

Mode III cleavage of a coin-shaped titanium implant in bone: effect of friction and crack propagation

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Abstract

Endosseous cementless implants are widely used in orthopaedic, maxillofacial and oral surgery. However, failures are still observed and remain difficult to anticipate as remodelling phenomena at the bone-implant interface are poorly understood. The assessment of the biomechanical strength of the bone-implant interface may improve the understanding of the osseointegration process.

An experimental approach based on a mode III cleavage mechanical device aims at understanding the behavior of a planar bone-implant interface submitted to torsional loading. To do so, coin-shaped titanium implants were inserted on the tibiae of a New Zealand White rabbit for seven weeks. After sacrifice, mode III cleavage experiments were performed on bone samples. An analytical model was developed to understand the debonding process of the bone-implant interface. The model allowed to assess the values of different parameters related to bone tissue at the vicinity of the implant with the additional assumption that bone adhesion occurs over around 70% of the implant surface, which is confirmed by microscopy images. The approach allows to estimate different quantities related to the bone-implant interface such as: torsional stiffness (around $20.5 \text{ N.m.rad}^{-1}$), shear modulus (around 240 MPa), maximal torsional loading (around 0.056 N.m), mode III fracture energy (around 77.5 N.m^{-1}) and stress intensity factor ($0.27 \text{ MPa.m}^{1/2}$).

This study paves the way for the use of mode III cleavage testing for the investigation of torsional loading strength of the bone-implant interface, which might help for the development and optimization of implant biomaterial, surface treatment and medical treatment investigations.

Keywords

Bone, Implant, Osseointegration, Mode III, Cleavage.

1. Introduction

Titanium implants are commonly used in maxillofacial and orthopaedic surgery (Albrektsson et al., 1988; Buser et al., 1996). However, implant failures are observed (Goodacre et al., 1999) and remain difficult to anticipate because the reasons for the stability of an implant are still partially understood. The parameters determining the biomechanical stability of an endosseous implant are still unclear.

Understanding the physical determinants of the implant biomechanical stability is of primary importance since implant failures necessitate additional hazardous painful and expensive surgical interventions. However, assessing the stability of an implant is difficult due to the complex heterogeneous nature of bone tissue and to the different multiscale factors impacting osseointegration, which may be of biomechanical, biochemical or biological nature. In cementless implants, bone is in direct contact with the biomaterial, which is the main difference with cemented implants (Butz et al., 2006; Miller et al., 2011). The biomechanical properties of the bone-implant interface are *the* critical parameters determining the implant stability. In particular, optimal bone healing leads to i) direct contact between bone and the implant and ii) a relatively important proportion of the implant surface in intimate contact with bone tissue. However, the biomechanical properties of newly formed bone tissue as well as the adhesion between the surfaces of newly formed bone tissue and of the implant remain poorly understood. Debonding of the bone-implant interface may occur when the mechanical solicitations overrule the mechanical strength of the bone-implant system.

Implant retention is a resultant of three major parameters: friction, mechanical interlocking and chemical bonding. Surface roughness at the micro and macro levels as well as the surface chemical properties of the implants have been demonstrated to influence the implant attachment (Ellingsen, 2000; Shalabi et al., 2006; Taborelli et al., 1997) and its mechanical stability (Ogawa et al., 2000; Schwartz et al., 2005).

Relative micromotions of the bone-implant interface during the cicatrisation are determinant for the success of the surgical intervention. Micromotions and microcracks at a relatively low level may lead to biomechanical stimulation of bone remodelling (O'Brien et al., 2002, 2003; Taylor et al., 2003). However, fibrous tissue may be formed at the bone-implant interface when there is excessive interfacial micromotion after surgery during the early phase of cicatrisation (Duyck et al., 2006; Orlik et al., 2003).

A better understanding of osseointegration phenomena necessitates the development of techniques capable of assessing the mechanical strength of the bone-implant interface.

Numerous animal studies on arthroplasty (Butz et al., 2006; Franchi et al., 2007; Gotfredsen et al., 2001; Muller et al., 2006; Seong et al., 2009; Stoppie et al., 2008) have focused on the mechanical stability of implants. Many of these studies are of limited interest to understand the basic biomechanical phenomena responsible for implant stability due to the complex implants geometry. Most studies on bone attachment of titanium implants have focused on the effect of shear forces using push out (Ogiso et al., 1998; Vercaigne et al., 1998), pull out (Berzins et al., 1997; Cook et al., 1995; Giavaresi et al., 2003; Jinno et al., 1998; Soncini et al., 2002) or torque test (Branemark et al., 1997; Branemark et al., 1998; Branemark and Skalak, 1998).

The geometrical properties of implants influence the results of biomechanical test results (Branemark et al., 1998), leading to spatially complex, nonuniform, multiaxial stress fields at the loaded interface (Shirazi-Adl, 1992). To overcome the problem of the influence of the implant shape on the interface strength, specific implant models with a planar bone-implant interface have been conceived to minimize the effects of friction and of mechanical forces and to work under standardized and controlled conditions (Edwards et al., 1997; Nakamura et al., 1985; Skripitz and Aspenberg, 1998, 1999). Interestingly, Ronold et al. (Ronold and Ellingsen, 2002a, b; Ronold et al., 2003a; Ronold et al., 2003b, c) have carried

out nice systematic studies aiming at establishing an animal model to test the functional attachment of implants *in situ*, with minimal influence of interlocking forces. Their model involves the use of flat coin-shaped implants placed onto cortical bone of rabbit tibia. They performed tensile tests by applying a gradual, calibrated force perpendicular to the bone-implant interface. The systematic approach of (Ronold and Ellingsen, 2002b) is promising but remains in some regards limited when it comes to analyse the phenomena involved in the rupture between bone and the implant. From a mechanical point of view, the tensile test performed corresponds to a flat punch configuration, which is an instable situation (Maugis, 2000). Therefore, the measured pull out force strongly depends on the initial boundary conditions at the edge of the coin-shaped implant.

