



HAL
open science

A Comparison of Two Methods for Selecting Vibrational Configuration Interaction Spaces on a Heptatomic System: Ethylene Oxyde

Didier Bégué, Neil Gohaud, Claude Pouchan, Patrick Cassam-Chenaï, Jacques Liévin

► **To cite this version:**

Didier Bégué, Neil Gohaud, Claude Pouchan, Patrick Cassam-Chenaï, Jacques Liévin. A Comparison of Two Methods for Selecting Vibrational Configuration Interaction Spaces on a Heptatomic System: Ethylene Oxyde. *Journal of Chemical Physics*, 2007, 127, <http://dx.doi.org/10.1063/1.2795711>. 10.1063/1.2795711 . hal-00151806

HAL Id: hal-00151806

<https://hal.science/hal-00151806>

Submitted on 5 Jun 2007

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

A Comparison of Two Methods for Selecting Vibrational Configuration Interaction Spaces on a Heptatomic System: Ethylene Oxide

Didier Bégué, Neil Gohaud and Claude Pouchan

*Institut Pluridisciplinaire en Recherche sur l'Environnement et les Matériaux (IPREM), UMR-5254-CNRS, Equipe de Chimie-Physique (ECP), IFR - rue Jules Ferry - BP 27540 - F-64075 PAU Cedex France.
didier.begue@univ-pau.fr, claude.pouchan@univ-pau.fr*

Patrick Cassam-Chenai

Laboratoire de Mathématique J. A. Dieudonné, UMR 6621 du CNRS, Faculté des Sciences, Parc Valrose, 06108 Nice cedex 2, France. cassam@unice.fr

Jacques Liévin

Université Libre de Bruxelles, Service de Chimie Quantique et Photophysique, CP 160/09, 50 Av. F.D. Roosevelt, B-1050 Bruxelles, Belgium. jlievin@ulb.ac.be

Abstract

Two recently developed methods for solving the molecular vibrational Schrödinger equation, namely, the parallel vibrational multiple window configuration interaction (P-VMWCI) and the vibrational mean field configuration interaction (VMFCI), are presented and compared on the same potential energy surface of ethylene oxide, $c\text{-C}_2\text{H}_4\text{O}$. It is demonstrated on this heptatomic system with strong resonances that both approaches converge towards the same fundamental frequencies. This confirms their ability to tackle the vibrational problem of large molecules for which full configuration interaction calculations are not tractable.

1 Introduction

The vibrational configuration interaction approach consists in diagonalizing the molecular vibrational Hamiltonian in a finite dimensional subspace of the Hilbert space associated to the system. This approximation method is known as Galerkin's method in mathematics. The variational principle insures that the larger the subspace the more accurate the results will be. However, in practice the rate of convergence depends not only on the dimension but also on the nature of the wave functions spanning the vector subspace. This dependency is crucial, as can be easily understood by considering the limit case where the variational subspace is the space spanned by the exact states searched for. Then, the diagonalisation of the Hamiltonian in this subspace will give the exact solution. Of course, this never happens in practice, however, clearly, it is advantageous to get as close as possible to this ideal case.

This issue has triggered the two variational approaches which are studied in this article, namely, the parallel vibrational multiple window configuration interaction (P-VMWCI) method [1,2] and the vibrational mean-field configuration interaction (VMFCI) method [3–5]. Our goal is to assess these approaches on a molecular system out-of-reach of standard methods. We have chosen a heptatomic molecule of astrophysical and exobiological interest [6–12], ethylene oxide, $c\text{-C}_2\text{H}_4\text{O}$, see Figure 1.

Since a full CI reference calculation is not feasible to assess each method individually, it is appropriate to evaluate them one against the other. As a matter of fact, the variational space selection processes in the two CI methods are unrelated, so the two approaches can be considered as independent. Comparison with the standard vibrational self-consistent field (VSCF)/vibrational configuration interaction (VCI) approach is also provided in order to demonstrate the superiority of the new selection strategies.

The article is organized as follows: In the next section, we recall the molecular vibrational eigenproblem and the two strategies we have developed to solve it. Then, we evaluate the convergence of numerical computations on ethylene monoxide. Finally, we conclude on the reliability of the two approaches and the new insight they provide on experimental data.

2 Two recently developed strategies to solve the molecular vibrational eigenproblem

2.1 The molecular vibrational eigenproblem

In this work, we consider a vibrational Hamiltonian to quartic order expressed as:

$$H_{vib} = H_{harm} + V_{cubic} + V_{quartic} \quad (1)$$

where,

$$H_{harm} = \left(\frac{\hbar}{2}\right) \sum_{s=1}^{n_{vib}} \lambda_s^{1/2} (p_s^2 + q_s^2), \quad (2)$$

$$V_{cubic} = \sum_{s,s',s''=1}^{n_{vib}} k_{s,s',s''} q_s q_{s'} q_{s''}, \quad (3)$$

$$V_{quartic} = \sum_{s,s',s'',s'''=1}^{n_{vib}} k_{s,s',s'',s'''} q_s q_{s'} q_{s''} q_{s'''}. \quad (4)$$

In Eqs. (2) to (4), the q_s 's are the scaled, mass-weighted, normal coordinates, the p_s 's their conjugate momenta, with s running from one to n_{vib} , the number of vibrational degrees of freedom.

