Probabilistic lifetime assessment of RC structures under coupled corrosion-fatigue deterioration processes

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Abstract

Structural deterioration is becoming a major problem when considering long term performance of infrastructures. The existence of a corrosive environment, cyclic loading and concrete cracking cause structural strength degradation. The interaction of these conditions can only be taken into account when modeling the coupled action. In this paper, a new model to assess lifetime of RC structures subject to corrosion-fatigue deterioration processes, is proposed. Separately, corrosion leads to cross section reduction while fatigue induces the nucleation and the propagation of cracks in steel bars. When considered together, pitting corrosion nucleates the crack while environmental factors affect the kinematics of crack propagation. The model is applied to the reliability analysis of bridge girders located in different chloride-contaminated environments. Overall results show that the coupled effect of corrosion-fatigue on RC structures affects strongly its performance leading to large reduction in the expected lifetime.

Key words: corrosion-fatigue, chloride ingress, cyclic load, lifetime assessment, reinforced concrete, reliability.

1. Introduction

Long-term performance of infrastructure systems is dominated by structural deterioration. Structural deterioration is loss of capacity due to physical, chemical, mechanical or biological actions. Since a corrosive environment and cyclic loading are two of the main causes of reinforced concrete (RC) deterioration, a significant amount of research has been devoted to these two specific damage mechanisms [1] [2] [3]. Corrosion is the most common form of steel deterioration and consists in material disintegration as a result of chemical or electrochemical action. Most metals corrode on contact with water (or moisture in the air), acids, bases, salts, and other solid and liquid chemicals. Metals will also corrode when exposed to gaseous materials like acid vapors, formaldehyde gas, ammonia gas, and sulfur containing gases [3]. Depending upon the case, corrosion can be concentrated locally to form a pit, or it can extend across a wide area to produce general wastage. On the other hand, fatigue is the damage of a material resulting from repeatedly stress applications (e.g. cyclic loading). Fatigue is conditioned by factors such as high temperature, i.e. creep-fatigue, and the presence of aggressive environments, i.e. corrosion-fatigue [1] [2].

The damage to RC structures resulting from the corrosion of reinforcing is exhibited in the form of steel cross section reduction, loss of bond between concrete and steel, cracking, and spalling of concrete cover [4] [5]. The corrosion of steel reinforcement has been usually associated to chloride ingress and carbonation [4]; however, recent studies have shown that other deterioration processes like biodeterioration might contribute significantly to this process [6]. In RC structures, the coupled effect of corrosion and fatigue has not been studied in as much detail as their separated effects. Coupled corrosion-fatigue deterioration results from the combined action of cycling stresses in corrosive environments. Localized corrosion leading to pitting may

provide sites for fatigue crack initiation. Corrosive agents (e.g., seawater) increase the fatigue crack growth rate [7], whereas the morphology of metals/alloys at micro-level governs the pit nucleation sites [8]. Under these conditions, the formation and growth of pits is influenced by both a corrosive environment and cyclic loads and become a coupled damage mechanism.

Examples of structures that experience this type of damage are bridges, chimneys, towers and offshore structures situated close to the sea or exposed to the application of de-icing salts. The effects of gradually accumulating corrosion on the low cycle fatigue of reinforcing steel have been recorded experimentally by Apostolopoulos et al. [9] showing that corrosion implies an appreciable reduction in the ductility, the strength and the number of cycles to failure.

Large research efforts have been made to predict the corrosion-fatigue life of structural members constituted by aluminum, titanium and steel alloys. Goswami and Hoepfner [10] proposed a seven-stage conceptual model in which the electrochemical effects in pit formation and the role of pitting in fatigue crack nucleation were considered. Other research studies focused on particular stages of the process. For instance, a transition model from pit to crack based in two criteria: stress intensity factor and the competition between pit growth and crack growth, was proposed by Kondo [11], and further discussed by Chen et al. [12]. In order to take into consideration the entire progressive damage process and the uncertainties in each stage, Shi and Mahadevan [13] proposed a mechanics-based probabilistic model for pitting corrosion fatigue life prediction of aluminum alloys.

The objective of this paper is to develop a probabilistic lifetime prediction model for RC structures under the coupled effect of corrosion and fatigue. The model assesses the total corrosion-fatigue life as the sum of three critical stages: (1) corrosion initiation and pit nucleation; (2) pit-to-crack transition, and (3) crack growth. The first considers the time from the end of construction until the generation of a pit. The length of this stage is estimated by considering Frick's diffusion law and electrochemical principles. The second stage includes the pit growth until crack nucleation. In this stage the interaction between electrochemical and mechanical processes is taken into account. The latter stage covers the time of crack growth until it reaches a critical crack size. The critical crack size is defined as the crack size at which the RC member reaches a limit state of resistance.

The model proposed is exposed in section 2. Section 3 presents a discussion about time-dependent reliability analysis. Finally, an application to bridge girders is exposed in section 4.