The present study has three objectives. The first aim is to develop an experimental device for mode III mechanical cleavage testing using a coin-shaped implant surgical model (Ronold and Ellingsen, 2002b). The interest of mode III cleavage testing is that it is naturally adapted to the cylindrical geometry of the sample. Moreover, mode III cleavage testing allows a stable fracture configuration. Ti-6Al-4V coin-shaped implants have been maintained on levelled rabbit tibia for seven weeks. After sacrifice, bone specimens were removed and subjected to mode III cleavage tests using a dedicated device. Secondly, the aim is to show that an analytical model inspired from similar experimental configurations (Chateauinois et al., 2010; Johansson et al., 1999) can be carried out in order to describe the experimental results. The last objective is to propose a methodology to derive orders of magnitude of important mechanical properties of newly formed bone tissue from experimental data, such parameters being potentially helpful for the understanding of the complex mechanisms playing a part in such a fracture configuration.

25 2. Experiments

2.1 Implants

Two coin-shaped implants (radius $a = 5 \pm 0.05\text{mm}$, thickness $L = 3 \pm 0.05\text{mm}$) of medical grade titanium alloy (Ti–6Al–4V) were used in this study. The implants surface was blasted with titanium dioxide (TiO₂) particles yielding an average R_a value of $1.9 \mu\text{m}$ ($270 \mu\text{m} \times 360 \mu\text{m}$ surface measured by a standard profilometry method; Zygo, Middlefield, Connecticut, USA). Polytetrafluoroethylene (PTFE) caps were placed around the implants in order to prevent bone growth on the lateral cylindrical boundaries of the implant (see Fig. 1). Prior to surgery, implants were cleaned with 70% ethanol, rinsed with distilled water and sterilized by autoclaving (1 ATM, 120 °C, 15 min).

2.2 Animal

A four month old (weight of 3500g) female New Zealand White rabbit (Charles River, L'Arbresle, France) was used in the study. The animal was housed in a metal hutch in an environment (ambient temperature 19°C and a humidity of 55%) in accordance with the requirements of *the European Guidelines for care and use of laboratory animals*. Artificial lightening and air conditioning systems were used in the animal housing facility. The animal was fed with commercial food and water was provided *ad libitum*.

2.3 Surgical procedure

One implant was placed on each tibia of the rabbit, which was anesthetized with intramuscular injection of 0.5 mg/kg Diazepan (Valium®, Roche, Basel, Switzerland), 0.25 mg/kg metedomidine hydrochloride (Domitor®, Virbac, France) and 100 mg/kg ketamine hydrochloride (Ketalar® 500, Pfizer, France), which were injected intramuscularly. Prior to surgery, the operating site was shaved and disinfected with betadine. One implant was placed on each tibia of the rabbit. A 5 cm longitudinal skin incision in soft tissue layers was made to

expose the proximal anterior aspect of each tibia, thus exposing the underlying periosteum part. A periossteal flap was then elevated, exposing bone implantation site. Using a custom made cutter and under continuous irrigation with isotonic saline solution (Tivoly, Saint Etienne, France), a bone surface of 5.6 mm diameter was levelled in order to: i) insure the stability the coin-shaped implant, ii) maximize the contact between levelled bone and the implant surface as described previously (Ronold and Ellingsen, 2002b). Before the placement of the implant, four holes (0.9 mm diameter) were drilled through the levelled cortical bone surface underlying the coin-shaped implant, in order to allow blood flow towards the bone-implant interface. Then, a custom made drill guide was used to position in a reproducible manner two 1.6 mm diameter osseosynthesis screws (Easy Implant, Chavanod, France) on both sides of the site of the implant. The implant was placed and stabilized with a calibrated, elastomeric, orthodontic elastic string maintained by the aforementioned osteosynthesis screws. After seven weeks of implantation, the animal was euthanized, the tibiae with the inserted implant were removed and cleared from the surrounding tissues. The specimens were conserved in 10% phosphate buffered formalin.

2.4 Mode III cleavage device

Mode III cleavage experiments were carried out with a dedicated self designed device described in Figure 2. The device allows the determination of the variation of the torque imposed to the specimen as a function of the axial rotation of the implant relatively to the superimposed bone tissue. The cleavage device is composed of a rigid frame on which a rotation stage (M062PD, Physik Instruments, Pantin, France) is fixed and allows a continuous rotation of the sample with an angular velocity equal to $0.01 \text{ }^\circ.\text{s}^{-1}$. The rotation stage is driven by appropriate electronics prescribing the variation of the rotational angle as a function of time. Note that the rotation angle is measured using an angular position sensor integrated in

the rotation stage. A static torque meter (CS 1213B, MEAS-France, Les Clayes sous Bois, France) records the variation of the torque as a function of the rotation angle through an electronic sensor interface (9205, Burster, Gernsbach, Germany) (sampling frequency 2.5 kHz). The torque sensor and the rotation stage are synchronized with appropriate electronics and are both controlled via Labview (National Instruments, Austin, Texas USA). The axes of the torque meter and of the rotation stage are aligned with a 50 μm tolerance.

First, the implant is fixed on the device by a chuck screwed to the torque meter, letting the bone sample hanging over a container (50* 25*20 mm) tightened in the clamp (Soncini et al., 2002). Second, the container is filled with a cold hardening resin (Varikleer, Buehler, Düsseldorf, Germany) allowing to rigidly fix the sample relatively to the rotation stage. This procedure aims at minimising the value of the normal force in order to reduce as far as practicable its influence on the experimental results. To do so, cold quick hardening resin is used for the fixation of the samples on the device (Soncini et al., 2002). Third, a thirty minutes waiting period is needed to allow a full solidification of the resin. Fourth, a 10° rotation is imposed by the rotation stage with an angular velocity of $0.01^\circ \cdot \text{s}^{-1}$. The value of 10° was chosen to ensure a complete debonding of the bone-implant interface. A post processing analysis is carried out to extract the data (torque and rotation angle as a function of time).

