Spectral and Spatial Classification of Hyperspectral Data Using SVMs and Morphological Profiles
Mathieu Fauvel, Jon Atli Benediktsson, Jocelyn Chanussot, Johannes R. Sveinsson

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Abstract—A method is proposed for the classification of urban hyperspectral data with high spatial resolution. The approach is an extension of previous approaches and uses both the spatial and spectral information for classification. One previous approach is based on using several principal components from the hyperspectral data and building several morphological profiles. These profiles can be used all together in one extended morphological profile. A shortcoming of that approach is that it was primarily designed for classification of urban structures and it does not fully utilize the spectral information in the data. Similarly, the commonly used pixel-wise classification of hyperspectral data is solely based on the spectral content and lacks information on the structure of the features in the image. The proposed method overcomes these problems and is based on the fusion of the morphological information and the original hyperspectral data, i.e., the two vectors of attributes are concatenated into one feature vector. After a reduction of the dimensionality the final classification is achieved using a Support Vector Machines classifier. The proposed approach is tested in experiments on ROSIS data from urban areas. Significant improvements are achieved in terms of accuracies when compared to results obtained for approaches based on the use of morphological profiles based on PCs only and conventional spectral classification. For instance, with one data set, the overall accuracy is increased from 79% to 83% without any feature reduction and to 87% with feature reduction. The proposed approach also shows excellent results with a limited training set.

Index Terms—Data fusion, hyperspectral data, support vector machines, feature extraction, extended morphological profile, high spatial resolution.

I. INTRODUCTION

In classification of remote sensing data from urban areas, the identification of relatively small objects, e.g., houses and narrow streets is important. Therefore, high spatial resolution of the imagery is necessary for accurate classification. The most commonly available remote sensing data of high spatial resolution from urban areas are single-band panchromatic data. However, using only one high-resolution panchromatic data channel is usually not sufficient for accurate classification of structural information. To overcome that problem, Pesaresi and Benediktsson [1] proposed the use of morphological transformations to build a Morphological Profile (MP). In [2] the method in [1] was extended for hyperspectral data with high spatial resolution. The approach in [2] is based on using several Principal Components (PCs) from the hyperspectral data. From each of the PCs, a morphological profile is built. These profiles are used all together in one Extended Morphological Profile (EMP), which is then classified by a neural network. The method in [2] has been shown to perform well in terms of accuracies when compared to more conventional classification approaches. However, a shortcoming of the approach is that it is primarily designed for classification of urban structures and it does not fully utilize the spectral information in the multispectral or hyperspectral data.

However this type of data contains a lot of information about the spectral properties and the land cover of the data. A finer definition of the classes is possible and more classes can be considered. Based on the spectral signatures of the classes, many advanced pixel-based classifiers have been proposed including advanced statistical classifiers [3] and distribution free approaches such as neural networks and support vector machines [4]. The later one has shown remarkable abilities to deal with remote multispectral data, especially with hyperspectral data. However, if the spatial content of the image is not used the resulting thematic map sometimes looks noisy (salt and pepper classification noise). Approaches involving Markov Random Field (MRF) and Monte Carlo optimization have been proposed in [5], [6]. These approaches use the contextual information. The main shortcoming of such algorithms is the computing time, which can be high even for small data sets. Regarding the high dimensionality of recently acquired data, both in the spectral and in the spatial domain, computationally light algorithm are of interest. In this sense, the MP has been proposed as an alternative way to use spatial information [1], [7]. Relatively to the MRF-based classifiers, the MP and its extension to a multiband image, the EMP, have the possibility to use geometrical contextual information (shape, size, etc) and perform well on many kinds of data (panchromatic, multispectral and hyperspectral data). However, as stated above, a shortcoming of this approach is it does not fully utilize the spectral information in the data, and consequently several approaches based on the MP/EMP have been proposed to fully exploit the spatial and the spectral information [8]–[10].

Each data set has its own properties, defining its ability to deal with different natures of classes. Table I sums up the properties of spectral and morphological/spatial data. The first main consideration is the complementary characteristics of the
data. It has a consequence in the discrimination ability of such a feature, as will be seen in the experiments. The fusion of two types of information should clearly results in an increase of the classification in terms of global accuracy. The use of spectral information can be critical for classification of non-structured information in urban areas, e.g., vegetation and soil classes while the use of spatial information can be useful for classification of structured objects, e.g., road and building classes.

The second consideration is the possible redundancy of each features set, see [3] for the spectral features and [11] for the spatial features. Hence feature extraction (FE) algorithms could be of an interest.

To include both type of information an extension to the approach in [2] is proposed in this paper. The proposed method is based on the data fusion of the morphological information and the original data: First, an extended morphological profile is created based on the PCs from the hyperspectral data. Secondly, feature extraction is applied on the original hyperspectral data and the extended morphological profile. Finally, the extracted feature vectors from both the original data and the extended morphological profile are concatenated into one stacked vector and classified. The proposed approach is different from approaches in [12–14], where the authors had extracted spatial information and used composite kernel to include both type of information. Here, feature extraction algorithms are used to select informative feature from the spectral and spatial domain.

For the multisource classification, Support Vector Machines (SVM) are used rather than a Neural Network, which was already been applied for multisource classification in [17] where SVM have already been applied for multisource classification in [17] where several output coding methods were investigated.

In this paper, the proposed approach has been compared to statistical classification methods and SVM classification. Experiments were conducted on two different high resolution remote sensing data sets from urban areas. The effectiveness of the proposed methodology with a limited training set has been also assessed.

The paper is organized as follows. Section II reviews the use of morphological transformations for processing of hyperspectral imagery in urban areas. In Section III, the considered supervised feature extraction approaches are introduced. Support Vectors Machines (SVM) are discussed in Section IV. The applied data fusion schemes are discussed in Section V. Experimental results obtained on two ROSIS data sets from urban areas are presented in Section VI. Finally, conclusions are drawn in Section VII.

