



HAL
open science

Hybrid control of a three-cell converter associated to an inductive load

Mohamed Trabelsi, Jean-Marie Rétif, Xuefang Lin-Shi, Xavier Brun, Florent Morel, Pascal Bevilacqua

► **To cite this version:**

Mohamed Trabelsi, Jean-Marie Rétif, Xuefang Lin-Shi, Xavier Brun, Florent Morel, et al.. Hybrid control of a three-cell converter associated to an inductive load. IEEE PESC, Jun 2008, Rhodes, Greece. pp.3519-3525, 10.1109/PESC.2008.4592500 . hal-00374698

HAL Id: hal-00374698

<https://hal.science/hal-00374698>

Submitted on 3 Jun 2009

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Hybrid Control of a Three-Cell Converter Associated to an Inductive Load

M. Trabelsi, J.M. Retif, X. Lin-Shi, X. Brun, F. Morel, P. Bevilacqua
INSA-Lyon, Laboratory AMPERE CNRS UMR 5005, Villeurbanne, France
mohamed.trabelsi@insa-lyon.fr

Abstract - This paper presents a control scheme for a multi-level multi-cell converter. For this type of converters, load current and capacitor voltages must be jointly controlled. Moreover the real-time constraint is important. This constraint leads us to propose a control based on a simplified state-space model. The model allows predicting the state vector evolution for every converter configuration. The control algorithm directly determines the converter switching state which minimizes a simple cost function. A normalization of the state variables is proposed for the cost function calculation in order to ensure a trade-off between the tracking of the load current and the tracking of the capacitor voltages. The proposed control scheme is detailed and compared with a classical control scheme with simulations. Finally, experimental results are presented to show the effectiveness of the proposed method.

Keywords - Dynamic Hybrid Systems, Multi-cell converter, Hybrid control, Digital Signal Processing.

I. INTRODUCTION

A large number of industrial applications are composed of a continuous process controlled by an energy modulator which has a finite number of configurations. These systems constitute a class of Hybrid Dynamic Systems (HDS). In the field of power electronics, static converters associated with a load is an example of this class of HDS.

During this last decade, multi-cell converters have grown from an attractive concept to industrial applications, especially for use in high-power applications [1] [2]. Indeed, the output waveforms of this type of topologies are improved compared to the classical two-level converter technologies with the same switching frequency. These structures also allow reducing filtering elements. Fig. 1 shows a three-cell converter feeding a passive load formed by an inductor (L) and a resistor (R). The control objective is to control the load current (I) as well as the capacitor voltages (E_1 and E_2). Generally a continuous control approach is used. Later, a modulation strategy is applied to translate the continuous control into switching orders [3]. For example, a nonlinear control by input-output linearization is proposed in [4]. Recently, a passivity based control using an averaged model [5], a stabilizing method using a Lyapunov function and a predictive control approach with optimization procedures [6] have been compared in [7].

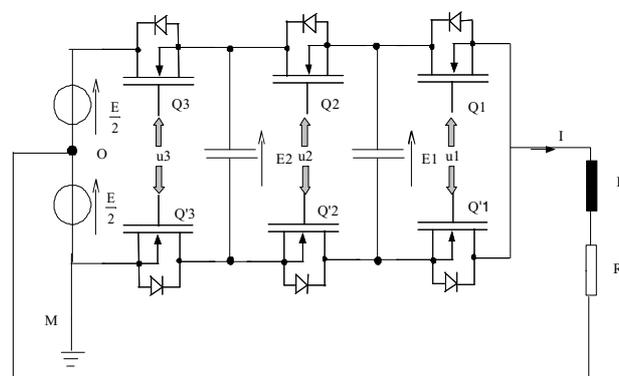


Fig. 1. The three-cell converter

In this paper, a direct control is proposed where the control variables are directly the converter switching states, so any modulation strategy is necessary. The control scheme takes into account the hybrid nature of the system. In this context, the hybrid control term is used in the following sections.

II. HYBRID CONTROL APPROACH

In the hybrid control context, the actuator and the continuous process are not separated for the modelling. So the state model includes continuous and discrete variables. Hybrid control directly chooses discrete state of the actuator in order to track the reference values for the continuous process state vector. Fig. 2 shows the synoptic of the hybrid control.