3. Analytical modelling

In order to understand the experimental results obtained with the cleavage device described above, an analytical model was considered taking into account the coupling of the crack propagation (shear mode fracture) between bone and titanium with friction phenomena, which allows to establish a relationship between the torque and the imposed twist angle. The shear failure of an adhesive contact during the incipient stages of sliding friction is often

referred to as a stiction process (Basire and Fretigny, 1999; Goddenhenrich et al., 1994), which corresponds to a situation where static friction occurs during sliding (Bhushan, 2003). In friction, stiction corresponds to the initial static loading phase which ends with the total rupture of the interface leading to full sliding. Since in sliding friction, the friction coefficient is lower than in static friction, stiction usually results in a force peak (Bowden and Tabor, 2001; Chateauminos et al., 2010), as observed herein. A fundamental question is to determine from the experiments the adhesion energy Γ and the shear modulus μ which rule the dynamics of crack propagation and its interplay with friction. An approach considering fracture mechanics concepts allows to consider that the rate of elastic strain energy is equated to the work done against surface forces, both frictional and adhesive.

Figure 3(a) shows a perspective view of the configuration of interest and Fig. 3(b) shows the expected evolution of the crack front position during the experiment. Let c be the radius of uncracked region corresponding to the value θ of the twist angle. The notation a designates the implant radius. \mathbf{e}_r , \mathbf{e}_θ and \mathbf{e}_z designate respectively the radial, orthoradial and axial directions. Five different steps are represented in Fig. 3(b) and correspond, from (i) to (v), to increasing values of the twist angle θ . Here, the crack front is supposed to be circular and the crack propagation is supposed to be pure mode III (given the geometry of the sample and the imposed rotation (Ehart et al., 1999)), these assumption being discussed in section 5. When the twist angle θ increases, the radius c of the circular adhesive region decreases from a to 0 . For all values of θ , the crack front separates the implant surface into two distinct regions. In Fig. 3, the grey regions correspond to the adhesive regions ($r < c$), while the white regions correspond to the sliding regions ($c < r < a$). In what follows, an elastic behaviour of bone tissue is assumed throughout crack propagation.

The model has been described in details in a recent paper (Chateauminos et al., 2010) and is briefly recalled herein. The reader interested in a detailed description should refer to the

original publication. The main assumption is to consider that the problem is decomposed into a normal indentation configuration on the one hand and a purely tangential problem on the other hand. In the present model, we assume that there is no normal force, so that the problem is only tangential and no cohesive traction is accounted for. This decomposition holds when the contact boundary conditions are given in terms of stress or strain at the surface. The adhesive contact may be more complex as discussed in (Johnson, 1997) but this aspect is not considered herein.

During stiction, orthoradial displacements are prescribed within a disk of radius c (the stick region) while interfacial stresses are prescribed in the sliding region ($a > r > c$). The model described in (Chateauinois et al., 2010) uses a variant of the unified model developed for normal loading (Johnson and Greenwood, 1997; Maugis, 1992) which considers the so-called Dugdale crack model (Haiat and Barthel, 2007; Haiat et al., 2003). In this description, the interfacial forces are supposed to be constant up to a given separation distance between the surfaces. Though rather rough, this model captures the essential features of the adhesive contact, as more realistic interfacial laws do not modify substantially the results obtained (Barthel, 1998). In (Chateauinois et al., 2010), a variant of this model is adapted for the twist experiment. Interfacial orthoradial stresses just beyond the stick region are supposed to be constant up to a radius which corresponds to a given separation distance Δ between points on both surfaces. Such an annulus corresponds to the Dugdale region and is defined by $c < r < c^*$. Adhesion phenomena are accounted for using the adhesion energy Γ between bone and the implant surface. Rupture of the bone-implant interface occurs in the Dugdale annulus and is modelled by a constant orthoradial stress τ_D . The problem in the Dugdale annulus is treated self-consistently. The value of c^* is determined by expressing the condition that the orthoradial displacement reaches the Dugdale limit Δ at the radius c^* and assuming i) that that the interfacial stress in the Dugdale region is much larger than the friction stress ($\tau_D \gg \tau_0$) and

much larger than the shear modulus ($\tau_D \gg \mu$) and ii) a small Dugdale region where $\varepsilon = (c^* - c)/c \ll 1$, similarly as what was done in (Chateauinois et al., 2010).

Beyond radius c^* (for $c^* < r < a$), a prescribed friction law accounts for the “free” sliding region stresses where friction phenomena occur independently of the Dugdale region. This second region ($c^* < r < a$) corresponds to a fully debonded bone-implant interface where friction is modelled by a constant homogeneous orthoradial stress τ_0 . Friction also influences the total torque between bone and the implant starting at the beginning of crack propagation ($c = a$), until the end of the cleavage test. To model such effects, an homogeneous distribution of the orthoradial surface stress $\sigma_{\theta z}$ was considered in the friction area, following:

$$\sigma_{\theta z}(r) = \tau_0, \text{ for } a > r > c. \quad (1)$$

The determination of the value of the parameter τ_0 is obtained by considering the value of the torque for a twist angle equal to infinity (T_∞), which corresponds to a fully debonded interface. Following Eq. (A8) of (Chateauinois et al., 2010), the torsional stress within the contact zone writes:

$$\sigma_{\theta z}(r) = \frac{2}{\pi} \left[\sqrt{\frac{\pi \mu \Gamma}{c}} \frac{r}{\sqrt{c^2 - r^2}} + \tau_0 \sin^{-1} \sqrt{\frac{\frac{a^2}{c^2} - 1}{\frac{a^2}{r^2} - 1}} \right], \text{ for } r < c. \quad (2)$$

In Eq. (2), the first term corresponds to the contribution of the Dugdale annulus, while the second one corresponds to that of the friction region. Γ corresponds to shear cohesion while τ_0 corresponds to friction. The choice of the parameter $\mu \Gamma$ determines the maximum value of the torque as a function of θ . In addition to the expression of the torsional stress at the bone-implant interface, it is necessary to consider an additional equation relating c and the torsional angle θ in order to derive the curve of the torque as a function of θ . This last expression is obtained using a non divergence condition allowing to express the solution of the Dugdale-friction problem and is given by (see Eq. 29 of (Chateauinois et al., 2010)):

$$2\theta - \frac{\tau_0}{\mu} \cosh^{-1} \frac{a}{c} = \sqrt{\frac{\pi \Gamma}{c \mu}} . \quad (3)$$

Coupling Eq. (2) integrated over r and Eq. (3) for different values of c allows to plot the curve of the resulting moment as a function of the imposed torsional angle θ .