<table>
<thead>
<tr>
<th>Spectral features</th>
<th>Mathematical Morphology</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fine physical description</td>
<td>Geometrical information</td>
</tr>
<tr>
<td>Directly accessible</td>
<td>Needs to be extracted</td>
</tr>
<tr>
<td>Redundancy</td>
<td>Redundancy</td>
</tr>
<tr>
<td>No spatial information</td>
<td>Reduced spectral information</td>
</tr>
</tbody>
</table>

II. EXTENDED MORPHOLOGICAL PROFILE

Mathematical Morphology is a theory aiming to analyze spatial relationship between pixels. For a remote sensing application, several morphological operators are available for extracting geometrical information. An overview of operators can be found in [18]. In the following sub-section, some basic notions of mathematical morphology are reviewed. Then, the concept of the Morphological Profile and its extension to multivalued data are detailed.

A. Mathematical Morphology

The two fundamental operators in mathematical morphology are erosion and dilation [19]. These operators are applied to an image with a set of known shape, called a structuring element (SE). To erode an image consists of finding where the SE fits the objects in the image. The dilation, which is dual to the erosion, shows where the SE hits the objects. Opening and closing are combinations of erosion and dilation. These operators remove from an original image structures of size less than the SE. But they also modify structures which are still present in the image after the opening/closing. Thus, they can introduce fake objects in the image. To avoid this problem, geodesic morphology and reconstruction should be used [19]. Opening and closing by reconstructions are connected operators that satisfy the following assertion: If the structure of the image cannot contain the SE, then it is totally removed, else it is totally preserved. For a given SE, geodesic opening or geodesic closing allows to know the size or shape of some objects present in the image: The objects that are smaller than the SE are deleted while the other (that are bigger than the SE) are preserved. To determine the shape or size of all elements present in an image, it is necessary to use a range of different SE sizes. This concept is called Granulometry.

Granulometries are typically used for the analysis of the size distribution of the structures in the images. Classical granulometry by opening is built by successive opening operations with an SE of an increasing size. By doing so, the image is progressively simplified. Using connected operators, like opening by reconstruction, no shape noise is introduced.

Morphological Profiles (MPs) are defined using the granulometry. An MP is composed of the opening profile (OP) and the closing profile (CP). The OP at the pixel x of the image I is defined as an n-dimensional vector:

\[
OP_i(x) = \gamma_R^{(i)}(x), \forall i \in [0, n]
\]

where \(\gamma_R^{(i)} \) is the opening by reconstruction with an SE of a size i and n is the total number of openings. Also, the CP at
the pixel \( x \) of image I is defined as an \( n \)-dimensional vector:
\[
CP_i(x) = \phi_R^{(i)}(x), \quad \forall i \in [0, n]
\]
(2)
where \( \phi_R^{(i)} \) is the closing by reconstruction with an SE of a size \( i \). Clearly we have \( CP_0(x) = OP_0(x) = I(x) \). By collating the \( OP \) and the \( CP \), the MP of image I is defined as \( 2n + 1 \)-dimensional vector:
\[
MP(x) = \{CP_n(x), \ldots, I(x), \ldots, OP_n(x)\}
\]
(3)
Example of MP is shown in Fig. I. Thus, from a single image results a multiband image, whose dimension corresponds to the number of transformations and spatial information is now contained in the MP for each pixel. However, an MP is built with only one band. Therefore, the spectral information is lost. One approach to deal with this problem is to extract several images that contain some parts of the spectral information and then build the MP on each of the individual images. This approach, namely the Extended Morphological Profile (EMP), is discussed in the following.

B. Extended Morphological Profile

In order to apply this approach to hyperspectral data, characteristic images need to be extracted. In [11], it was suggested to use several principal components of the hyperspectral data for such a purpose. Hence, the MP is applied on the first PCs, corresponding to a certain amount of the cumulative variance and a stacked vector is built with the MP on each PC. This yields to the extended morphological profile (EMP). Following the previous notation, the EMP is an \( m(2n + 1) \)-dimensional vector:
\[
MP_{ext}(x) = \{MP_{PC1}(x), \ldots, MP_{PCm}\}
\]
(4)
where \( m \) is the number of retaining PCs. Example of EMP is shown in Fig. 2.
As with multispectral data, the MP/EMP may include some redundancy. Classical feature reduction algorithm can be applied, as detailed in the following section.

III. Supervised Feature Extraction

Feature extraction can be viewed as finding a set of vectors that represents an observation while reducing the dimensionality. In pattern recognition, it is desirable to extract features that are focused on discriminating between classes of interest. Although a reduction in dimensionality is desirable, the error increment due to the reduction in dimension has to be without sacrificing the discriminative power of classifiers. In linear feature extraction, the number of input dimensions corresponds to the number of selected eigenvectors [3]. The transformed data are determined by
\[
\tau = \Phi^T x
\]
where \( \Phi \) is the transformation matrix composed of the eigenvectors of the feature matrix, \( x \) is the data in the input space and \( \tau \) is the transformed data in the feature space. We have in general \( \dim(x) \geq \dim(\tau) \). Several statistical extraction approaches have been proposed for remote sensing data [3], including Decision Boundary Feature Extraction (DBFE) and Nonparametric Weighted Feature Extraction (NWFE).

A. Decision Boundary Feature Extraction

It was shown in [20], that both discriminantly informative features and redundant features can be extracted from the decision boundary between two classes. The features are extracted from the decision boundary feature matrix (DBFM). The eigenvectors of the DBFM corresponding to non-zero eigenvalues are the necessary feature vectors to achieve the same classification accuracy as in the original space. The efficiency of the DBFE is related to the training set and can be computationally intensive.