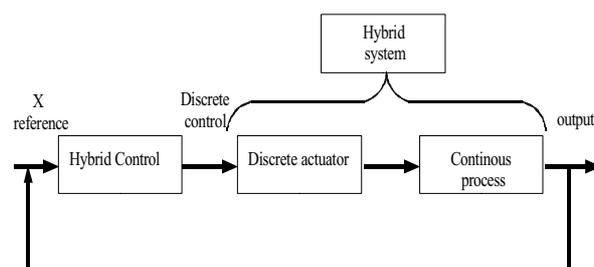


Fig. 2. Hybrid control synoptic

The hybrid control approach includes four fundamental steps. The first one consists in modelling the hybrid system by taking in consideration both the discrete and the continuous variables. The obtained model may be non-linear. In the case where the real-time constraint is important, a second step consists on finding a simplified model valid for a computation occurrence which will be computed for each possible system configuration at each calculation period. In the third step, hybrid control uses a choice strategy to select a configuration which minimizes a cost function. Finally, the selected configuration is applied for the next sampling period.

In this paper, these steps are detailed for the three-cell converter. Simulated results will be compared between a classical PWM control and the hybrid proposed control. Finally, experimental results obtained with the proposed control approach will be exposed.

III. THREE-CELL DC-DC CONVERTER MODEL

In the following section, a simple algebraic method will be detailed in order to find an explicit standard model including all the converter configurations.

A. Hybrid Model

For the proposed hybrid control, an instantaneous model of the three-cell dc-dc converter involving continuous elements (capacitors, inductor and resistor) as well as discrete elements (switching states) is used. The switching state associated with each commutation cells (Q_j, Q'_j) is noted as $u_j \in \{0,1\}$ ($j = 1, 2, 3$). When $u_j = 1$, the upper switch of the cell j is "on" and the lower switch is "off" whereas it will be "off" whenever $u_j = 0$ and the lower switch is "on". From electrical equations, it can be written:

$$\begin{aligned} C_1 \frac{dE_1}{dt} &= I(u_2 - u_1); C_2 \frac{dE_2}{dt} = I(u_3 - u_2) \\ V_{ao} &= L \frac{dI}{dt} + R.I \end{aligned} \quad (1)$$

By noting V_{swj} the voltage on the transistor Q'_j , it can be written:

$$\begin{aligned} V_{sw3} &= u_3(E - E_2); V_{sw2} = u_2(E_2 - E_1) \\ V_{sw1} &= u_1.E_1 \\ V_{ao} + \frac{E}{2} &= V_{sw1} + V_{sw2} + V_{sw3} \end{aligned} \quad (2)$$

By choosing the two flying capacitor voltages $E_1(t)$, $E_2(t)$ and the load current $I(t)$ as three state variables noted $\underline{X}(t) = [E_1(t) \ E_2(t) \ I(t)]^T$, switching states of the commutation cells $\underline{U}(t) = [u_3 \ u_2 \ u_1]^T$ as the control vector, the state equation, obtained from (1) and (2) can be written as follow:

$$\dot{\underline{X}}(t) = \underbrace{\begin{pmatrix} 0 & 0 & \frac{u_2 - u_1}{C_1} \\ 0 & 0 & \frac{u_3 - u_2}{C_2} \\ \frac{u_1 - u_2}{L} & \frac{u_2 - u_3}{L} & -\frac{R}{L} \end{pmatrix}}_{A(u)} \cdot \underline{X}(t) + \underbrace{\begin{pmatrix} 0 \\ 0 \\ \frac{1}{L} \cdot u_3 - \frac{1}{2L} \end{pmatrix}}_{B(u)} \cdot E \quad (3)$$

For the considered converter, there are two switching states for each leg, so that eight different configurations are noted, from U_1 to U_8 ($\underline{U}_i(t), i=1, \dots, 8$) with $U_i = [u_3 \ u_2 \ u_1]$. The hybrid model (3) can be expressed by:

$$\dot{\underline{X}}_i(t) = A_i \cdot \underline{X}(t) + B_i \quad (4)$$

For a given configuration U_i , A_i and B_i are constant matrix. So a corresponding discrete-time model for a sampling period T_e can be calculated:

$$\underline{X}_i(k+1) = \phi_i(T_e) \cdot \underline{X}(k) + \Psi_i(T_e) \cdot B_i \quad (5)$$

with $\phi_i(T_e) = e^{A_i T_e}$ and $\Psi_i(T_e) = \int_0^{T_e} \phi_i(\theta) \cdot d\theta$

B. Simplified Model

As the real-time constraint is important for the considered system, a simplified model is mandatory.