2. Coupled corrosion-fatigue model

The corrosion-fatigue damage process in RC structures is conceptually depicted in Figure 1. The process takes into account the interaction between: (1) chloride ingress, (2) RC cracking and (3) cyclic load. Chloride ingress leads to steel depassivation, and takes part in the kinematics of the corrosion process. Besides, corrosion as a result of chloride ingress induces a high localized corrosion (i.e., pitting corrosion) leading to reinforcing steel crack nucleation [3]. Concrete cracking generated by the accumulation of corrosion products in the steel/concrete interface plays an important role in the steel corrosion rate. Its importance depends of both the width of the crack in the concrete and the aggressiveness of the environment. On the other hand, cyclic loading is important in the transition from pit to crack and crack growth.

The corrosion-fatigue deterioration process is basically divided in two stages: (1) pit formation and growth; and (2) fatigue crack growth. Pit formation and growth involves electrochemical processes depending predominantly on environmental factors. Crack growth is estimated in terms of Linear Elastic Fracture Mechanics (LEFM) and depends mostly upon both cyclic loads and material properties. Goswami and Hoepfner [10] proposed to separate conceptually the corrosion-fatigue life into the following stages: (1) electrochemical stage and pit nucleation, (2) pit growth, (3) competitive mechanisms between pit growth and fatigue crack nucleation, (4) chemically, "short" crack growth, (5) transition from "short crack" to "long crack", (6) long crack growth, and (7) corrosion fatigue crack growth until instability. However, assuming initial immunity of RC structures and the fact that some of these stages proposed by Goswami and Hoepfner are transitional stages, the total corrosion-fatigue life, τ_T , will be divided in the following stages (Figure 1):

- (i) corrosion initiation and pit nucleation, τ_{cp} ,
- (ii) pit-to-crack transition, τ_{pt} , and
- (iii) crack growth, τ_{cg} .

2.1. Corrosion initiation and pit nucleation

This stage is divided into two sub-stages:

- (i) time to corrosion initiation, τ_{ini} , and
- (ii) time to pit nucleation, τ_{pn} .

The first describes the time from the end of construction until the depassivation of the corrosion protective layer of reinforcing steel, and subsequently, corrosion initiation. For RC structures, the length of this stage depends mainly upon the concrete characteristics and the thickness of the cover. It is calculated by using the Frick's second law under the assumption that concrete is an homogenous and isotropic material [14]:

$$\frac{\partial C}{\partial \tau} = D_{cl} \frac{\partial^2 C}{\partial x^2} \quad (1)$$

where C is the chloride ion concentration, D_{cl} is the chloride diffusion coefficient in concrete, τ is the time and x is depth in the diffusion direction. If the following initial conditions are defined: (1) at time $\tau = 0$, the chloride concentration is zero; (2) the chloride concentration on the surface is constant. The solution to eq. 1 leads to the chloride ion concentration $C(x, \tau)$ at depth x after time τ :

$$C(x, \tau) = C_s \left[1 - \operatorname{erf} \left(\frac{x}{2\sqrt{D_{cl}\tau}} \right) \right] \quad (2)$$

where C_s is the surface chloride concentration and $\operatorname{erf}()$ is the error function. The threshold concentration C_{th} is defined as the chloride concentration for which the rust passive layer of steel is destroyed and the corrosion begins. When $C(x, \tau)$ is equal to C_{th} and the depth x is equal to the bar cover c , i.e. $x = c$, the time to corrosion initiation, τ_{ini} , becomes:

$$\tau_{ini} = \frac{c^2}{4D_{cl}} \left[\operatorname{erf}^{-1} \left(1 - \frac{C_{th}}{C_s} \right) \right]^{-2} \quad (3)$$

Pit nucleation is the result of an electrochemical processes induced by corrosion. Computing time to pit nucleation, τ_{pn} , is a non-trivial task because its value depends on several environmental, material and loading factors whose interaction is not well understood yet. The pit depth at time τ , $p(\tau)$ (Figure 2b), can be calculated as [3]:

$$p(\tau) = 0.0116\alpha \int i_{corr}(\tau) d\tau \quad (4)$$

where $p(\tau)$ is given in mm, α is the ratio between pitting and uniform corrosion depths, and $i_{corr}(\tau)$ is the time-variant corrosion rate which is given in $\mu\text{A}/\text{cm}^2$. Time to pit nucleation is estimated by defining a threshold, p_0 , for the pit depth, $p(\tau)$. For example, according to Harlow and Wei [15] this value is $p(\tau_{pn}) = p_0 = 1.98 \times 10^{-6} \text{m}$. During a brief time period after steel depassivation, i.e. $\tau_{ini} + 1\text{yr} \geq \tau > \tau_{ini}$, it is reasonable to assume that $i_{corr}(\tau)$ remains constant (i.e. $i_{corr}(\tau) = i_{ini}$) and is equal to [16]:

$$i_{ini} = \frac{37.8(1 - wc)^{-1.64}}{c} \quad (5)$$

where wc is the water-cement ratio and c is given in mm. Consequently, by making $p(\tau_{pn}) = p_0$ in eq. 4, substituting eq. 5 in eq. 4 and by integrating, the time to pit nucleation, τ_{pn} , can be written:

$$\tau_{pn} = \frac{2.281cp_0}{\alpha} (1 - wc)^{1.64} \quad (6)$$

Equation 6 gives a simple relationship to estimate τ_{pn} based on electrochemical principles. Other proposals to obtain τ_{pn} can be found in the literature [13], however, this discussion is beyond the scope of this paper.