B. Nonparametric Weighted Feature Extraction

To overcome the limitations of the DBFE, Kuo and Landgrebe [21] proposed the nonparametric weighted feature extraction. NWFE is based on the Discriminant Analysis Feature Extraction by focusing on samples near the eventual decision boundary. The main ideas of the NWFE are 1) putting different weights on every sample to compute the local means and 2) defining nonparametric between-class and within-class scatter matrices [3].

Many experiments have shown the effectiveness of these approaches for the classification of hyperspectral data [3]. They are usually applied on the spectral data, but it was successfully applied to the EMP [11].

IV. Classification by the Support Vector Machine

So far, in our previous approach [2], [7], [11], [22] the classification was done with either a statistical classifier (Gaussian Maximum Likelihood), a neural network or a fuzzy classifier. Here it is proposed to use the Support Vector Machines (SVM). Early work in classification of remotely sensed images by SVM showed excellent results [17], [23], [24]. In [15], several SVM-based classifiers were compared to other classical classifiers such as a K-nearest neighbors classifier and a neural network classifier and the SVM using the kernel method outperformed the other classifiers in terms of accuracy. Multiclass SVM performances were also positively compared with a discriminant analysis classifier, a decision tree classifier and a feedforward neural network classifier with a limited training set [25]. SVM show good results in the situation of limited training set in [26]. Semisupervised SVM were also investigated for multi-spectral data classification [27], [28].

SVM are surely among the most used kernel learning algorithm. It performs robust non-linear classification of samples using the kernel trick. The idea is to find a separating hyperplane.
in some feature space induced by the kernel function while all the computations are done in the original space [4]. A good introduction to SVM for pattern recognition can be found in [29]. Given a training set \( S = \{ (x^1, y_1), \ldots, (x^t, y_t) \} \in \mathbb{R}^n \times \{-1; 1\} \), the decision function is found by solving the convex optimization problem:

\[
\max_{\alpha} g(\alpha) = \sum_{i=1}^{t} \alpha_i - \frac{1}{2} \sum_{i,j=1}^{t} \alpha_i \alpha_j y_i y_j k(x^i, x^j)
\tag{6}
\]

subject to \( 0 \leq \alpha_i \leq C \) and \( \sum_{i=1}^{t} \alpha_i y_i = 0 \)

where \( \alpha \) are the Lagrange coefficients, \( C \) a constant that is used to penalize the training errors, and \( k \) the kernel function. To be an acceptable kernel, \( k \) should be a positive semi-definite function [30]. One classical effective kernel is the Gaussian kernel:

\[
k_\sigma(x^i, x^j) = \exp\left(-\frac{\|x^i - x^j\|^2}{2\sigma^2}\right)
\tag{7}
\]

where the norm is the Euclidean-norm and \( \sigma \in \mathbb{R}^+ \) tunes the flexibility of the kernel. A short comparison of kernels for remotely sensed image classification can be found in [26].

When the optimal solution of (6) is found, i.e., the \( \alpha_i \), the classification of a sample \( x \) is achieved by looking to which side of the hyperplane it belongs:

\[
y = \text{sgn}\left(\sum_{i=1}^{t} \alpha_i y_i k(x^i, x) + b\right).
\tag{8}
\]

To deal with multicase classification problem, the pairwise approach was used in our experiments [31]. More advanced multiclass approaches applied to remote sensing data can be found in [15]. For the particular case of one-class-classification, a dedicated methodology is proposed in [32].

The SVM are mainly a non-parametric method, yet some parameters need to be tuned before the optimization. In the Gaussian kernel case, there are two parameters: \( C \), the penalty term, and \( \sigma \), the with of the exponential. It is usually done by a cross-validation step, where several values are tested. In our experiments, \( C \) was fixed to 200 and \( \sigma^2 \in \{0.5, 1, 2, 4\} \) was selected using a 5-fold cross validation. The SVM optimization problem was solved using the LIBSVM [33].

V. DATA FUSION

The proposed method is based on the data fusion of the morphological information and the original data. In a previous work [34], it was proposed to fuse the classification results of two SVM classifiers, each one working with either the spectral or the EMP data. It consisted in an appropriate adaptive fusion scheme based on the output’s characteristics of the SVM. The results in terms of accuracy were increased but it needed two training of SVM, that could be time consuming.

Here it is proposed to use a multisource strategy to fuse spectral and spatial information. First, an EMP is created based on applying the PCA on the hyperspectral data. Secondly, feature extraction is applied on both the EMP and the original hyperspectral data. Finally, the extracted feature vectors are concatenated into one stacked vector and classified by the SVM.

In the morphological processing we usually retain PCs corresponding to 99% of the cumulative variance. This is done in order to reduce the redundancy in the data but keep most of the variation. The EMP is built using the \( m \) PCs that correspond to the 99% variance. Each MP is composed of \( n \) geodesic openings, \( n \) geodesic closing and the corresponding PC. The SE is a disk with initial radius of \( r \) pixels. The size increment is \( s \). Hence, each MP has \( 2n + 1 \) features and the EMP has \( m(2n + 1) \) features. Noting \( x_\varphi \), the features associated to the spectral bands and \( x_\omega \), the features associated to the EMP, the corresponding extracted features from the FE algorithm are:

\[
\begin{align*}
    r_\varphi &= \Phi_\varphi^T x_\varphi \\
    r_\omega &= \Phi_\omega^T x_\omega.
\end{align*}
\tag{9}
\]

The stack vector is finally \( r = [r_\varphi, r_\omega]^T \).

Fig. 3 presents the data fusion scheme. Note that in this work, only morphological information is extracted, but it is possible to extract other types of spatial information with other processing and include them in the stacked vector.