If the sample time is sufficiently small, the state trajectories in the state space can be considered as rectilinear. With this hypothesis, the 8 states at time $(k+1)$ in the state space can be approximated by:

$$\tilde{\underline{X}}_i(k+1) = \underline{X}(k) + \dot{\underline{X}}_i(t) \cdot T_e \quad (6)$$

From a measured state $\underline{X}(k)$, by using (6), the 8 possible directions in the state space after T_e can be determined. Fig. 3 shows an example of these directions.

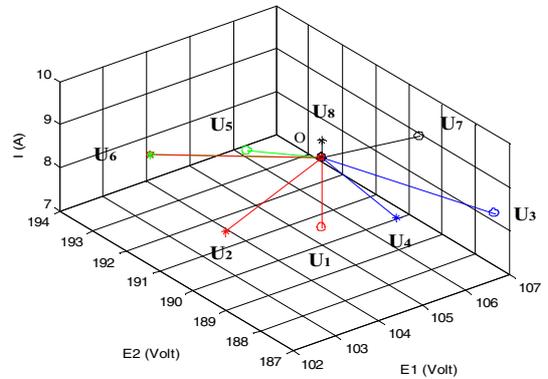


Fig. 3. Example of possible state-vector directions in the state space at a given operating point

For the configurations U_1 and U_8 , the capacitor voltages are constant and the load current varies.

For the configurations U_2 to U_7 , the load current traverses one or two capacitors and the voltage variations are proportional to the current.

C. Validity Domain of the Simplified Model

In order to verify the validity of the simplified model, simulation studies have been made by comparing the discrete-time model (5) and the simplified model (6) with:

$$E = 300V, C_1=C_2=33\mu F, R=33\Omega, L=50mH, T_c = 100\mu s$$

Fig. 4 shows the simulation results for the configuration U_2 when the load current $I=0.5A$. It can be seen that in the plane (E_1, E_2) , the trajectory from $E_1(k) = 100V$, $E_2(k) = 200V$ after T_c will be ever rectilinear but the final point calculated with the discrete-time model is different to the final point calculated with the simplified model. This difference changes with the load current.

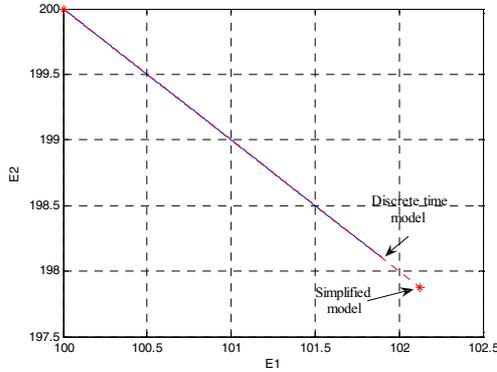


Fig. 4. Difference between discrete final point and approximate final point

We note $ErrE_1$, $ErrE_2$ and $ErrI$ the voltage and current errors between the simplified model and the discrete-time model.

It can be seen from Fig. 5 and Fig. 6 that these errors are proportional to the load current.

We note that the max error on E_2 is similar to on E_1 for different configurations. This can be explained by the fact that the two capacitors are identical.

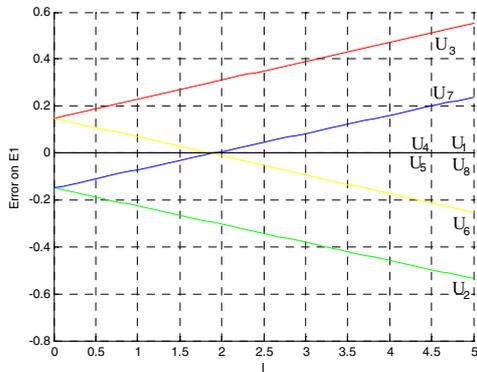


Fig. 5. Error on E_1 (V) versus I (A)

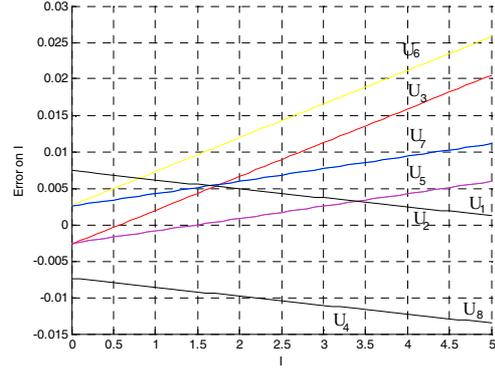


Fig. 6. Error on I (A) versus I (A)

As shown by Fig. 5 and Fig. 6, the maximum errors due to the simplified model are too small, 0.6% for E_1 and 0.3% for E_2 and 25mA for the load current.