2.2. Pit-to-crack transition

The time of transition from pit to crack, τ_{pt} , is defined as the time at which the maximum pit depth reaches a critical value leading to crack nucleation. Crack nucleation depends on the competition between the processes of pit and crack growth. To estimate this transition period, two criteria can be taken into account [11] [12]:

- (i) *Rate competition criterion*: the transition takes part when the crack growth rate, $da/d\tau$, exceeds the pit growth rate, $dp/d\tau$, as illustrated in Figure 2a.

- (ii) *Fatigue threshold criterion*: the transition occurs when the stress intensity factor of the equivalent surface crack growth for the pit, ΔK_{eq} , reaches the threshold stress intensity factor for the fatigue crack growth, ΔK_{tr} .

In this study, the fatigue threshold criterion was not taken into consideration because experimental observations indicate that this criterion is not appropriate to estimate fatigue crack nucleation at low loading frequencies [12]. Therefore, the rate competition criterion where pit growth rate is described by electrochemical mechanisms and fatigue crack growth rate is estimated in terms of LEFM will be discussed in the following sections. This discussion will focus on:

- (i) Pit growth rate
- (ii) Fatigue crack growth rate
- (iii) Computation of pit-to-crack transition

2.2.1. Pit growth rate

After pit nucleation and as a result of a localized galvanic corrosion, pit growth can be estimated in terms of a change in the volumetric rate by using the Faraday's law [11] [15]:

$$\frac{dV}{d\tau} = \frac{Mi_{corr}}{nF\rho} \quad (7)$$

where M is the molecular weight of iron, (i.e. $M = 55.85$ g/mol), i_{corr} is the corrosion rate, n is the valence of iron, (i.e. $n = 2$), F is the Faraday's constant, (i.e. $F = 96500$ C/mol), and ρ is the density of iron, (i.e. $\rho = 8000$ kg/m³). Corrosion rate is the effective galvanic current between the particles and the steel matrix. The relationship between corrosion rate and temperature is taken into account by using the Arrhenius equation:

$$i_{corr} = i_{p0} \exp\left(\frac{-\Delta H}{RT}\right) \quad (8)$$

where i_{p0} is the pitting current coefficient, ΔH is the activation enthalpy, R is the universal gas constant ($R = 8.314$ /mol K), and T is the absolute temperature. It is clear, from eq. 8, that the corrosion rate increases when temperature is raised. Nevertheless, given the complexity of the corrosion process in RC, the relationship between i_{corr} and T is not simple [17]. For instance, it has been found that the corrosion kinetics of different RC structures under conditions of constant temperature can vary widely [17]. This variability results from the interaction between temperature and other factors such as conductivity and relative humidity. In addition, corrosion rate in RC is a function of environmental aggressiveness. Thus, the corrosion rate becomes a time-variant function depending mostly upon: concrete pH, oxygen, water and chlorides availability. In this context, Bastidas-Arteaga et al. [18] proposed a time-variant corrosion rate function, $i_{corr}(\tau)$, which takes into account environmental hostility. This function is based on a fuzzy inference system under the following assumptions:

- (i) during the period corresponding to the initial corrosion age, the initial corrosion rate function, $i_{ini}(\tau)$ is estimated as [16]:

$$i_{ini}(\tau) = \begin{cases} \frac{37.8(1 - wc)^{-1.64}}{c} & \text{if } \tau_{ini} + 1\text{yr} \geq \tau > \tau_{ini} \\ \frac{32.13(1 - wc)^{-1.64}}{c}(\tau - \tau_{ini})^{-0.3} & \text{if } \tau > \tau_{ini} + 1\text{yr} \end{cases}; \quad (9)$$

- (ii) during the period corresponding to the maximum corrosion age, i_{corr} leads to a maximum corrosion rate, i_{max} . The value of i_{max} depends principally on the availability of water, oxygen and salts at the corrosion cell as a result of severe concrete cracking.

If the membership function for the initial corrosion age is $\mu_{ini}(\tau)$ and for the maximum corrosion age is $\mu_{max}(\tau)$, the time-variant corrosion rate considering concrete cracking and environmental aggressiveness takes the form:

$$i_{corr}(\tau) = \frac{\mu_{ini}(\tau)i_{ini}(\tau) + \mu_{max}(\tau)i_{max}}{\mu_{ini}(\tau) + \mu_{max}(\tau)} \quad (10)$$

Figure 2b depicts the time-variant corrosion rate functions. It is observed that the initial corrosion rate function (i.e. dotted line) decreases after $\tau_{ini} + 1$ yr. This is caused by the formation of rust products on the steel surface that reduce the diffusion of iron ions away from the steel surface. Moreover, the accumulation of corrosion products reduces the area ratio between the anode and the cathode [16]. The time-variant corrosion

rate (i.e. continuous line) follows the initial corrosion rate function until the time for several concrete cracking. After the time of severe cracking, τ_{sc} , there is a transition towards the maximum corrosion rate. The advantage of this fuzzy approach is that the corrosion rate can be estimated based on local conditions, experts' knowledge and empirical models or observations. For example, for a given site, an expert can define the shape of the membership functions or the value of the maximum corrosion rate taking into account its knowledge about concrete quality, material properties, environmental hostility, RC behavior in similar conditions etc. Finally, it is important to clarify that the function can be permanently updated based on field measurements and experimental data.

