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► **To cite this version:**

Alexis Angelidis, Marie-Paule Cani, Geoff Wyvill, Scott King. Swirling-Sweepers: Constant Volume Modelling. Siggraph Technical Sketches and Applications, 2004, Los Angeles, United States. 10.1145/1186223.1186273 . inria-00537465

HAL Id: inria-00537465

<https://inria.hal.science/inria-00537465>

Submitted on 18 Nov 2010

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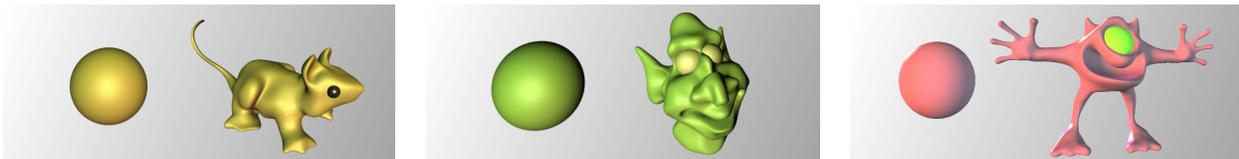
Swirling-Sweepers: Constant Volume Modeling

Alexis Angelidis*
University of Otago

Marie-Paule Cani†
Laboratoire GRAVIR‡

Geoff Wyvill§
University of Otago

Scott King¶
University of Otago



Swirling-sweepers is a new method for modeling shapes while preserving volume. The artist describes a deformation by dragging a point along a path. The method is independent of the geometric representation of the shape. It preserves volume and avoids self-intersections, both local and global. It is capable of unlimited stretching and the deformation can be controlled to affect only a part of the model.

1 Motivation

In a virtual modeling context, there is no material. A challenge for computer graphics is to provide a modeling tool that convinces the artist that there is a material. Volume is one of the most important factors influencing the way an artist models with real materials.

The limitation of existing volume-preserving methods is either that they only apply to a specific type of geometric representation, or they only apply to shapes whose volume can be computed, with the exception of [Decaudin 1996]. His technique does not always preserve volume, and is discontinuous at one point.

2 Principle of Swirling-Sweepers

A Swirling-Sweeper is a new space deformation based on our framework called Sweepers [Angelidis et al. 2004b]. It is a blend of simpler deformations that we call *swirls*. In Figure 1, we show that a swirl is a rotation whose magnitude decreases away from its center, c . We represent the magnitude of rotation by a C^2 monotonic scalar function, ϕ , which vanishes outside a neighborhood of radius λ around c . More formally, a swirl is a rotation matrix raised to the power ϕ

$$f(p) = \exp(\phi(\|p - c\|) \log M) p \quad (1)$$

A swirl preserves volume since the determinant of its Jacobian is always equal to 1. There is a convenient way of blending n swirls to produce a more complex deformation

$$f_n(p) = \exp\left(\sum_{i=1}^n \phi(\|p - c_i\|) \log M_i\right) p \quad (2)$$

See [Angelidis et al. 2004a] for computing exp and log.

From Swirls to Swirling-Sweepers: By specifying a single translation \vec{t} , an artist can input n swirls. As shown in Figure 2, we place n swirl centers, c_i , on the circle of center h , and radius r lying in a plane perpendicular to \vec{t} . These points correspond to n consistently-oriented unit tangent vectors \vec{v}_i . Each pair, (c_i, \vec{v}_i) , together with an angle, θ , define a rotation. Along with radii of neighborhood $\lambda = 2r$, we define n swirls. The radius of the circle, r , is left to the user to choose. The following value for θ will transform h exactly into $h + \vec{t}$, and preserves volume for sufficiently small \vec{t} :

$$\theta = \frac{2\|\vec{t}\|}{nr} \quad (3)$$

*email:alexis@cs.otago.ac.nz

†email:Marie-Paule.Cani@imag.fr

‡GRAVIR is a joint lab of CNRS, INRIA, Institut National Polytechnique de Grenoble and Université Joseph Fourier.

§email:geoff@cs.otago.ac.nz

¶email:scott@cs.otago.ac.nz

Preserving coherency and volume: To preserve coherency and volume, it is necessary to subdivide input vector \vec{t} into a series of smaller vectors. We use $s = \max(1, \lceil -4\|\vec{t}\|/r \rceil)$ sub-vectors. This decomposition is shown in Figure 3.

Achieving Real-Time: We have a closed-form for the logarithm of a rotation matrix and also for computing $(\exp N)^p$, when N is the logarithm of an unknown rotation matrix. These formulas, together with a more complete discussion can be found in [Angelidis et al. 2004a]. They save otherwise expensive numerical approximations.

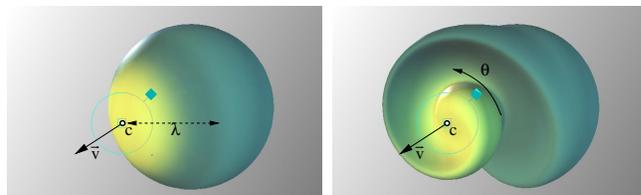


Figure 1: Swirl of center c , rotation angle θ around \vec{v} .

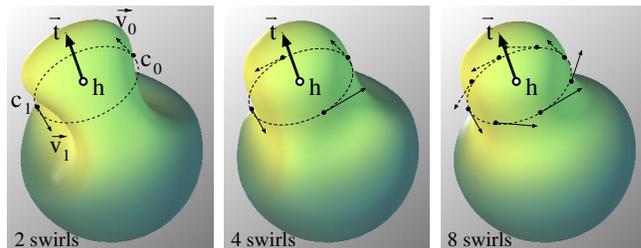


Figure 2: n swirls arranged in a ring creates more complex deformations. There are no visible artifacts with 8 swirls.

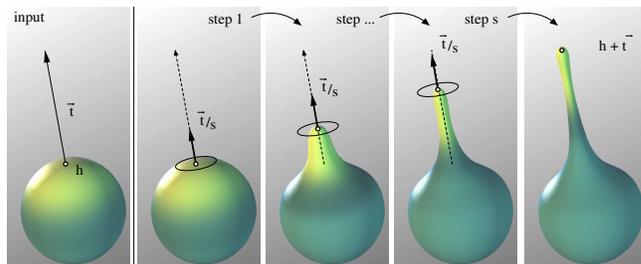


Figure 3: Volume preservation is obtained by composing rings of swirls. The selected point is precisely controlled.

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