This phenomenon can be explained by algebraic way from the expressions of the estimated states as given in the following for the voltage E_1 . The expressions of the voltage value E_1 after a sampling period determined by the model (5) and (6) are respectively:

$$E_{1i}(k+1) = \phi_i(T_c).E_1(k) + \Psi_i(T_c).B_i \quad (7)$$

$$\tilde{E}_{1i}(k+1) = E_1(k) + E_{1i} \cdot T_c \quad (8)$$

Taking, for example, as configuration $U_3 = [0 \ 1 \ 0]$, (7) and (8) become:

$$E_{13}(k+1) = [\beta(E_1(k), E_2(k)) + \delta.I(k)] + \Psi(T_c).B_3 \quad (9)$$

$$\tilde{E}_{13}(k+1) = E_1(k) + \frac{T_c}{C_1}.I(k) \quad (10)$$

where β and δ are constant which depend on Taylor series expansion of $\phi_3(T_c) = e^{A_3.T_c}$.

For the simulation, this expansion is developed in the fifth order. So the constant δ will be different to the constant $\frac{T_c}{C_1}$. Consequently, in the error expression given by (11):

$$ErrE_{13} = \tilde{E}_{13}(k+1) - E_{13}(k+1) = \underbrace{(E_1(k) - \beta(E_1(k), E_2(k)) - \Psi(T_c).B_3)}_{\text{constant}} + \underbrace{\lambda}_{\neq 0}.I(k) \quad (11)$$

the coefficient λ of the load state $I(k)$ will not be null and the error is proportional to the load current. This phenomenon is true for all configurations U_i . The same explanation can be given for the voltage E_2 and the load current I .

Due to the small errors shown in this section, the simplified model is validated for the considered application.

IV. CONTROL STRATEGY

The proposed control proceeds as follows during each sampling period:

- Measure capacitor voltages $E_1(k)$, $E_2(k)$ and load current $I(k)$.
- Predict the state vector $\tilde{\mathbf{X}}_i(k+1) = [\tilde{E}_{1i}(k+1) \ \tilde{E}_{2i}(k+1) \ \tilde{I}_i(k+1)]^T$ for the 8 possible control vectors $\underline{U}_i(t)$ by using (6).
- For a desired reference state $\underline{X}_c = [E_{1c} \ E_{2c} \ I_c]^T$, the control selects the configuration which gives the smallest distance between $\tilde{\mathbf{X}}_i(k+1)$ and $\underline{X}_c = [E_{1c} \ E_{2c} \ I_c]^T$.

The desired reference state is a point in the state space with the coordinates E_{1c} , E_{2c} and I_c . The choice of the capacitor voltages references influences on the values of the output voltage and the quality of the tracking.

A. Voltage Reference Choice

Generally, $E_{1c} = \frac{E}{3}$, $E_{2c} = \frac{2E}{3}$ are chosen in order to share out the voltages on the cells. This section will prove that these voltage references allow the maximum freedom degrees in the state space. The freedom degree is defined as the possibility of increase or decrease of a state variable.

Considering the state variations with a positive value of the load current, the projection in the plane (E_1, E_2) of the vector evolutions relative to the 8 converter configurations is shown by Fig. 7.

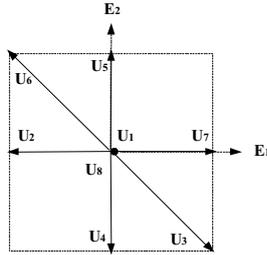


Fig. 7. State vectors projections in the plane $E_1 E_2$ for $I > 0$

From (3), it can be determined the derivative of the load current for each configuration (Table I).