Pit formation and shape are random phenomena which depend mainly on material properties, fabrication processes and electrochemical factors [10]. Currently this dependence is not well understood. Some authors assume that pit growth follows the shape of a hemisphere or a prolate spheroid [15] [11]. For simplicity, a spherical shape of the pit is assumed herein (Figure 2b) and its radius, $p(\tau)$, can be estimated from eq. 4. Then, the volumetric rate of pit growth (eq. 7) can be directly rewritten in terms of pit growth rate by deriving eq. 4 with respect to time:

$$\frac{dp}{d\tau} = 0.0116\alpha i_{corr}(\tau) \quad (11)$$

2.2.2. Fatigue crack growth rate

The fatigue crack growth rate is estimated by means of the Paris-Erdogan law:

$$\frac{da}{dN} = C_p(\Delta K)^m \quad (12)$$

where a is the crack size, N is the number of cycles, ΔK is the alternating stress intensity factor, and C_p and m are material constants. It is known that there is a strong correlation between C_p and m , and their values are highly depending on the environmental aggressiveness. For RC structures, Salah el Din and Lovegrove [19] reported experimental values for C_p and m corresponding to medium and long crack growth stages, leading to:

$$\frac{da}{dN} = \begin{cases} 3.83 \times 10^{-29}(\Delta K)^{20.863} & \text{if } \Delta K \leq 9 \text{ MPa}\sqrt{\text{m}} \\ 3.16 \times 10^{-12}(\Delta K)^{3.143} & \text{otherwise} \end{cases} \quad (13)$$

and the stress intensity factor, ΔK , is computed as:

$$\Delta K(a) = \Delta\sigma Y(a/d_0)\sqrt{\pi a} \quad (14)$$

where $\Delta\sigma$ is the stress range, i.e. $\Delta\sigma = \sigma_{max} - \sigma_{min}$, d_0 is the initial diameter of the bar and $Y(a/d_0)$ is a dimensionless geometry notched specimen function, which can be approximated by [20]:

$$Y(a/d_0) = \frac{1.121 - 3.08(a/d_0) + 7.344(a/d_0)^2 - 10.244(a/d_0)^3 + 5.85(a/d_0)^4}{[1 - 2(a/d_0)^2]^{3/2}} \quad (15)$$

The dotted line in Figure 2a follows the shape of the fatigue crack growth rate as function of time, which starts growing after corrosion initiation and pit nucleation.

2.2.3. Computation of pit-to-crack transition

In order to find the time for pit-to-crack transition, τ_{pt} , an equivalent stress intensity factor for the pit, ΔK_{pit} must be estimated. ΔK_{pit} is found by substituting a in eq. 14 by the pit depth $p(\tau)$ (eq. 4):

$$\Delta K_{pit}(\tau) = \Delta\sigma Y(p(\tau)/d_0)\sqrt{\pi p(\tau)} \quad (16)$$

Then, the equivalent crack growth rate becomes:

$$\frac{da}{d\tau} = C_p [\Delta K_{pit}(\tau)]^m f \quad (17)$$

where f is the frequency of the cyclic load. Therefore, the time of pit-to-crack transition is obtained by equating the pit growth rate (eq. 11) with the equivalent crack growth rate (eq. 17), and solving for τ_{pt} in:

$$0.0116\alpha i_{corr}(\tau_{pt}) = C_p(\Delta K_{pit}(\tau_{pt}))^m f \quad (18)$$

In order to calculate τ_{pt} , eq. 18 must be solved numerically. Figure 2a illustrates the graphical solution for τ_{pt} . Pit-to-crack transition is found at the intersection between the continuous and dotted lines.

2.3. Crack growth

Crack growth modeling is concerned with the time from the crack initiation until the crack size has reached a value that defines the failure of the cross section. The size of the initial crack on the steel reinforcement, a_0 , is estimated as the pit depth when the transition from pit to crack is reached, i.e. $a_0 = p(\tau_{pt})$ (eq. 4). The size of the critical crack, a_c , is defined as the crack size at which the RC member reaches a limit state of resistance (e.g. bending capacity). This time is obtained as:

$$\tau_{cg} = \frac{1}{f} \left[\begin{array}{ll} \int_{a_0}^{a_1} \frac{da}{3.83 \times 10^{-29} (\Delta K)^{20.863}} + \int_{a_1}^{a_c} \frac{da}{3.16 \times 10^{-12} (\Delta K)^{3.143}} & \text{if } a_0 < a_1 \\ \int_{a_0}^{a_c} \frac{da}{3.16 \times 10^{-12} (\Delta K)^{3.143}} & \text{otherwise} \end{array} \right] \quad (19)$$

where a_1 is the crack size at which the crack growth rate changes from medium to long crack growth. The transition between medium and long crack growth occurs when the crack size reaches a threshold stress intensity factor -i.e. $\Delta K(a_1) = 9 \text{ MPa}\sqrt{\text{m}}$ [19].