The mode III stress intensity factor K_{III} is then given by (Maugis, 1999):

$$K_{III} = 2\sqrt{\mu \Gamma} . \quad (4)$$

Note that in the initial stage, the model leads to a linear elastic deformation field corresponding to a stiffness of bone tissue k given by (Jager, 1995):

$$k = \frac{16}{3} \cdot \mu \cdot a^3 . \quad (5)$$

10 4. Results

Figure 4 shows a comparison between the experimental results obtained for two different cleavage experiments (grey solid lines) and the results of the elastic model described in subsection 3. Figure 4(a) corresponds to the results of the left tibia implant cleavage test while Figure 4(b) represents the results of the cleavage of the right tibia implant. The value of the parameter $\mu \cdot \Gamma$ is chosen equal to 1.02 GPa.N.m⁻¹ (respectively 0.94 GPa.N.m⁻¹) for the configuration of Fig. 4(a) (respectively Fig. 4(b)) following the maximum value of the torque of the experimental results. Table 1 shows the different values of μ and Γ considered in Fig. 4. The value of μ equal to 40 MPa (respectively 20 MPa) for left tibia implant (respectively right tibia implant) gives the best agreement between experimental and analytical results during the crack propagation stage. However, none of the investigated values of μ allows to predict the variation of the torque as a function of the twist angle. Decreasing the value of μ leads to a decrease of the initial slope of the torque – twist angle curve during the initial elastic deformation stage.

In order to understand the discrepancy between the experimental and analytical results, the implants surfaces were observed using standard light microscopy. Figure 5 represents post mortem images of both samples. Figure 5(a) shows the titanium surface of left tibia implant and Fig. 5(b) shows the titanium surface of right tibia implant after the cleavage test. As shown in Fig. 5, scarce fragments of bone tissue remain attached to the titanium surface after the cleavage test. The results show that the interface fracture modes are mixed and may be adhesive (in implant regions where no bone tissue is attached to the implant surface) or cohesive (when some bone tissue remains attached to the implant surface). Moreover, Fig. 5 shows the heterogeneous nature of bone remodelling phenomena around the implant surface, indicating that adhesion phenomena occurred over a limited portion of the implant surface. The adhesion properties are not homogeneous and some regions of the implant exhibit low (or even possibly no) adhesion energy, while some other regions have higher adhesion energy, which may be due to inhomogeneous remodelling phenomena.

5. Discussion

This work constitutes the first study proposing the use of experimental mode III cleavage tests to investigate the biomechanical strength of the interface of cementless implants. This study is also the first one to provide a measurement of the Mode III stress intensity factor and fracture energy of the bone implant interface. The originality of the present study consists in coupling experimental surgery with advanced biomechanical testing and analytical modelling to describe the behaviour of the bone-implant interface during crack propagation. In this study, coin-shaped titanium implants were inserted on the tibiae of a New Zealand White female rabbit. After euthanasia, bone samples were removed and mode III cleavage tests were realised.

The main difference between the pull-out test performed by Ronold et al. and the present experimental configuration is that (Ronold and Ellingsen, 2002b) used an experimental configuration which is highly dependent of the crack initiation conditions while the mode III cleavage configuration allows a measurement of crack propagation in a stable configuration, avoiding the influence of crack initiation (Maugis, 1999).

(Ronold and Ellingsen, 2002b) performed tension tests and measured a mean pull-out load of 20 N (Ronold et al., 2003a) after an equivalent period of healing. In (Branemark et al., 1997), the mechanical strength of the bone – implant interface was investigated both in tensional and torsional loading for real dental implants after the same healing duration. A 95 N pull out load was measured for real implants, while a maximal torque value of 0.045 N.m was obtained. The results found herein for the maximum torque during the mode III cleavage test are in qualitative agreement with the results of (Branemark et al., 1997) for implants with an approximately similar surface in contact with bone tissue. However, the pull out load is five times higher for real implants than for coin-shaped implants. This apparent discrepancy can be explained by the fact that the shape and geometry of commercial implants (particularly the thread) induce higher resistance in tension tests for real implants than for the simple flat circular bone – titanium interface of the coin-shaped implant model.

Although the global shapes of the torque – angle curves are qualitatively similar for the experimental and theoretical results, the model described in section 3 does not provide a good quantitative agreement between experimental and analytical results (see Fig. 4). This discrepancy may be explained by the fact that bone does not adhere to the implant surface over the entire surface area of the sample but rather to a certain percentage p , as shown in Fig. 5. In order to verify the aforementioned hypothesis, an empirical model taking into account energetic considerations is developed in what follows. Such model corresponds to a much simpler approach to understand the basic phenomena at works.

The total work necessary to debond the bone-implant surface W_{debond} is given by:

$$W_{debond} = \int_{\theta=0}^{\theta=10^{\circ}} T(\theta).d\theta. \quad (6)$$

Here, we consider that the bone-implant interface is fully debonded for $\theta=10^{\circ}$ because the torque does not vary as a function of θ . Moreover, the work W_{fric} associated to friction

5 phenomena is assumed to be given by:

$$W_{fric} = \int_{\theta=\theta_{max}}^{\theta=10^{\circ}} T_{\infty} d\theta, \quad (7)$$

where θ_{max} corresponds to the angle at which the torque reaches a maximum. Equation (7) corresponds to a simple way of considering constant friction phenomena starting when the crack initiates. The work of adhesion W_{adhes} is then given by:

$$10 \quad W_{adhes} = W_{debond} - W_{fric}, \quad (7)$$

and is related to the adhesion energy Γ through:

$$W_{adhes} = \Gamma \cdot S \cdot p, \quad (9)$$

where p is the percentage of the implant surface where adhesion occurred and $S=\pi a^2$ is the surface of the bone-implant interface.