VI. EXPERIMENTS

A. Data set

Airborne data from the ROSIS-03 (Reflective Optics System Imaging Spectrometer) optical sensor are used for the experiments. The flight over the city of Pavia, Italy, was operated by the Deutsches Zentrum fur Luft- und Raumfahrt (DLR, the German Aerospace Agency) in the framework of the HySens project, managed and sponsored by the European Union. According to specifications, the number of bands of the ROSIS-03 sensor is 115 with a spectral coverage ranging from 0.43 to...
TABLE II
INFORMATION CLASSES AND TRAINING-TEST SAMPLES FOR THE
UNIVERSITY AREA data set.

<table>
<thead>
<tr>
<th>No</th>
<th>Name</th>
<th>Train</th>
<th>Test</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Asphalt</td>
<td>541</td>
<td>6641</td>
</tr>
<tr>
<td>2</td>
<td>Meadows</td>
<td>540</td>
<td>18649</td>
</tr>
<tr>
<td>3</td>
<td>Gravel</td>
<td>392</td>
<td>2099</td>
</tr>
<tr>
<td>4</td>
<td>Trees</td>
<td>524</td>
<td>3921</td>
</tr>
<tr>
<td>5</td>
<td>Metal Sheets</td>
<td>265</td>
<td>1345</td>
</tr>
<tr>
<td>6</td>
<td>Soil</td>
<td>532</td>
<td>5029</td>
</tr>
<tr>
<td>7</td>
<td>Bitumen</td>
<td>375</td>
<td>1330</td>
</tr>
<tr>
<td>8</td>
<td>Bricks</td>
<td>514</td>
<td>3682</td>
</tr>
<tr>
<td>9</td>
<td>Shadows</td>
<td>231</td>
<td>947</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>3921</td>
<td>42776</td>
</tr>
</tbody>
</table>

TABLE III
INFORMATION CLASSES AND TRAINING-TEST SAMPLES FOR THE PAVIA
CENTER data set.

<table>
<thead>
<tr>
<th>No</th>
<th>Name</th>
<th>Train</th>
<th>Test</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Water</td>
<td>824</td>
<td>65971</td>
</tr>
<tr>
<td>2</td>
<td>Trees</td>
<td>820</td>
<td>7598</td>
</tr>
<tr>
<td>3</td>
<td>Meadows</td>
<td>824</td>
<td>3090</td>
</tr>
<tr>
<td>4</td>
<td>Bricks</td>
<td>808</td>
<td>2685</td>
</tr>
<tr>
<td>5</td>
<td>Soil</td>
<td>820</td>
<td>6584</td>
</tr>
<tr>
<td>6</td>
<td>Asphalt</td>
<td>816</td>
<td>9248</td>
</tr>
<tr>
<td>7</td>
<td>Bitumen</td>
<td>808</td>
<td>7287</td>
</tr>
<tr>
<td>8</td>
<td>Tiles</td>
<td>1260</td>
<td>42826</td>
</tr>
<tr>
<td>9</td>
<td>Shadows</td>
<td>476</td>
<td>2863</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>7456</td>
<td>148152</td>
</tr>
</tbody>
</table>

0.86μm. The data have been atmospherically corrected but not
georometrically corrected. The spatial resolution is 1.3m per pixel.
Two data sets were used in the experiment:

1) University Area: The first test set is around the Engi-
neering School at the University of Pavia. It is 610 by
340 pixels. Some channels (twelve) have been removed
due to noise. The remaining 103 spectral dimensions
are processed. Nine classes of interest are considered,
i.e., trees, asphalt, bitumen, gravel, metal sheets, shadow,
bricks, meadows and soil.

2) Pavia Center: The second test set is the center of Pavia.
The Pavia center image was originally 1096 by 1096
pixels. A 381 pixel wide black stripe in the left part of
image was removed, resulting in a “two parts” image. This
“two parts” image is 1096 by 715 pixels. Some channels
(thirteen) have been removed due to noise. The remaining
102 spectral dimensions are processed. Nine classes of
interest are considered, i.e., water, trees, meadows, bricks,
soil, asphalt, bitumen, tiles and shadows.

Available training and testing set for each data set are given in
Table II and III and Fig. 4 presents false colors images for both
data set.

The classification accuracy was assessed with:

- An overall accuracy (OA) which is the number of well
  classified samples divided by the number of test’s samples
- An average accuracy (AA) which represents the average of
  class classification accuracy
- A kappa coefficient of agreement (κ) which is the percent-
age of agreement corrected by the amount of agreement
that could be expected due to chance alone [35].

These criteria were used to compare classification results and
were computed using the confusion matrix. Furthermore, the
statistical significance of differences was computed using Mc-
Nemar’s test, which is based upon the standardized normal test
statistic [36]:

$$Z = \frac{f_{12} - f_{21}}{\sqrt{f_{12} + f_{21}}} \quad (11)$$

where $f_{12}$ indicates the number of samples classified correctly
by classifier 1 and incorrectly by classifier 2. The difference in
accuracy between classifiers 1 and 2 is said to be statistically
significant if $|Z| > 1.96$. The sign of $Z$ indicates whether
classifier 1 is more accurate than classifier 2 ($Z > 0$) or vice-
versa ($Z < 0$). This test assumes related testing samples and
thus is adapted to our situation since the training and testing set
were the same for each experiment.

The feature extractions were done with MultiSpec© [3] while
the morphological operations were done with the Image Pro-
cessing Toolbox of Matlab©. The SVM classification was done
using the LIBSVM through its Matlab© interface [33]. From
previous experiments on the same data set, the Gaussian kernel
provides the best results and was used for the experiments [26].
The range of each feature, be it spectral or morphological, was
stretched between 0 and 1.