The flowchart that summarizes the entire procedure is presented in Figure 3. The corrosion initiation process depends upon both environmental features and structural configuration. After corrosion initiation, the accumulation of corrosion products in the concrete/steel interface increases the corrosion rate as a result of concrete cracking. By considering the interaction between pit growth and cyclic load, the rate competition criterion is evaluated, and consequently, the time of pit-to-crack transition is assessed. Finally, once crack growth has become the preponderating process, the crack growth induces failure in the cross section.

This model allows the evaluation of the total structural lifetime including: corrosion initiation, pit-to-crack transition and crack propagation. Its robustness lies in the implicit integration of various parameters and processes affecting the RC lifetime, which is very convenient for reliability analysis.

3. Time-dependent reliability analysis

The cumulative distribution function (CDF) of the total corrosion-fatigue life, $F_{\tau_T}(\tau)$, is defined as [21]:

$$F_{\tau_T}(\tau) = \Pr\{\tau_T \leq \tau\} = \int_{\tau_{cp} + \tau_{pt} + \tau_{cg} \leq \tau} f(\mathbf{x}) d\mathbf{x} \quad (20)$$

where $\mathbf{x}$ is the vector of the random variables taken into account and $f(\mathbf{x})$ is the joint probability density function of $\mathbf{x}$. If structural failure is achieved when the crack size reaches a critical value inducing failure of the cross section, the limit state function becomes:

$$g(\mathbf{x}, \tau) = a_c(\mathbf{x}) - a_\tau(\mathbf{x}, \tau) \quad (21)$$

where $a_\tau(\mathbf{x}, \tau)$ is the crack size at time τ and $a_c(\mathbf{x})$ is the critical crack size defined in terms of a limit state of resistance. For example, if the limit state of bending capacity is chosen, since the crack growth induces a reduction in the bending capacity of the structural member, the ultimate bending capacity is reached when a_c is achieved. By taking into account eq. 21, the failure probability, p_f , can be estimated as:

$$p_f = \int_{g(\mathbf{x}, \tau) \leq 0} f(\mathbf{x}) d\mathbf{x} \quad (22)$$

Corrosion-fatigue deterioration process is a time-dependent problem where conditional probabilities are involved. Given the complexity of the problem, closed form solutions for both the CDF of the total corrosion-fatigue lifetime and the failure probability are difficult to obtain. To solve this problem, it is necessary to use Monte-Carlo simulations or analytical approximations such as FORM/SORM.

4. Application to bridge girder

This section presents an illustrative example describing the coupled effect of corrosion-fatigue of a simply supported RC bridge girder subject to cyclic loading. The span of the girder is 10 m with the geometrical characteristics of the cross section and the steel reinforcement shown in Figure 4. The girder has been designed according to EUROCODE 2 [22]. Besides the dead load, a truck wheel load is applied on the girder. The design load, P_k , corresponds to a wheel load located in the center of the span. Table 1 presents the load and the material properties used in the design.

In order to study the implications of the traffic frequency, f , the values of 50, 500, 1000 and 2000 cycles/day are considered. It is important to stress that these frequencies are in the range defined by the EUROCODE 1 for heavy trucks [22]. The effect of environmental hostility on structural reliability, was considered by taken into consideration four levels of aggressiveness (Table 2). Each level is characterized by: (1) a chloride surface concentration, C_s , (2) a maximum expected value of the corrosion rate, i_{max} , and (3) a concrete cover, c . The chloride surface concentration is treated as a random variable for which the mean depends largely on proximity to sea and is computed based on the work of McGee [23]. The maximum expected values of the corrosion rate are based on the EN206 [24]. The cover is defined according to EUROCODE 2 [22]. Table 2 summarizes the characteristics of each level of environmental aggressiveness.

The basic considerations and assumptions of the study are:

- Section confinement is taken into account by using the Kent and Park model [25] and stress-strain relationship for steel follows an elasto-plastic model.
- The elasticity modulus and the tensile strength of concrete are given in terms of the compression strength according to EUROCODE 2 [22].
- A limit crack width of 0.5 mm is used as a threshold for severe concrete cracking, τ_{sc} .
- The water/cement ratio is calculated by using the Bolomey's formula [16].
- A threshold pit depth, p_0 , of 1.98×10^{-6} m is utilized to estimate the time to pit nucleation.
- The deterioration process is continuous, -i.e. there is no maintenance.