15 In order to validate this empirical approach based on energetic considerations, the values of W_{debond} and W_{fric} were calculated for each analytical curves plotted in Fig. 4. Since the analytical model described in section 3 considers that adhesion occurs on the entire implant surface, Eq. 9 was used considering $p=100\%$ in order to calculate the adhesion energy corresponding to each analytical curve in Fig. 4. Table 1 shows the comparison
20 between adhesion energy used as input data in the analytical model and the adhesion energy derived from the application of the energetic approach to the analytical results. A good agreement is observed between the input data and the results of the empirical model, which constitutes a validation of the energetic approach. The empirical energetic model can therefore be applied to the experimental results in order to provide an estimation of the

adhesion energy. To do so, a simple analysis of the images of the debonded surfaces (see Fig. 5) allowed to estimate the value of p for each sample. The results are given in Table 2. W_{debond} and W_{fric} were calculated for the two experimental curves and Eqs. 8-9 were then used in order to provide an estimation of the adhesion energy for each implant. Table 2 shows the results obtained for the values of W_{adhes} , W_{debond} , Γ , W_{fric} and p .

The values of the bone stiffness k were deduced from the initial slope of the torque – angle curve during the linear elasticity stage and the values of the shear modulus μ were deduced from the values of k using Eq. 5. The results are also summarized in Table 2 for each implant.

In the literature, (Berzins et al., 1997) proposed an experimental methodology to estimate the shear modulus of the bone – implant interface *in vitro* using pull-out tests. The same methodology was used by (Muller et al., 2006) with cylindrical implants inserted in New Zealand White rabbits. The results showed mean values of shear modulus of newly formed bone tissue varying between 25 and 40 MPa, which is lower than the results obtained in the present study. However, the present experimental configuration is fundamentally different since we consider a steady state crack propagation configuration. Moreover, the mean value for shear modulus in mature cortical bone is equal to 3.5 GPa (Laugier and Haiat, 2011). This difference may be explained by the degree of mineralisation of mature cortical bone which is higher in mature cortical bone than in newly formed bone tissue (Mathieu et al., 2011) and by the fact that the bone-implant contact is usually comprised between 30 and 70% (Branemark et al., 1997; Marin et al., 2010).

The values of shear modulus of Ti-6Al-4V and of PMMA found in the literature are equal to 42.3 GPa (Pattijn et al., 2007) and 1.1 GPa (Royer and Dieulesaint, 1996) respectively. The shear moduli of Ti-6Al-4V and of PMMA are significantly higher than the values of μ found herein (230-250 MPa), which justifies the assumption of neglecting the

deformation of the implant and of the resin. The torsional rigidity of the device is a critical point in order to assess accurately the bone shear modulus. The critical component in the experimental device is the static torque meter, which has a torsional rigidity equal to 273 N.m.rad⁻¹ (constructor data). This value is about 15 times superior to the highest value of torsional stiffness derived from the analytical model. As a consequence, it is assumed that the torsional rigidity of the device does not significantly affect the accuracy of the measurement.

During functional loading, the bone – implant interface is subjected to multiaxial stresses (traction, compression and torsion loadings) (Butz et al., 2006). Therefore, mode I cleavage testing (Morais et al., 2010) could also be an interesting approach, but would necessitate the development of another implant model with a rectangular flat bone – implant interface in order to have a constant length of the crack front. Mode I fracture characterization has been investigated by (Morais et al., 2010) in cortical bone (no implant present in bone), following an approach described by (de Moura et al., 2008), leading to a value of mode I stress intensity factor K_I in average equal to 6.17 MPa.m^{1/2} for hydrated cortical bone. It would be of interest to compare these results of K_I for cortical bone with mode I cleavage strength of the bone – implant interface.

This study has several limitations. First, only two samples were considered due to the complexity of the surgical procedure, which makes it impossible to consider the scatter of the mechanical properties derived from the experiments. Therefore, special care is needed for the interpretation of the values of such parameters estimated with our method. However, the two experimental curves are qualitatively similar and the results obtained for both samples are of the same order of magnitude.

Secondly, the estimation of the mechanical properties of interest results from necessary multiple approximations and parameters adjustments. Several limitations apply to the analytical model, which assumes an isotropic behaviour of bone tissue while bone tissue is

a highly anisotropic material. Based on the geometrical configuration of testing (Ehart et al., 1999), the model assumes a pure mode III crack propagation, which is supported by Fig. 5 showing that the crack plane is approximately parallel to the implant surface. Moreover, the model assumes a homogeneous distribution of the mechanical properties at the implant surface. However, the remaining normal force may induce mixed mode propagation and Fig. 5 shows that remodelling phenomena at the bone implant interface occur in a non uniform manner (failure involving a material as heterogeneous as bone is likely to be stochastic and heterogeneous), which might complicate crack propagation and lead to mixed modes crack propagation due to the rupture of symmetry (Koester et al., 2011; Zimmermann et al., 2009; Zimmermann et al., 2010).

Third, a simplistic model of friction is considered herein and spatiotemporal variations of friction properties may occur due to wear phenomena (Younesi et al., 2010). The visualisation of the evolution of the crack front during the mechanical cleavage test could help to account for more realistic situations in the model. However, such measurement is not possible at the current stage of development of the experimental device, because of the opacity of bone tissue and titanium. The difference between of the torque obtained with the models compared to the experimental results may be explained by the aforementioned limitations.