TABLE I.
CURRENT DERIVATIVE

Configuration	Current Derivative
U_1	$\frac{-E-2.R.I}{2.L}$
U_2	$\frac{2.E_1-E-2.R.I}{2.L}$
U_3	$\frac{-E-2.E_1+2.E_2-2.R.I}{2.L}$
U_4	$\frac{-E+2.E_2-2.R.I}{2.L}$
U_5	$\frac{-E-2.E_2-2.R.I}{2.L}$
U_6	$\frac{E+2.E_1-2.E_2-2.R.I}{2.L}$
U_7	$\frac{E-2.E_1-2.R.I}{2.L}$
U_8	$\frac{E-2.R.I}{2.L}$

On the Fig. 8, the straight lines in the lower triangles refer to the null variation of the load current (the configurations U_1 and U_8 are not presented because the capacitor voltages are constant). The (+) area refers to the positive variation of the current load and the (-) area refers to the negative variation.

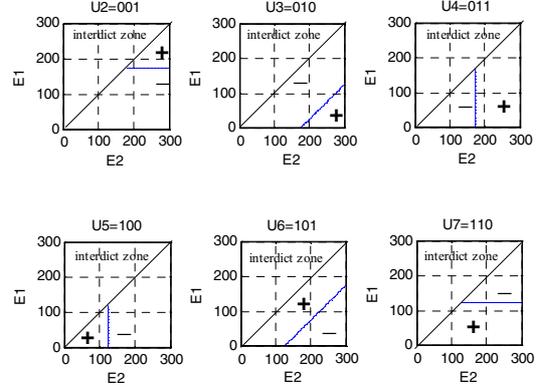


Fig. 8. Iso-increase of the load current on the voltages plane

The concatenation of these areas in the same plane (E_2, E_1) allows parting the plane in ten areas as presented in Fig. 9.

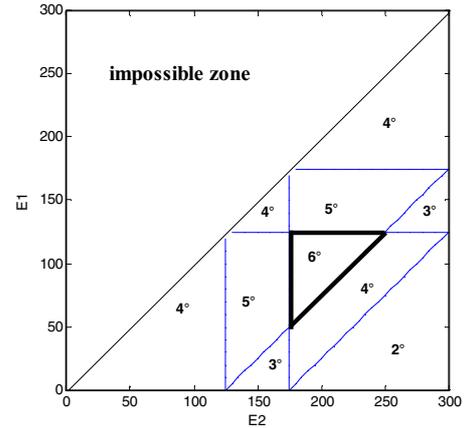


Fig. 9. Reference areas on the plane (E_2, E_1)

Each area refers to voltages references and is marked by the number of freedom degrees available to reach this reference. The best choice is the voltage references which correspond to maximum freedom degree area.

For $E=300V$, the choice of the classic reference $E_{1c} = \frac{E}{3} = 100V$, $E_{2c} = \frac{2E}{3} = 200V$ leads to 6 freedom degrees which is maximum.

B. Choice Strategy

At each sampling period, the control algorithm calculates the distance between the reference point and the reached point of each configuration. The configuration which corresponds to the minimal distance is selected. This choice strategy does not allow to reach suitably the reference. On the one hand, state vector components are not homogeneous (Ampere and Volt). On the other hand, the weight of the components are very different for the

considered application (hundreds Volt for voltages and a few Ampere for current).

Due to these facts, the state variables are normalized. The normalization influences the configuration selection. By choosing:

$$\begin{cases} \Delta E_1 = \left| \max(\tilde{E}_{1i}(k+1)) - \min(\tilde{E}_{1i}(k+1)) \right| \\ \Delta E_2 = \left| \max(\tilde{E}_{2i}(k+1)) - \min(\tilde{E}_{2i}(k+1)) \right| \\ \Delta I = \left| \max(\tilde{I}_i(k+1)) - \min(\tilde{I}_i(k+1)) \right| \end{cases} \quad (12)$$

the distance between $\tilde{\underline{X}}_i(k+1)$ and $\underline{X}_c = [E_{1c} \ E_{2c} \ I_c]^T$ after normalization is calculated by:

$$\text{dist}_i = \sqrt{\left(\frac{E_{1c} - \tilde{E}_{1i}}{\Delta E_1}\right)^2 + \left(\frac{E_{2c} - \tilde{E}_{2i}}{\Delta E_2}\right)^2 + \left(\frac{I_c - \tilde{I}_i}{\mu \cdot \Delta I}\right)^2} \quad (13)$$

μ is a weighting factor which allows a trade-off between the current tracking and the voltage tracking. Indeed, a good tracking of the capacitor voltages leads to oscillations on the load current. For better current tracking, voltage tracking performance must be reduced. The factor μ is determined experimentally and is kept constant during the running of the algorithm. When μ is small, the priority is given to the current tracking. When μ is large, it favours the voltages tracking.