The reliability analysis was carried out using Monte-Carlo simulations. The probabilistic models for the variables are given in Table 3. It is worthy to notice the high variability of surface chloride concentration and the chloride diffusion coefficient. In the case of C_s , data reported by McGee [23] were obtained from a field-based study of 1158 bridges in the Australian state of Tasmania. This work appears to be the most comprehensive study for bridges in different environmental conditions. The chloride diffusion coefficient is influenced by many factors such as mix proportions (i.e. water-cement ratio, cement type), curing, compaction and environment (i.e. relative humidity and temperature), among others. Therefore, the high variability of the chloride diffusion coefficient results from the variability of the factors influencing D_{cl} .

The stress range induced by the cyclic load, $\Delta\sigma$, was computed by evaluating the equilibrium conditions between the internal forces and external actions. Tension at bottom reinforcement was defined as critical since this reinforcement is subject to both pitting corrosion and cyclic tension forces. Tension force inducing fatigue varies between T_{min} corresponding to the dead load, and T_{max} resulting from the combined action of to dead and live loads. Based on these considerations, the stress range, $\Delta\sigma$, is computed as:

$$\Delta\sigma(P) = \frac{T_{max}(P) - T_{min}}{A_s} \quad (23)$$

where A_s is the initial cross section area of the reinforcement in tension (i.e. at the bottom).

4.1. Distributions of life stages

4.1.1. Corrosion initiation and pit nucleation

For all levels of aggressiveness, the goodness-of-fit test indicates that both τ_{ini} and τ_{pn} follow a lognormal distribution. The Kolmogorov-Smirnov test (KS-test) with a level of significance of 5% was chosen as selection criterion. As expected, the mean, $\mu_{\tau_{ini}}$, and standard deviation, $\sigma_{\tau_{ini}}$, decrease when the environmental aggressiveness is increased (Figure 5). The high standard deviations result from the high COVs of C_s and D_{cl} (Table 3). The impact of the high variability of C_s and D_{cl} on the PDF of τ_{ini} , is studied by varying their COVs, as shown in Figure 6. For all the considered COVs, $\mu_{\tau_{ini}}$ diminishes when μ_{C_s} increases, and tends to larger values when the COVs of C_s and D_{cl} are augmented. It is also observed that the relationship between μ_{C_s} and $\mu_{\tau_{ini}}$ is not linear and there is a limit (e.g. $\mu_{C_s} = 2 \text{ kg/m}^3$) from which an increase of μ_{C_s} does not produce significant variation of $\mu_{\tau_{ini}}$. In addition, it should be noted that the COV(C_s) has a higher impact on $\mu_{\tau_{ini}}$ than the COV(D_{cl}), particularly, for smaller values of μ_{C_s} (Figure 6b).

For the time to pit nucleation, the mean of τ_{pn} varies between 3.9 – 5.4 days with a COV(τ_{pn}) of 0.25 for all levels of aggressiveness. Therefore, given both the higher magnitude and variability of the time to corrosion initiation, it can be concluded that the time to pit nucleation is negligible.

4.1.2. Pit-to-crack transition

For all levels of aggressiveness and traffic frequencies, the KS-test has shown that the time to transition from pit to crack follows a lognormal distribution. Figure 7 presents the mean and 90% confidence interval

of τ_{pt} , for several traffic frequencies. Values between 8.3 – 51.4 years and 3.2 – 42.8 years are obtained for $\mu_{\tau_{pt}}$ and $\sigma_{\tau_{pt}}$, respectively. In all cases, the mean and confidence interval of τ_{pt} reduce for higher values of traffic frequency. This decrease is expected because the crack growth rate is function of f , and therefore, the intersection between $dp/d\tau$ and $da/d\tau$ occurs early when f is increased. It can also be observed that the mean and the dispersion of τ_{pt} are smaller when environmental aggressiveness is increased. This reduction is explained by fact that high levels of environmental aggressiveness are related with high values of i_{max} . Thus, when the i_{max} leads to high values, the fatigue crack growth rate is increased producing an early crack nucleation.

Since a crack is nucleated at the end of this stage, and the initial crack size is an input data to compute the length of the following stage, Figure 8 depicts the PDFs of a_0 , for both various levels of aggressiveness and several traffic frequencies. In all cases, the goodness-of-fit test shows that a_0 follows a lognormal distribution with μ_{a_0} varying between 1.6– 9 mm and σ_{a_0} of 0.98–5.99 mm. The overall behavior indicates that both the mean and standard deviation tend to higher values when the level of aggressiveness is increased (Figure 8a). This increase is expected because given the preponderance of pitting corrosion on fatigue for higher levels of aggressiveness, the transition occurs for higher initial crack sizes. From the relationship between the mean and standard deviation of a_0 and traffic frequency is possible to notice that both μ_{a_0} and σ_{a_0} decrease when f is increased (Figure 8b). This reduction is due to the fact that the augmentation of the traffic frequency turns the fatigue into the preponderating process, and subsequently, accelerates the pit-to-crack transition.