Fourth, the normal force arising due to the expansion of the volume of the cold hardening resin during the polymerization process is not measured and may affect the measurements and influence friction phenomena. However, the use of such a resin in order to attach the sample to the device allows to minimize the mechanical stresses applied to the bone-implant interface (Soncini et al., 2002). Moreover, monitoring of the torque imposed to the sample during the resin hardening reports values lower than the sensitivity of the torque sensor ($<10^{-3}$ N.m). The normal force cannot be controlled nor measured in the present

version of the device and future work should include such measurement, which could provide important information about the friction phenomena occurring at the bone – implant interface and allow distinguishing the respective contributions of crack propagation and friction phenomena. However, the effect of the normal force should be the same for the two samples because identical experimental conditions were reproduced for the two mechanical tests (orientation of the sample, shape of the container, volume of injected resin).

6. Conclusion

A mode III cleavage testing configuration allows to investigate the behaviour of the bone-implant interface because the implant is routinely exposed to torsional stresses *in vivo* (hip prosthesis, dental implant). The combination of the developed analytical model together with partial adhesive contact at the bone-implant interface enables to explain the results obtained during the interface debonding. Stiffness, shear modulus, maximal torsional load and mode III stress intensity factors are good candidates for a quantitative assessment of the resistance of the implant to shear stresses. Our approach could provide accurate indicators for the development and the optimization of implant material, surface treatment and medical treatment investigations.

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Figure Captions:

Figure 1: Schematic representation of the surgical model.

5 **Figure 2:** Schematic representation of the mode III cleavage test device.

Figure 3: Description of the crack propagation configuration. (a): perspective view of the configuration of interest, (b): evolution of the crack front position during the experiment. c is the radius of the uncracked region corresponding to the value θ of twist angle. a designates the radius of the implant. \mathbf{e}_r , \mathbf{e}_θ and \mathbf{e}_z designates respectively the radial, orthoradial and axial directions. Five different steps are represented and correspond, from (i) to (v), to increasing values of the twist angle θ . The grey areas correspond to the adhesive regions, while the white ones correspond to the sliding regions.

10
15 **Figure 4:** Total torque measured experimentally (grey solid line) and calculated from the analytical elastic model as a function of the imposed twist angle for different values of shear modulus μ : left tibia implant (a) and right tibia implant (b).

Figure 5: Post mortem images of both samples. (a): left tibia implant and (b): right tibia
20 implant. Both images were obtained by standard light microscopy.