V. COMPARISON WITH PWM CONTROL

In order to show the advantages of the proposed control, simulation study has been performed to make a comparison with the classical PWM control.

The PWM control applied to the three-cell converter consists on comparing a reference signal chosen sinusoidal with three triangle waveforms which have the same period T_{mod} but phase-shifted to $T_{\text{mod}}/3$ and $2T_{\text{mod}}/3$. The reference signal is given by a current PI controller.

The simulation of the hybrid control and the PWM control are made on the same conditions than the experiment study presented in the previous section: $C_1=C_2=33\mu\text{F}$, $R=33\Omega$, $L=50\text{mH}$, $E=120\text{V}$. The voltages references are chosen as $E_{1c} = \frac{E}{3}$, $E_{2c} = \frac{2E}{3}$ while a sinusoidal current reference is imposed. For the PWM control, $T_{\text{mod}}=1\text{ ms}$ and the computation period is $10\ \mu\text{s}$.

Fig. 10 and Fig. 11 show the tracking of the load current with the two controls. The simulation test of the hybrid control is made with a small value of the weighting factor μ .

Fig. 12, Fig. 13 and Fig. 14 show the waveforms of the capacitor voltages and the load voltage.

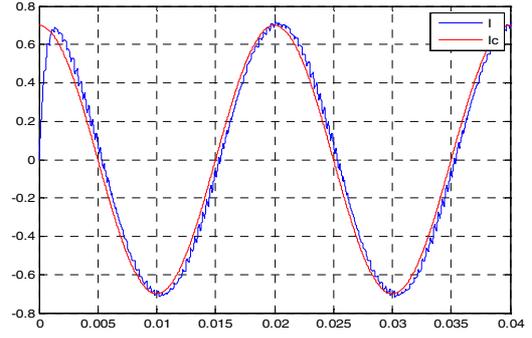


Fig. 10. Load current (A) with the PWM control versus time (s)

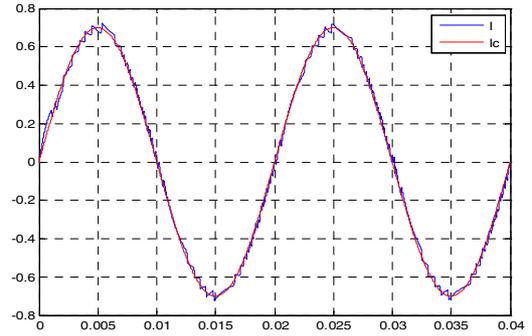


Fig. 11. Load current (A) with the Hybrid control versus time (s)

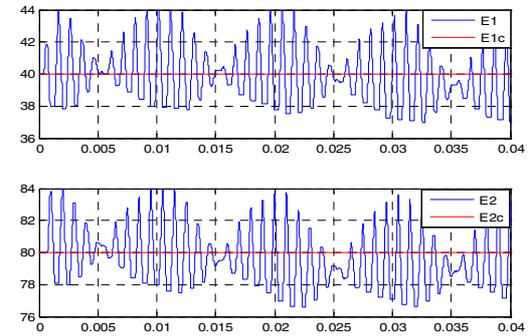


Fig. 12. Capacitors voltages (V) with the PWM control versus time (s)

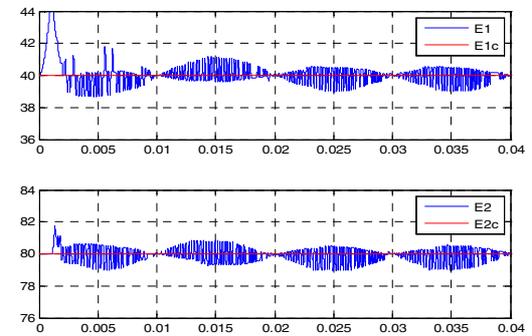


Fig. 13. Capacitors voltages (V) with the Hybrid control versus time (s)

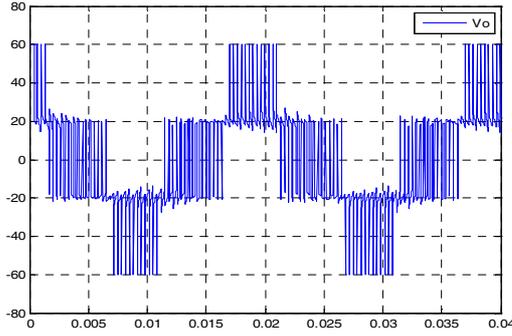


Fig. 14. Load voltage (V) versus time (s)

With the PWM control, a phase shift between the reference and the obtained load current can be noted.