To obtain a baseline result for comparison, the classification
was also done using the Gaussian Maximum Likelihood (ML)
classifier on the hyperspectral data using MultiSpec©. Feature
extraction was done using the two FE algorithms (DBFE and
NWFE) but only the best results have been reported for both
data sets. The results were compared to those obtained by the
proposed approach.

1 For the ML, the kappa coefficient was not accessible.
B. University Area data set

PCs were computed from the hyperspectral data. The results for the eigenvalues are shown in Table IV. The left column gives the component number, the center column the eigenvalues in percentage of the total amount of variance and the right column the cumulative amount of variance. From the table, three PCs were necessary to retain 99% of the variance criterion. EMPs were built according to the scheme presented in the Section V. A circular SE with a step size increment of 2 was used. Four openings and closings were computed for each PC, resulting in an EMP of dimension 27.

First, the classification with SVM was done using the spectral information and the extended morphological profile. The best ML accuracy was obtained using 8 features extracted with the NWFE, following Landgrebe's recommendations in [3].

The results are reported in Table V. Regarding the global accuracies, both SVM approaches perform equally well, for instance the difference between the classification using the spectral information and the EMP is not statistically significant, see Table VI. Note that it is consistent with the characteristics of the scene: The University Area is a mix between man-made structures and natural materials. Therefore, the morphological information is not as useful as it could be in a very dense urban area. When a careful analysis is done on the class-specific accuracies, we can see from Table V that each approach performed well for complementary classes, e.g. the spectral approach performed better for classes 3, 6, 9 while the EMP approach performed better for classes 1, 2, 7, 8. After the data fusion we have to look at these classes and see if the best information was used, i.e., if the classification accuracy increased for these classes.

The experiment was then performed with the concatenated vector. The vector was made of the 103 spectral bands and the 27 features of the EMP. The vector was directly used as an input to the SVM. The classification results are reported in Table V. As can be seen from the table, the global accuracies increased. The $\kappa$ value in percentage is 79.13% against 74.47% for the spectral approach and 73.25% for the EMP and the differences are statistically significant (see Table VI).

Regarding the class-specific accuracies, the results in terms of accuracies have increased for classes 1, 7, 8 when compared to both individual approaches. In fact all the classes are more accurately classified than the worst respective cases for the individual approaches.

In the last experiment, feature reduction was applied on the morphological data and the original data before the concatenation. Then the stacked vector was classified by the SVM. Table VII summarizes the test accuracies for several values of the variance criterion for the DBFE and NWFE. Best results were obtained with 95% and 80% variance criterion for the DBFE and NWFE, respectively. Using 95% of the variance criterion with DBFE, the hyperspectral data were reduced to 27 features and the EMP to 10 features. With NWFE and 80%, 7 features were extracted from the hyperspectral data and 6 from the EMP. Again, as can be seen in Table VI, differences between the classification accuracies are statistically significant.

Considering the class-specific accuracies, the DBFE approach improved the classification for class 2 while class 3 was less accurately classified than with the concatenated full hyperspectral data and EMP. However, the DBFE outperformed the individual classifications of the spatial or spectral information. On this data set, the classification of the DBFE feature extracted data gave the best classification results. Similar comments can be made for the accuracies obtained with classifications of the NWFE. Still, the number of features needed to achieve the same accuracy is significantly lower for the NWFE approach than for the DBFE. Since the SVM is linearly related to the dimensionality of the data, lower dimensional data reduced the training time and increased the speed of the classification.

To assess this increase, comparison of the processing time (training and classification process) for the different approaches was made. Table VIII summarizes the results, which are clearly different according to the features used. The training time could depend on several factors:

1) The dimension of the data;
2) The size of the training set;
3) The number of parameters for the kernel.

For our given problem, items 2) and 3) are the same. Reducing the size of the data is beneficial for the processing time, since data with lower dimensionality (EMP and NWFE) have the shortest processing time. For the best case (NWFE), the gain is about 73%.

For the classification processing time, two factors have an influence: The dimension of the data and the number of support vectors (non-zero $\alpha_i$ in (8)). Thus, approaches with low dimensionality and few support vectors perform the classification task of the whole image faster (EMP and NWFE). Nevertheless, the classification processing is really fast by comparison to the training time, in all the cases.

Classification maps for the different approaches are shown in Fig. 5.
TABLE V

**University Area. Summary of the Global and the Class-Specific Test Accuracies in Percentage for the Classification. The Numbers of Features from the Spectral Data and the Morphological Data, Respectively, Are Given in Brackets.**

<table>
<thead>
<tr>
<th>Features</th>
<th>ML (NWFE)</th>
<th>Spectral</th>
<th>EMP</th>
<th>Spec. EMP</th>
<th>DBFE 95%</th>
<th>NWFE 80%</th>
</tr>
</thead>
<tbody>
<tr>
<td>OA</td>
<td>80.10</td>
<td>79.48</td>
<td>79.14</td>
<td>82.53</td>
<td>87.95</td>
<td>87.59</td>
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<td>87.00</td>
<td>88.14</td>
<td>84.30</td>
<td>89.39</td>
<td>89.43</td>
<td>88.93</td>
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<tr>
<td>κ</td>
<td>-</td>
<td>74.47</td>
<td>73.25</td>
<td>79.13</td>
<td>84.40</td>
<td>83.89</td>
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<tr>
<td>Class 1</td>
<td>76.00</td>
<td>84.36</td>
<td>94.50</td>
<td>95.33</td>
<td>90.92</td>
<td>86.80</td>
</tr>
<tr>
<td>Class 2</td>
<td>73.90</td>
<td>66.20</td>
<td>72.82</td>
<td>73.46</td>
<td>85.91</td>
<td>86.95</td>
</tr>
<tr>
<td>Class 3</td>
<td>70.80</td>
<td>71.99</td>
<td>53.22</td>
<td>65.89</td>
<td>57.88</td>
<td>63.26</td>
</tr>
<tr>
<td>Class 4</td>
<td>96.70</td>
<td>98.01</td>
<td>98.89</td>
<td>99.18</td>
<td>99.22</td>
<td>98.53</td>
</tr>
<tr>
<td>Class 6</td>
<td>87.60</td>
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<td>58.11</td>
<td>84.15</td>
<td>85.32</td>
<td>82.62</td>
</tr>
<tr>
<td>Class 7</td>
<td>92.00</td>
<td>91.20</td>
<td>96.09</td>
<td>97.22</td>
<td>95.19</td>
<td>96.61</td>
</tr>
<tr>
<td>Class 8</td>
<td>87.30</td>
<td>92.26</td>
<td>95.27</td>
<td>96.12</td>
<td>95.84</td>
<td>95.38</td>
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<tr>
<td>Class 9</td>
<td>99.10</td>
<td>96.62</td>
<td>91.24</td>
<td>93.66</td>
<td>95.14</td>
<td>90.60</td>
</tr>
</tbody>
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TABLE VI