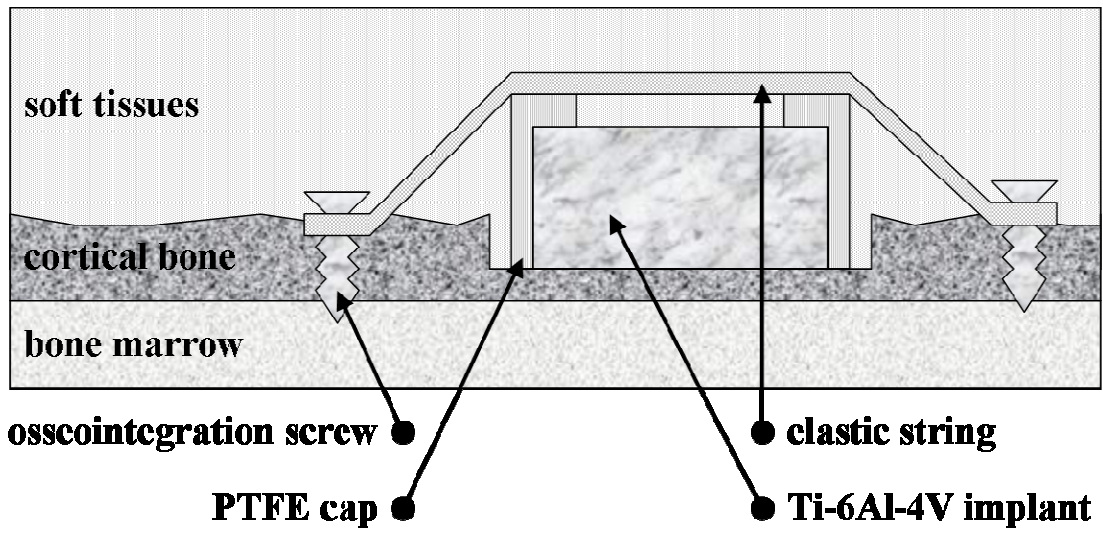


Figure 1

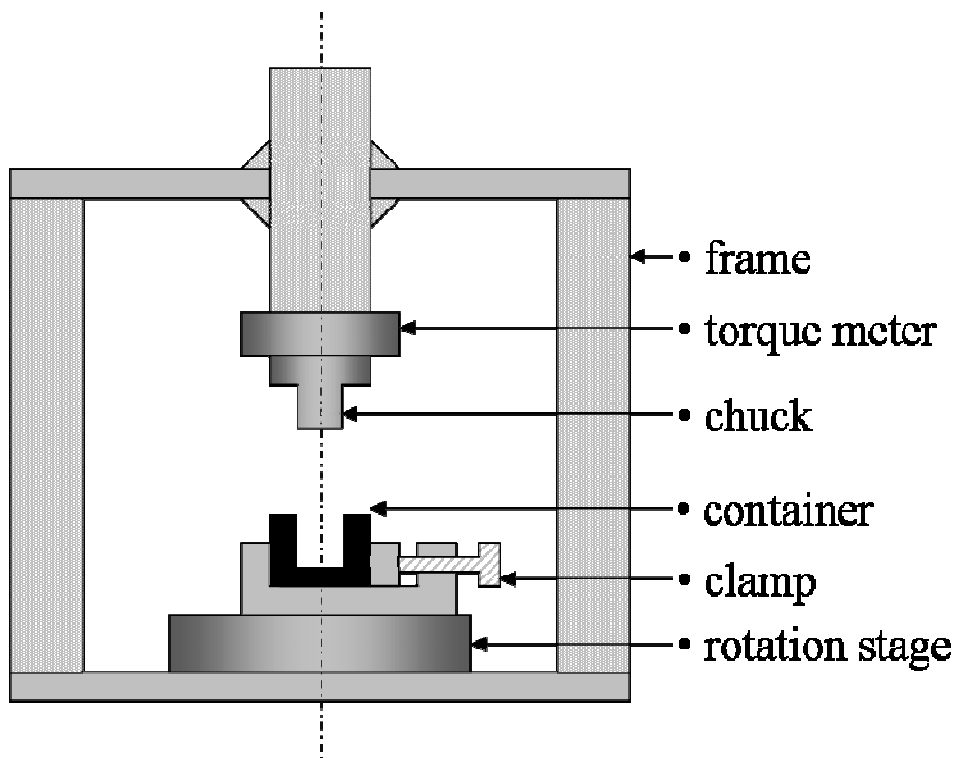


Figure 2

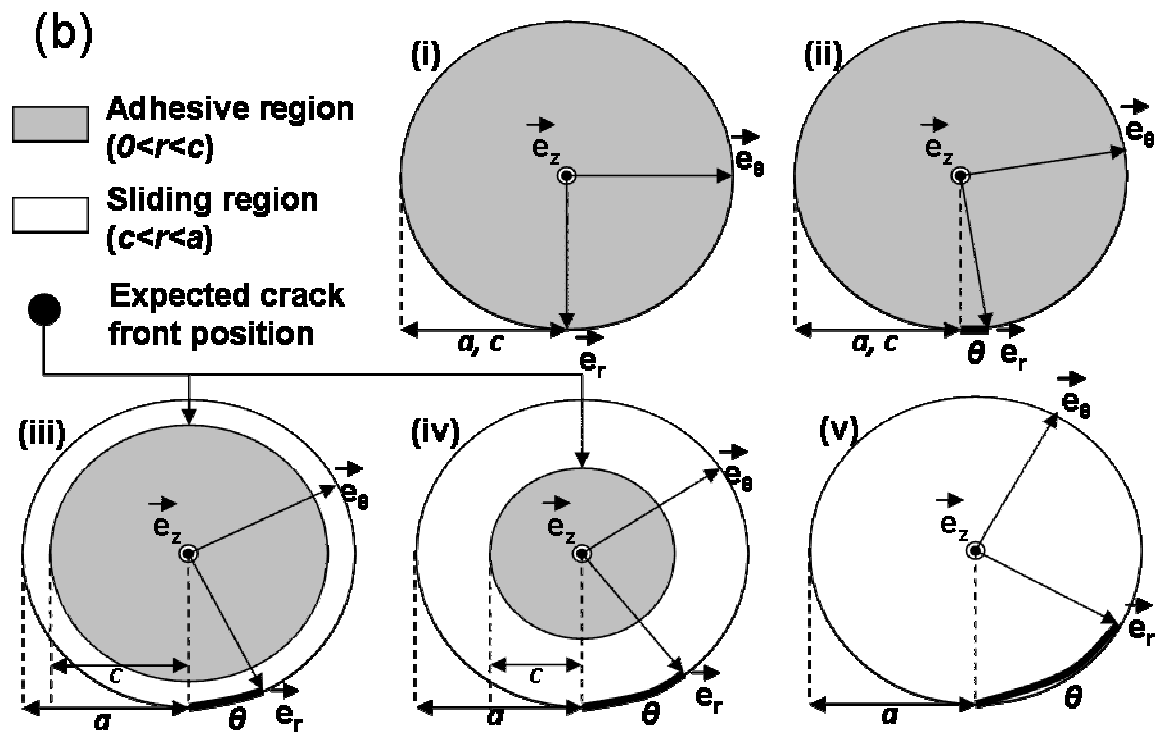
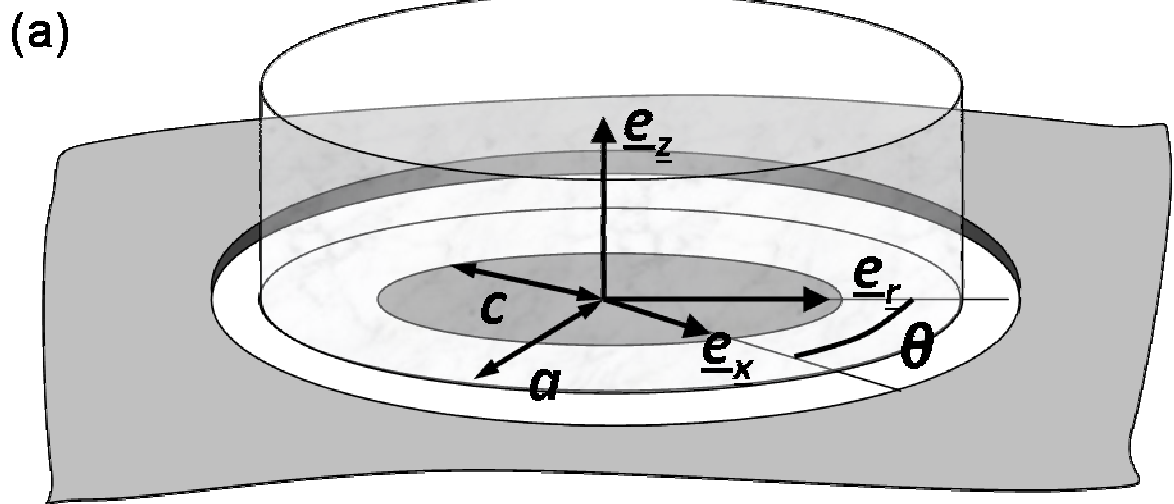


