tr>
</thead>
<tbody>
<tr>
<td>Opt-participant</td>
<td>Commit, Acknowledge</td>
</tr>
<tr>
<td>Non-opt-participant</td>
<td>Start2PC, Prepare</td>
</tr>
<tr>
<td>All participants</td>
<td>Vote, Decision</td>
</tr>
<tr>
<td>Coordinator</td>
<td>StartCO2PC, Votes, Decision</td>
</tr>
</tbody>
</table>

Table 5. Logging during CO2PC.
– OTM maintains global serializability.
– Autonomy of underlying DBMS is preserved. No information about local ordering is required.
– No extra wireless messages are necessary.
– Concerning traditional approaches, using homogeneous concurrency control protocols does not guarantee global serializability. Exception is using strong 2PL [BER 87], however this approach does not allow early unlocking (i.e. optimistic commit) and is therefore not suitable for mobile environments.
– Sequential execution of global transactions preserves global serializability only when it is combined with timestamp ordering [BER 87]. This approach is not suitable because it reduces concurrency, and applied to mobile environments may generate undefined waiting periods of time for the entire system.

The main idea in OTM is that indirect conflicts are converted into direct ones. For this, each underlying DBMS has a special data item, called ticket. Each global subtransaction reads the ticket at the host where it executes (there is one ticket by host), increments it, and writes it into the database. At global level, a global serialization graph (GSG) is maintained.

TransMobi uses OTM at $EA_k$ level and combines it with CO2PC. The GSG is maintained by a global serializability manager (SM), located on a TMServer. When the commit process of an $EA_k$ begins, the SM creates an $EA_k$ node in the GSG. Each $t_{ki}$ increments the ticket and when the execution terminates the participant sends the vote and the ticket value to the CO2PC coordinator. The latter sends the ticket value to the SM which inserts edges between $EA_k$ and recently committed $EA_j$s. Edges must reflect the relative ticket order [GEO 93]. As soon as a cycle is generated, the SM advises the coordinator which aborts the $EA_k$. If no cycle is generated, after all edges have been inserted, the coordinator is able to commit $EA_k$. Communication cost to maintain the GSG is minimal: 1 message to create the $EA_k$ node (from the CO2PC coordinator), 1 message by participant to transmit the ticket (from the CO2PC coordinator) and 1 message to validate/abort $EA_k$ (to the CO2PC coordinator). Maintaining GSG does not require extra wireless messages. Information needed by the SM is included in messages used in the CO2PC process.

4.4. Disconnection Management

A key property of mobile computing is to support disconnections as a normal state of the system. For this, TransMobi gives support to disconnections at a transactional level. That is, during the transaction execution, participant MHs may disconnect. There are two kinds of disconnection, the programmed one and the unexpected one. The former is requested by the user and the latter is a consequence of some mobile environment variations e.g. MH is out of the area covered by the wireless network or MH battery is exhausted.

TransMobi protocols tolerate both kind of disconnections. In CO2PC, after the vote is sent, an MH may disconnect temporally. In that case, the coordinator de-
cision is logged in a TMAgent and sent to the MH when reconnection occurs. In the same way, the timeout assigned to each component transaction allows the MH to disconnect provided that the vote is sent before the timeout expires. Both, opt and non-opt-participants may disconnect. Nevertheless resources of non-opt-participants will remain blocked until reconnection (because their 2PC phase is not finished).

Concerning the OTM protocol, disconnections are not a problem because the serialization order is dictated by the ticket updating. This is completely independent of the MH connection state. The unique requirement is to send the ticket value to the coordinator. Nevertheless, the disconnection duration has an important consequence. The GSG is constructed in the commit order of the execution alternatives (actually the $T_{AMT}$s). Thus, if there is a conflict, the alternative trying to be serialized will be aborted. That is, the abort/success probability is related to the time that a transaction takes to be serialized.