**University Area. Statistical Significance of Differences in Classification Accuracies.**

<table>
<thead>
<tr>
<th>EMP/Spectral</th>
<th>Spectral/Spec. EMP</th>
<th>Spectral/DBFE 95%</th>
<th>Spectral/NWFE 80%</th>
<th>Spec. EMP/DBFE 95%</th>
<th>Spec. EMP/NWFE 80%</th>
<th>DBFE 95%/NWFE 80%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Z</td>
<td>-1.36</td>
<td>-19.55</td>
<td>-37.98</td>
<td>-36.61</td>
<td>-25.19</td>
<td>-21.79</td>
</tr>
</tbody>
</table>

TABLE VIII

**University Area. Processing Time in Seconds as Function of Dimensionality and Number of Support Vectors.**

<table>
<thead>
<tr>
<th>Spectral</th>
<th>EMP</th>
<th>Spec. EMP</th>
<th>DBFE 95%</th>
<th>NWFE 80%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dimension</td>
<td>103</td>
<td>27</td>
<td>130</td>
<td>37</td>
</tr>
<tr>
<td>Training</td>
<td>3074</td>
<td>850</td>
<td>3257</td>
<td>1184</td>
</tr>
<tr>
<td>Number of SVs</td>
<td>1085</td>
<td>406</td>
<td>529</td>
<td>727</td>
</tr>
<tr>
<td>Classification</td>
<td>76</td>
<td>9</td>
<td>41</td>
<td>18</td>
</tr>
</tbody>
</table>

Fig. 5. **University Area:** Classification map obtained with SVM from: (a) the original hyperspectral data, (b) the EMP, (c) 37 DBFE features and (d) 13 NWFE features. Classification accuracies are reported in the Table V.

C. Pavia Center data set

For the second test, the scene is a very dense urban area in the center of the city of Pavia. Because of that, morphological information should be useful for the discrimination. PCs were computed from the hyperspectral data. The results for the eigenvalues are shown in Table IX. From the Table, three PCs were necessary to retain 99% of the variance criterion. The EMP was built according to the scheme presented in the section V: A circular SE with a step size increment of 2 was used. Four openings and closings were computed for each PC, resulting in
an EMP of dimension 27.

SVM classification was applied to the original hyperspectral data and the EMP. The best ML accuracy was obtained using 29 features extracted with the DBFE. The results are reported in Table X. From the Table, it can be seen that SVM classifier achieved excellent global accuracies. In these experiments, the morphological approach performs better than the spectral based approach. Table XI shows the statistical significance of differences between the classification accuracies for the different approaches. This is consistent with the characteristics of the picture: it is a very dense urban area and morphological processing provides discriminative information. In terms of accuracies, the main improvement in the classification is achieved for class 4. The other classes are classified equally accurately. The data fusion should thus improve the classification of class 4 while preserving very good results for the others classes.

Next, the experiment was performed using the concatenated vector. The vector was made of the 102 spectral bands and the 27 features of the EMP. This vector was used as an input for the SVM without any additional processing. The classification results are reported in Table X. The differences of classification accuracies between the EMP and the concatenated vector are not statistically significant, since the McNemar’s test is almost equal to zero, see Table XI. Thus, both EMP and concatenated vector perform equally well.

As in the previous experiment, feature reduction was applied both on the morphological data and on the original data before the concatenation. Then, the stacked vector was classified by the SVM. Table XII summarizes the test accuracies for several values for the variance criterion for the DBFE and NWFE. The best results are obtained with 99% variance criterion for both DBFE and NWFE. Using 99% of the variance with the DBFE, the hyperspectral data is reduced to 51 features and the EMP is reduced to 15 features. With the NWFE and 99% of the variance criterion, 44 features were extracted from the hyperspectral data and 20 from the EMP. The results are given in Table X.

For this experiment, the DBFE does not help for the classification since the Z test is not significant. On the other hand, similar classification accuracy is reached with far less features, nearly half the size of the previous feature set, thus decreasing the total training and classification time. The NWFE leads to a significant increase of the classification accuracies, $|Z| = 7.75$ by comparison to the best results obtained with the concatenation vector, which is contrary to the previous experiment. Classification maps for the different approaches are shown in Fig. 6. Visually, the thematic map produced with the classification of the NWFE features seems less noisy than the one obtained with the classification of the DBFE features. This is especially true in the top-left corner which correspond to a very dense urban area.

Regarding the computing time, the results for the training and the classification are reported in Table XIII. As expected, using feature extraction methods reduces the processing time for both the training and the classification.

Classification maps for the different approaches are shown in Fig. 6.