4.1.3. Crack growth

In all cases considered, the KS-test gives as a result that τ_{cg} follows a lognormal distribution with $\mu_{\tau_{cg}}$ varying between 1.6 – 48.6 years and $\sigma_{\tau_{cg}}$ between 0.31 – 11.14 years. Figure 9 depicts the relationship between the mean and the 90% confidence interval of τ_{cg} and the traffic frequencies. The overall behavior indicates that the mean and dispersion of τ_{cg} diminishes when traffic frequency is increased. This behavior is explained by the fact that failure, i.e. eq. 21, is reached in a shorter period when the frequency tends to higher values (i.e. eq. 19). Furthermore, it can be noted that the mean and dispersion decrease when the level of aggressiveness is increased. This decrement is related to the fact that the size of the initial crack leads to larger values for higher levels of environmental aggressiveness, and therefore, the time to reach failure is lower.

For all traffic frequencies and levels of environmental aggressiveness, the KS-test shows that the size of the critical crack at which the RC member reaches the bending limit state, a_c , follows a Weibull distribution with mean and standard deviation of 11.86 and 0.97 mm, respectively. This non dependency of f and environmental aggressiveness is expected because the bending limit state depends mainly on the effective cross section of the bar.

4.2. Total corrosion-fatigue lifetime

The goodness-of-fit test demonstrates that τ_T follows a lognormal distribution with mean varying between 35.8 – 448.8 years and standard deviation between 49 – 264.7 years. The PDFs of τ_T for various levels of aggressiveness and $f = 500$ cycles/day are depicted in Figure 10a. As expected, μ_{τ_T} and σ_{τ_T} decrease when the level of aggressiveness is increased. Figure 10b presents the mean of τ_T for both, various levels of aggressiveness and traffic frequencies. In general, the critical time, τ_T , occurs earlier when the traffic frequency is augmented.

The relationship between the mean of τ_T and the level of aggressiveness is plotted in Figure 11a. It should be noted that the mean of τ_T without considering fatigue damage (i.e. $f = 0$ cycles/day), is also included. The increase of traffic frequency induces an appreciable reduction of μ_{τ_T} , in particular, in environments with low aggressiveness. By taking as a reference the case without considering fatigue damage, it is possible to estimate the additional lifetime reduction induced by the coupled action of corrosion and fatigue (Figure 11b). The additional reduction of τ_T is high for smaller levels of aggressiveness and bigger traffic frequencies. It can be also noticed that considering the coupled effect of corrosion and fatigue can represent an additional lifetime reduction from 4 – 43%. Considering the effect of corrosion and fatigue does not produce an appreciable additional lifetime reduction for both smaller traffic frequencies and very aggressive environments. However, for traffic frequencies between 500–2000 cycles/day, the coupled effect of corrosion-fatigue induces additional lifetime reductions between 21–43% of τ_T . These results strengthen the importance of including the coupled effect of corrosion and fatigue in the lifetime assessment, in particular, when the structure is placed in

corrosive environments under cyclic loading.

The percentage of participation of each stage in the total corrosion-fatigue life is estimated by the ratios of the mean values (Figure 12). In all cases the participation is mainly due to τ_{cp} , followed by τ_{pt} and τ_{cg} . Whereas for τ_{cp} , the participation decreases when the level of aggressiveness is increased, for τ_{pt} and τ_{cg} , it grows when the level of environmental aggressiveness is augmented. This behavior seems logical because an increment in the level of environmental aggressiveness accelerates the time to corrosion initiation and, subsequently, augments the participation of τ_{pt} and τ_{cg} . By considering the relationship between τ_{cp} and f , the percentage of participation of τ_{cp} increases when the traffic frequency grows. Contrary, for τ_{pt} and τ_{cg} , their percentages decrease when f leads to higher values. This behavior is explained by the fact that larger traffic frequencies reduce the length of the crack nucleation and propagation stages. To conclude, given the larger impact of the time to corrosion initiation and pit nucleation on the total corrosion-fatigue life (i.e. 47 to 92% of τ_T), the maintenance efforts must be directed towards controlling this stage of the process.

The failure probability of the girder, p_f is plotted in Figure 13. It can be observed that the importance of traffic frequency on the failure probability for higher frequencies is minor. For instance, for a time window of 100 years, a moderate level of aggressiveness, without considering fatigue damage, a failure probability of 2.7×10^{-2} is obtained; for the same conditions but different frequencies, failure probability becomes 1.6×10^{-1} , 3.4×10^{-1} , 3.5×10^{-1} and 3.7×10^{-1} for traffic frequencies of 50, 500, 1000 and 2000 cycles/day, respectively. That means, the failure probability is increased by 6, 12.5, 13.1 and 13.5 times for the traffic frequencies of 50, 500, 1000 and 2000 cycles/day, respectively. Whereas this difference varies considerably between 50 and 500 cycles/day, for values between 500 and 2000 cycles/day the increment is not significant. From these results it is possible to affirm that, although the coupled effect of corrosion and fatigue causes a significant increase of p_f , there is a limit after which the increase of f does not produce an appreciable change in p_f .