5. Related Work

The AMT model was inspired from DOM [BUC 92] and Flex [ELM 90] where the general idea is to define equivalent transactions for being executed in case of failures. The DOM transaction model allows close and open nested transactions. Compensating transactions as well as contingency ones can be specified for being executed if a given transaction fails. In the Flex transaction model, contingency transactions are defined in terms of functionally equivalent transactions. A failure order is defined where the execution of a transaction depends on the failure of another one. Unlike AMT, DOM and Flex transactions are not defined to deal with mobile environments and the notion of context awareness is not considered.

The panorama of mobile transactions is vast. A detailed analysis of several works is given in [SER 03b]. In general, the adaptability vision is very limited, almost all studied systems adapt their behavior to support disconnections. Only Moflex [KU 00] addresses execution adaptability when hand-off occur. On the contrary, our proposition – AMT model – can take into account any defined environment characteristics. As in KT [DUN 97], Pre-serialization [DIR 00] and Moflex [KU 00], our work addresses mobile transactions as multidatabase ones. Unlike AMT, none of these propositions consider execution on MHs.

Concerning atomicity protocols for mobile environments we identify UCM [BOB 00] and TCOT [KUM 02]. UCM defines an Unilateral Commit Protocol that supports off-line executions (on MHs) and disconnection. Several assumptions are made, for instance, all participants are constrained to use strict 2PL and at commit time the effects of all local transactions are logged on stable storage. UCM guarantees atomicity and durability, nevertheless, transactions are blocked until global commit and log of updates must be flushed (on a FH) at each transaction commit. In TCOT, participants may commit locally before the global commit using timeouts. If global commit fails, compensating transactions are executed. To be able to commit independently, a mobile participant must send its log of updates to the coordinator. This protocol does
not take disconnections into account. Our proposal – CO2PC – makes no as-
ssumptions about concurrency control and recovery techniques used by DBMS participants. Thus, their autonomy is preserved and heterogeneity is allowed. Further, CO2PC re-
duces the use of the wireless network (2 messages by participant are necessary) and allows cohabitation of compensable and non-compensable transactions.

6. Conclusion and Perspectives

This paper addressed mobile transactions and made several contributions: (1) We proposed the AMT model inspired by previous extended transaction models. How-
ever, we put a special emphasis on environment awareness by considering specific dimensions, e.g., bandwidth rate, connection state, mobile host resources, etc. The model concerns transactions involving several heterogeneous DBMS running on mo-
bile or fixed hosts. (2) We provided an analytical study that can be viewed as a semi automatic tool to optimize mobile transaction design and executions. This is done by an a priori study of several execution alternatives and their respective probabilities of success. (3) We defined a TransMobi middleware which implements the AMT model. It uses a client/agent/server architecture and among others it manages environment awareness based on events. (4) Inside TransMobi we proposed the CO2PC commit protocol to guarantee semantic atomicity of $T_{AMT}$. It preserves the autonomy of participant DBMSs, reduces the use of the wireless network (2 messages by participant are necessary) and allows cohabitation of compensable and non-compensable trans-
actions. (5) We developed a prototype of TransMobi. It uses Personal Java and the PointBase DBMS (Java package). Mobile hosts are of type Ipaq H3850 (Compaq) over a WLAN 802.11b. This is a first prototype to validate our ideas. Experiences in a more general environment for specific mobile applications are part of our future works.

Research perspectives include:

(1) The implementation of an application developer utility in order to facilitate the design of AMT transactions. Environment awareness provided by TransMobi can be used to profile the application environment and users habits. Once the environment profiled, an analytical calculus – like the one presented here – could be done to dy-
namically optimize $T_{AMT}$ in regards to required quality of service. (2) The analysis of the suitability of adapting transactions not only at the beginning (as done in our cur-
rents proposal) but also during their execution; aspects related to reusing work already done by the adapted transaction have to be explored. (3) Applying the AMT model to peer-to-peer and network ad-hoc environments; as the mobile environment they are characterized by high variability.

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7. References