Figure 3

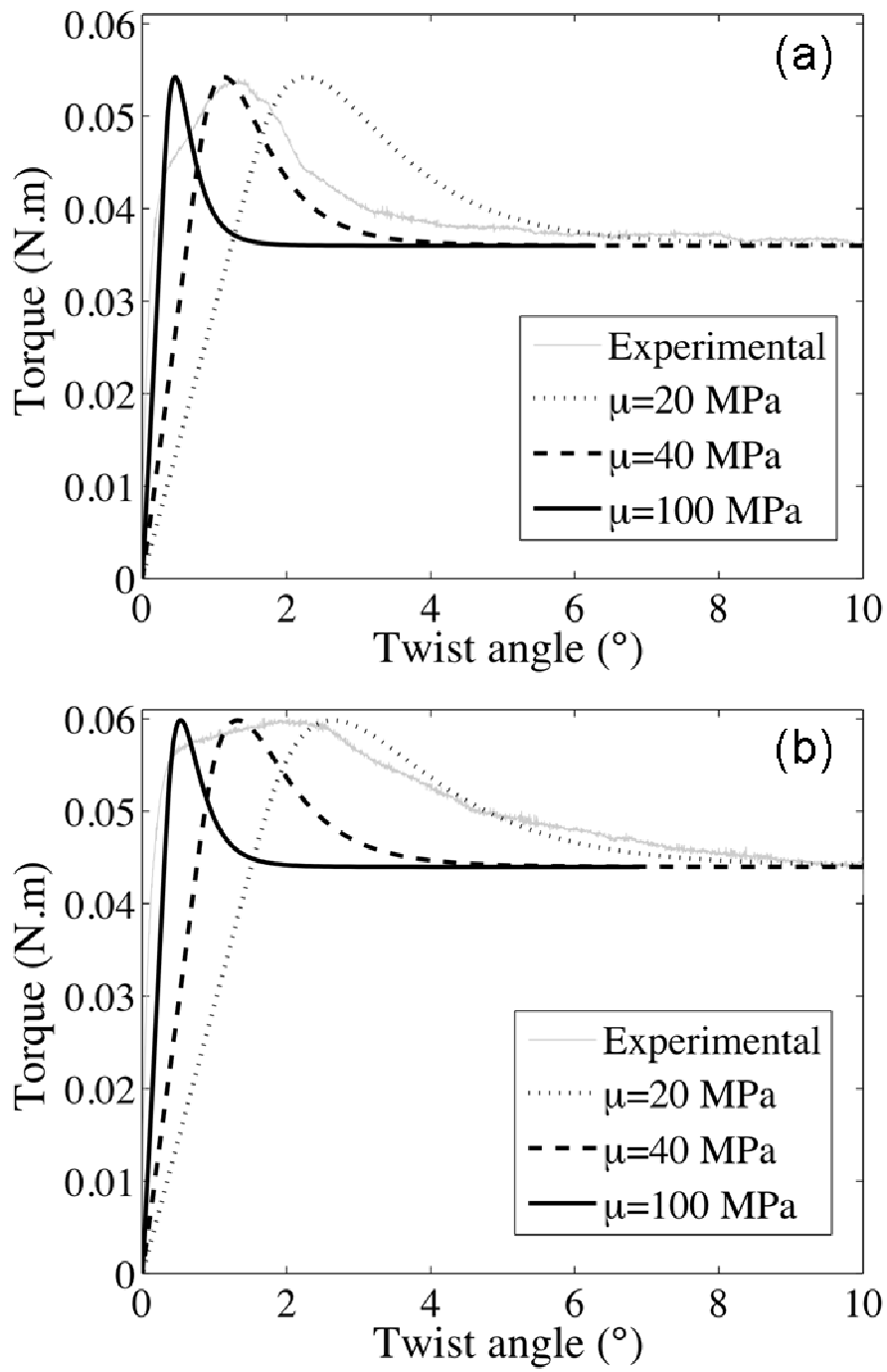


Figure 4

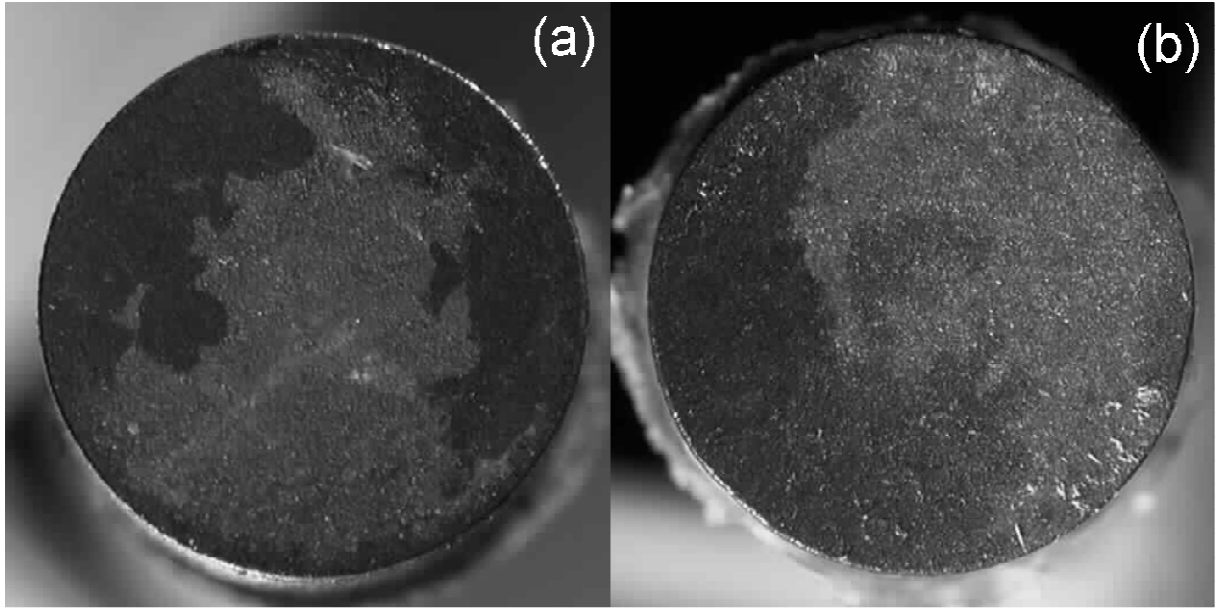


Figure 5