### D. Small training set experiment: University Area

To assess the effectiveness of the proposed methodology for a limited training set, we have randomly extracted a few training samples from the training set. For this experiment, we used 20 samples for each class, which represents less than 5% of the original training set. We have used the same EMP but had some problems with the DBFE, the covariance matrix was non-invertible (the NWFE does not suffer from this problem). In order to overcome this shortcoming and to apply the DBFE anyway, we use the leave on out covariance (LOOC) to estimate the covariance matrix and perform a statistical enhancement with unlabeled samples, both algorithms were implemented in the MultiSpec software [37], [38]. We have repeated the training samples selection and the classification process five times, and the mean classification results are reported in the paper.
TABLE X

<table>
<thead>
<tr>
<th></th>
<th>ML (DBFE)</th>
<th>Spectral EMP</th>
<th>Spec. EMP</th>
<th>DBFE 99%</th>
<th>NWFE 99%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Features</td>
<td>29</td>
<td>102</td>
<td>27</td>
<td>129</td>
<td>66 (51,15)</td>
</tr>
<tr>
<td>OA</td>
<td>94.50</td>
<td>97.67</td>
<td>98.69</td>
<td>99.69</td>
<td>98.65</td>
</tr>
<tr>
<td>AA</td>
<td>94.00</td>
<td>95.60</td>
<td>97.69</td>
<td>98.07</td>
<td>97.30</td>
</tr>
<tr>
<td>κ</td>
<td>-</td>
<td>96.71</td>
<td>98.15</td>
<td>98.15</td>
<td>98.10</td>
</tr>
</tbody>
</table>

TABLE XI

<table>
<thead>
<tr>
<th></th>
<th>EMP/Spectral</th>
<th>EMP/Spec. EMP</th>
<th>EMP/DBFE 99%</th>
<th>EMP/NWFE 99%</th>
<th>Spec. EMP/DBFE 95%</th>
<th>Spec. EMP/NWFE 80%</th>
<th>DBFE 95%/NWFE 80%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Z</td>
<td>27.84</td>
<td>-0.06</td>
<td>1.44</td>
<td>-8.14</td>
<td>1.42</td>
<td>-7.75</td>
<td>-9.44</td>
</tr>
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</table>

TABLE XIII

<table>
<thead>
<tr>
<th></th>
<th>Spectral</th>
<th>EMP</th>
<th>Spec. EMP</th>
<th>DBFE 95%</th>
<th>NWFE 80%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dimension</td>
<td>102</td>
<td>27</td>
<td>129</td>
<td>66</td>
<td>66</td>
</tr>
<tr>
<td>Training (s)</td>
<td>5178</td>
<td>1569</td>
<td>5909</td>
<td>3520</td>
<td>3962</td>
</tr>
<tr>
<td>Number of SVs</td>
<td>691</td>
<td>265</td>
<td>401</td>
<td>558</td>
<td>408</td>
</tr>
<tr>
<td>Classification (s)</td>
<td>143</td>
<td>20</td>
<td>105</td>
<td>73</td>
<td>47</td>
</tr>
</tbody>
</table>

As with the previous experiments, we perform the classification using the spectral or the morphological feature with SVM. The ML produced very poor results, simply close to random classification and hence not reported. The global accuracies are reported in Table XIV. Statistical significance of differences is reported in Table XV.

First of all, the test results are lower than those in Table V and VII, due to the limited training set. For instance, with the concatenated feature vector, the overall accuracy and the κ are respectively, 83.53% and 79.13% for the original training set while using a limited training set, the overall accuracy and the κ are respectively, 75.35% and 68.66%. Nevertheless, with a very small training set, the results are still good.

For the feature extraction, NWFE with 99% of the cumulative variance provides the best results: The obtained overall accuracy is 85.42% and the κ is 80.87%, which is closed to the best.
results obtained with the full training set (OA=97.87% and \( \kappa = 84.40\% \), see Table V). The \( |Z| \) between the best results with limited training and the best results with full training set is equal to 13.65.

Furthermore, the accuracies are better than those obtained with the full training set with the spectral or morphological information alone. It is also important to note that NWFE outperforms better DBFE without any statistical enhancement.

Considering the processing time, with only 20 samples for each class, the training as well as the classification of the entire data set are done in 1 or 2 seconds.

VII. Conclusion
Classification of hyperspectral data with a fine spatial resolution has been investigated. The contribution of this work is a methodology to include both spatial and spectral information in the classification process by a data fusion scheme. Experimental results on two ROSIS data sets showed excellent accuracies and improvements compared to those obtained with pixel-based classifiers and the EMP-based classifier.

The use of feature extraction was motivated by the fact that the full stacked vector contains a lot of redundancy, because there is a redundancy in the hyperspectral data [3] as well as in the EMP [11], which was confirmed by the experiments. On the other hand, SVM are known to be robust to dimensionality. Therefore, the use of feature reduction for SVM could be disputable. However, in the experiments lower dimensional data decreased the processing time, which can be crucial for some applications, and more important it has been showed that SVM can suffer from the dimensionality when many features are irrelevant [39]. By construction, the stacked vector may contain many copies of the same information and a feature extraction step may finally be needed to ensure correct classification on every data set, which is confirmed by the experiments (Usefulness of features reduction for the classification of remote sensing data with SVM was also assessed in [40]).

It is clear that feature extraction helps for the classification of hyperspectral data but it is not clear which one of the feature extraction methods should be used for the fusion of morphological and spectral features. From a theoretical point of view, the NWFE was derived because of some intrinsic problems with the DBFE [3], i.e., "DBFE can involve lengthy calculations and more significantly it does not perform as well for small numbers of training samples". Hence, the NWFE might be more preferable, especially when a small training set is available. The experiments performed with a limited training set confirmed that.

In conclusion, the proposed fusion method succeed in taking advantage of the spatial and the spectral information simultaneously. It outperformed previous results [2], [10]. Our current research is oriented to the definition of additional spatial features, such as textural characteristics [41], to be include in the feature vectors.