It can be noted also that the voltage errors in the hybrid case are about $\pm 1V$ while the PWM control has about $\pm 4V$ voltage errors.

For the load voltage, the two controls reach suitably the intermediary voltage levels.

We note that the PWM method not pose any difficulty for analogical realisation. But it requires a large computation frequency in the case of digital implementation. Due to this technologic constraint, the experiment study was conducted only for the hybrid control in the next section.

VI. EXPERIMENTAL RESULTS

The experiment study of the hybrid control was conducted with an equipment composed of a three cell converter ($C_1=C_2=33\mu F$) fed by a continuous supply ($E=120V$) and associated to a passive load ($R=33\Omega$, $L=50mH$). The proposed control algorithm is implemented in C language and computations are performed by a dSpace dS1104 controller board. The sampling period is fixed to $70\mu s$ since L/R is about $1.5ms$. For each period, an interruption starts and the proposed control determines the switching states $\underline{U}(t)=[u_1 \ u_2 \ u_3]^T$ to apply. The numeric outputs of the dS1104 are used to control the converter drivers by optical fibres. Data recording and reference value tuning are performed within the Control Desk environment.

The voltages references are chosen as $E_{1c} = \frac{E}{3}$, $E_{2c} = \frac{2E}{3}$ while a sinusoidal current reference is imposed.

Many tests are made for different values of the factor μ in order to show its influence on the tracking quality.

At first, a small value of μ is chosen to favour the current tracking as shown in Fig. 15. Voltages references are maintained with about $\pm 3V$ oscillation amplitude (Fig. 16).

The load voltage levels are given by Fig. 17. It can be noted that four voltage levels can be obtained.

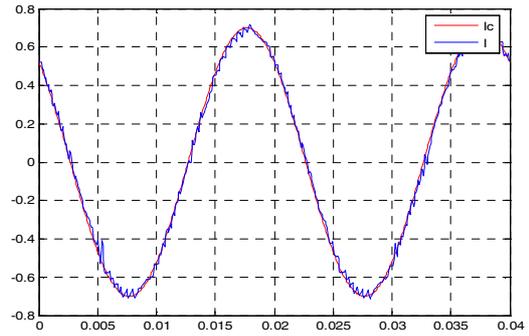


Fig. 15. Load current (A) versus time (s)

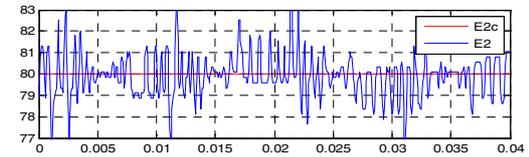
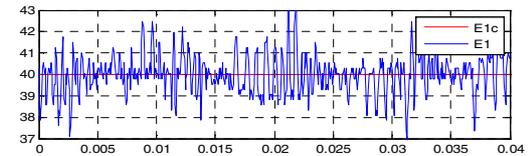


Fig. 16. Capacitor voltages (V) versus time (s)

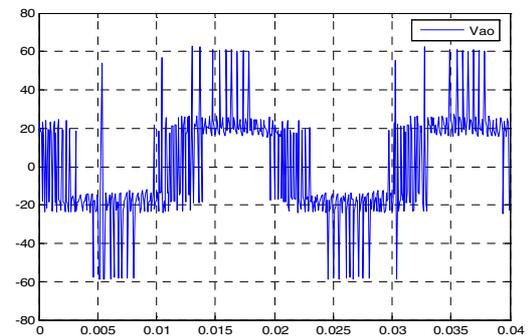


Fig. 17. Load voltage (V) versus time (s)

In the second time, the test is made with increasing the value of μ . It can be noted the deterioration of the current tracking (Fig. 18) and the improvement of the capacitor voltages which is maintained to reference values with about $\pm 1.9V$ oscillation amplitude (Fig. 19).