The influence of reinforcement, A_s , on failure probability for a traffic frequency of 1000 cycles/day is plotted in Figure 14. If p_{ft} represents the target failure probability -i.e. $p_{ft} = 10^{-4}$, and a lifetime of 50 yr is chosen, it can be observed from Figure 14 that the reinforcement resulting from the design does not assures p_{ft} . For the case of low aggressiveness (Figure 14a), increasing A_s can guarantee this condition. Nevertheless, although increasing A_s tends to amplify the time to reach p_{ft} , for the other levels the failure probability is lower than p_{ft} . Therefore, to ensure p_{ft} during the lifetime of the structure, it is necessary to implement other countermeasures such as inspection and maintenance programs for corrosion control.

5. Conclusions

The combined action of corrosion and fatigue influences strongly the structural performance of RC structures and reduces substantially their lifetime. In this paper, a new model that couples these two phenomena is developed and the consequences on the life-cycle of RC structures are assessed. The model takes into account the interaction between the following processes: (1) corrosion induced by chloride ingress, (2) concrete cracking resulting from the accumulation of corrosion products and (3) reinforcement fatigue produced by cyclic loading. The corrosion-fatigue deterioration process is divided within the following three stages: (1) corrosion initiation and pit nucleation, (2) pit-to-crack transition and (3) crack growth. Corrosion initiation is induced by chloride ingress causing the nucleation of a pit. Pit-to-crack transition is achieved when the crack growth produced by cyclic loading becomes the preponderating process. A crack is nucleated at the end of this stage. Finally, crack growth ends when the crack size causes the structural failure.

In order to illustrate the model, a bridge girder located in several chloride-contaminated environments was studied. The time-dependant reliability analysis of the girder included the random nature of the material parameters, the loading scheme and the environmental conditions; the solution was found by using Monte-Carlo simulation. After the analysis, it was noted that the failure probability depends highly on the maximum corrosion rates, surface chloride concentration and traffic frequency.

The results also show that the time to corrosion initiation is highly influenced by the coefficient of variation of the chloride surface concentration. The mean of the time to pit nucleation had a smaller value in comparison to the mean of the time to corrosion initiation; therefore, it is possible to affirm that the length of this sub-stage can be neglected. It was also observed that pit-to-crack transition and crack growth occur early when both the level of aggressiveness and traffic frequency are increased. Regarding external loading, it was remarked that for traffic frequencies between 500 – 2000 cycles/day, the coupled effect of corrosion-fatigue becomes paramount by leading to additional lifetime reductions between 21 – 43%. However, there

is a limit after which the increase of traffic frequency does not produce an appreciable change in the failure probability.

Finally, it was observed that if the target failure probability is set as 10^{-4} , for a structure with a lifetime of 50 years, the structural configuration selected does not reach this value for all environmental conditions considered. Therefore, to guarantee the operation above a predefined target failure probability it is necessary to implement countermeasures such as inspection and maintenance programs for corrosion control.

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Table 1
Design load and material constants.

Variable	Value	Description
P_k	150 kN	Characteristic punctual design load
E_{st}	200000 N/mm ²	Elastic modulus of steel
f'_{c_k}	30 MPa	Characteristic concrete compression strength
f_{y_k}	500 MPa	Characteristic steel strength
γ_c	22 kN/m ³	Specific weight of concrete
γ_p	18 kN/m ³	Specific weight of pavement
ν_c	0.2	Concrete Poisson ratio
ρ_{st}	8000 kg/m ³	Density of steel

Table 2
Description of the studied environments.

Level of aggressiveness	Description	C_s [23] kg/m ³	i_{max} [24] $\mu\text{A}/\text{cm}^2$	c [22] mm
Low	structures located at 2.84 km or more from the coast; sea spray 0.35 carried by the wind is the main source of chlorides.		0.5	40
Moderate	structures located between 0.1 and 2.84 km from the coast 1.15 without direct contact with seawater.		2	45
High	structures situated to 0.1 km or less from the coast, but without direct contact to seawater. RC structures subject to de-icing salts can also be classified in this level.		5	50
Extreme	structures subject to wetting and drying cycles; the processes of surface chloride accumulation are wetting with seawater, evaporation and salt crystallization.	7.35	10	55

Table 3
Probabilistic models of the variables used in the model.

Variable	Distribution	Mean	COV	Source
P	Lognormal	115 kN	0.20	
f'_c	Normal	40 MPa	0.15	[26]
f_y	Normal	600 MPa	0.10	[26]
C_{th}	Uniform	0.90 kg/m ³	0.19	[16]
C_s				
Low	Lognormal	0.35 kg/m ³	0.50	[23]
Moderate	Lognormal	1.15 kg/m ³	0.50	[23]
High	Lognormal	2.95 kg/m ³	0.50	[23]
Extreme	Lognormal	7.35 kg/m ³	0.70	[23]
D_{cl}	Lognormal	63 mm ² /yr	0.75	[27]
ρ_{rust}	Normal	3600 kg/m ³	0.10	[28]
t_{por}	Lognormal	12.5×10 ⁻⁶ m	0.20	[28]
α	Gumbel	5.65	0.22	[29]

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