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REFERENCES

TABLE XV

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<tr>
<th>Z</th>
<th>EMP/Spectral</th>
<th>EMP/Spec. EMP</th>
<th>EMP/DBFE 95%</th>
<th>EMP/NWFE 99%</th>
<th>NWFE 99%/DBFE 95%</th>
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<tr>
<td>2</td>
<td>17.5</td>
<td>2.67</td>
<td>-25.4</td>
<td>-51.14</td>
<td>21.32</td>
</tr>
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</table>

Jón Atli Benediktsson (S’84-M’90-SM’99-F’04) received the Cand. Sci. degree in electrical engineering from the University of Iceland, Reykjavík, in 1984, and the M.S.E.E. and Ph.D. degrees from Purdue University, West Lafayette, IN, in 1987 and 1990, respectively. He is currently Director of Academic Development and Innovation and Professor of Electrical and Computer Engineering at the University of Iceland. He has held visiting positions at the Department of Information and Communication Technology, University of Trento, Trento, Italy (2002-present), School of Computing and Information Systems, Kingston University, Kingston Upon Thames, U.K. (1999-2004), the Joint Research Centre of the European Commission, Ispra, Italy (1998), Denmark Technical University (DTU), Lyngby (1998), and the School of Electrical and Computer Engineering, Purdue University (1995). He was a Fellow at the Australian Defence Force Academy, Canberra, A.C.T., Australia, in August 1997. From 1999 to 2004, he was a Chairman of the energy company Metan Ltd. His research interests are in remote sensing, pattern recognition, neural networks, image processing, and signal processing, and he has published extensively in those fields. Dr. Benediktsson is Editor of the IEEE TRANSACTIONS ON GEOSCIENCE AND REMOTE SENSING (TGARS) and Associate Editor of the IEEE GEOSCIENCE AND REMOTE SENSING LETTERS. He was Associate Editor of TGARS from 1999 to 2002. He co-edited (with Prof. D. A. Landgrebe) a Special Issue on Data Fusion of TGARS (May 1999). In 2002, he was appointed Vice President of Technical Activities in the Administrative Committee of the IEEE Geoscience and Remote Sensing Society (GRSS) and (with P. Gamba and G. G. Wilkinson) a Special Issue on Urban Remote Sensing from Satellite (October 2003). From 1996 to 1999, he was the Chairman of GRSS Technical Committee on Data Fusion and was elected to the Administrative Committee of the GRSS for the term 2000 to 2002, and in 2002, he was appointed Vice President of Technical Activities of GRSS. He was the founding Chairman of the IEEE Iceland Section and served as its Chairman from 2000 to 2003. Currently, he is the Chairman of the University of Iceland’s Quality Assurance Committee (2006- ). He was the Chairman of the University of Iceland’s Science and Research Committee (1999-2005), a member of Iceland’s Science and Technology Council (2003-2006), and a member of the Nordic Research Policy Council (2004). He was a member of a NATO Advisory Panel of the Physical and Engineering Science and Technology SubProgramme (2002-2003). Dr. Benediktsson is a Fellow of the IEEE. He received the Stevan J. Kristof Award from Purdue University in 1991 as outstanding graduate student in remote sensing. In 1997, he was the recipient of the Icelandic Research Council’s Outstanding Young Researcher Award, in 2000, he was granted the IIEEE Third Millennium Medal, in 2004, he was a co-recipient of the University of Iceland’s Technology Innovation Award, in 2006 he received the yearly research award from the Engineering Research Institute of the University of Iceland, and in 2007, he received the Outstanding Service Award from the IEEE Geoscience and Remote Sensing Society. He is a member of Societas Scinetiarum Islandica and Tau Beta Pi.

Jocelyn Chanussot (SM’04) received the M.Sc. degree in electrical engineering from the Grenoble Institute of Technology (Grenoble INP), France, in 1995, and the Ph.D. degree from the Savoie University, Annecy, France, in 1998. In 1999, he was with the Geography Imagery Perception laboratory (GIP) for the Delegation Generale de l’Armement (DGA-French National Defense Department). Since 1999, he has been with Grenoble INP as an Assistant Professor from 1999 to 2005), an Associate Professor from 2005 to 2007, and currently a Professor of signal and image processing. He is conducting his research at the Grenoble Images Speech Signals and Automatics Lab (GIPSA-Lab, Grenoble, France). His research interests include image analysis, multicomponent image processing, nonlinear filtering and data fusion in remote sensing. Prof. Chanussot is an Associate Editor for the IEEE TRANSACTIONS ON GEOSCIENCE AND REMOTE SENSING and for Pattern Recognition. He is the Co-Chair of the GRS Data fusion Technical Committee and a Member of the Machine Learning for Signal Processing Technical Committee of the IEEE Signal Processing Society. He is the founding president of IEEE Geoscience and Remote Sensing French chapter.

Johannes R. Sveinsson (S’86-M’90-SM’02) received the B.S. degree from the University of Iceland, Reykjavík, and the M.S. (Eng.) and Ph.D. degrees from Queen’s University, Kingston, ON, Canada, all in electrical engineering. He is currently a Professor in the Department of Electrical and Computer Engineering, University of Iceland. From 1981 to 1982, he was with the Laboratory of Information Technology and Signal Processing, University of Iceland. He was a Visiting Research Student with the Imperial College of Science and Technology, London, U.K. from 1985 to 1986. At Queen’s University, he held teaching and research assistantships and received Queen’s Graduate Awards. From November 1991 to 1998, he was with the Engineering Research Institute, University of Iceland, as a Senior Member of the research staff and a Lecturer in the Department of Electrical Engineering, University of Iceland. His current research interests are in systems and signal theory.