Finally, a test is made while a square current reference is imposed (Fig.20).

REFERENCES

- [1] L.M. Tolbert and F.Z. Peng, "Multilevel converters for large electric drives", *Proc. IEEE APEC'98*, vol. 2, pp. 530-536, February 1998.
- [2] T. A. Meynard, H. Foch, P. Thomas, J. Courault, R. Jakob and M. Nahrstaedt, "Multi-cell converters: basic concepts and industry applications", *IEEE Transaction on Industrial Applications*, vol. 49, no. 5, p. 955-964, October 2002.
- [3] P.M. Bhagwat and V.R. Stefanovic, "Generalized structure of a multilevel PWM inverter", *IEEE Trans. on Industrial Applications*, vol. 32, pp 509-517, May/June 1996.
- [4] G. Gateau, M. Fadel, P. Maussion, R. Bensaid and T. Meynard, "Multicell converters: active control and observation of flying-capacitor voltages", *IEEE Trans. on Industrial Electronics*, vol. 49, no. 5, pp 998-1008, October 2002.
- [5] H. Sira-Ramirez, R. Perez-Moreno, R. Ortega and M. Garcia-Esteban, "Passivity-based controllers for the stabilization of dc-to-dc power converters", *Automatica*, vol. 33, no. 4, pp. 499-513, April 1997.
- [6] B. Potoenik, G. Music and B. Wupancic, "Model predictive control of discrete-time hybrid systems with discrete inputs", *ISA Transactions*, vol. 44, no. 2, April 2005.
- [7] M. Baja, D. Patino, H. Cormerais, P. Riedinger and J. Buisson, "Hybrid control of a three-level three-cell dc-dc converter", *American control conference*, p. 5458 – 5463, July 2007.

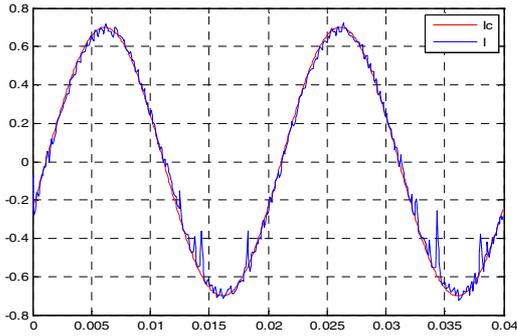


Fig. 18. Load current (A) versus time (s)

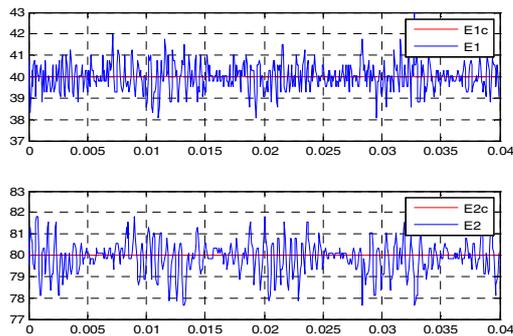


Fig. 19. Load current (A) versus time (s)

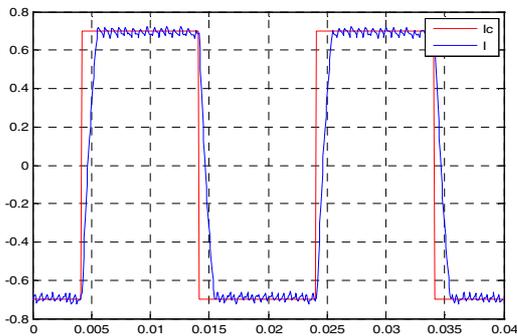


Fig. 20. Load current (A) versus time (s)

We note that the measured load current reaches the reference value after 1.5ms. This value refers to the L/R ratio.

VII. CONCLUSION

In this paper, a hybrid control strategy has been presented for the control of a three-cell DC-DC converter. It is based on a hybrid model in which both discrete and continuous variables are considered. Due to the real-time constraint, a simplified model is used. For real-time implementation, the validity of the simplified model is demonstrated. The choice of the reference voltages is justified. This paper presents a comparative simulation study between the classic PWM control and the proposed hybrid control which proves the advantages of the exposed approach. The experimental results are exposed with explaining the influence of the normalization and the weighting factor for a suitable reaching of the references.