The harmonic Hamiltonian, H_{harm} will be considered as the zero order Hamiltonian. For each degree of freedom, the wavefunctions and energies, solutions of the harmonic vibrational equation, will be denoted by $|n_s\rangle$ and $E_s^{(0)}(n_s)$ respectively, with,

$$\langle n'_s | n_s \rangle = \delta_{n_s, n'_s}, \quad (5)$$

and

$$E_s^{(0)}(n_s) = hc\nu_s \left(n_s + \frac{1}{2}\right), \quad (6)$$

where ν_s is the harmonic wavenumber.

The tensor product functions $|n_1, n_2, \dots, n_{n_{vib}}\rangle$,

$$|n_1, n_2, \dots, n_{n_{vib}}\rangle = \bigotimes_{s=1}^{n_{vib}} |n_s\rangle \quad (7)$$

are orthonormal and represent a base for the expansion of the vibrational wave functions $|\Psi_i\rangle$, ($i \in [1, N]$) that are searched for:

$$|\Psi_i\rangle = \sum_{n_1, n_2, \dots, n_{n_{vib}}} C_{n_1, n_2, \dots, n_{n_{vib}}}^i |n_1, n_2, \dots, n_{n_{vib}}\rangle. \quad (8)$$

Generally, the anharmonic vibrational Schrödinger equation:

$$H_{vib} |\Psi\rangle = E |\Psi\rangle \quad (9)$$

is solved with the help of variational [1–4,13–26], perturbational [27–31] (although even for the one-dimensional quartic oscillator the perturbation series is strongly divergent and particularly hard to renormalize [32]), or hybrid methods [33–36]. Choosing one of these approaches is often related to the numerical precision one wants to obtain.

Ideally, the best variational approach would consist in diagonalizing the Hamiltonian H_{vib} in the space spanned by the $|n_1, n_2, \dots, n_{n_{vib}}\rangle$'s. However, this becomes rapidly prohibitive as the number of degrees of freedom increases, even if a finite but realistic set of functions per degree is used. It is necessary to build variational subspaces of tractable dimensions on which the projection of the vibrational wave functions of interest is as large as possible. This issue has triggered the two variational approaches which are presented hereafter, namely, the parallel vibrational multiple window configuration interaction (P-VMWCI) method and the vibrational mean-field configuration interaction (VMFCI) method.

2.2 P-VMWCI

Performing a full VCI in a reasonable basis set for a molecule of five or more atoms is out-of-reach of present days' computer capabilities. However, the vibrational spectrum of molecules of this size becomes amenable to theoretical calculations if the total spectrum is splitted into several windows of smaller sizes.

The configuration space corresponding to a given window can be constructed iteratively, starting with an initial space, S_0 , chosen by the user as a subset of the N -dimensional full VCI space,

$$S = \left\{ |n_1^i, n_2^i, \dots, n_{n_{vib}}^i\rangle; 1 \leq i \leq N \right\}. \quad (10)$$

Let A be the union of the set reduced to the identity and the set of all the excitation operators and their Hermitian conjugate (de-excitation operators) appearing with a significant coefficient in the anharmonic potential, Eqs.(3,4),

if the latter is rewritten in second quantization. That is to say, denoting by Q_s^\dagger , (respectively Q_s), the creation, (respectively annihilation), operator for mode s :

$$\begin{aligned}
A &= A_0 \cup A_1 \cup A_2 \cup A_3 \cup A_4 \\
A_0 &= \{1\} \text{ , (no excitation)} \\
A_1 &= \left\{ Q_s^\dagger, Q_s, \text{ such that } \exists s', |k_{s,s',s'}| > \varepsilon ; 1 \leq s, s' \leq n_{vib} \right\} \\
&\cup \left\{ Q_s^{\dagger 2}, Q_s^2, \text{ such that } \exists s', |k_{s,s,s',s'}| > \varepsilon ; 1 \leq s, s' \leq n_{vib} \right\} \\
&\cup \left\{ Q_s^{\dagger 3}, Q_s^3, \text{ such that, } |k_{s,s,s}| > \varepsilon ; 1 \leq s \leq n_{vib} \right\} \\
&\cup \left\{ Q_s^{\dagger 4}, Q_s^4, \text{ such that, } |k_{s,s,s,s}| > \varepsilon ; 1 \leq s \leq n_{vib} \right\} \text{ ,} \\
A_2 &= \left\{ Q_s^\dagger Q_{s'}^\dagger, Q_s^\dagger Q_{s'}^\dagger, Q_s Q_{s'}^\dagger, \text{ such that, } \exists s'', |k_{s,s',s'',s''}| > \varepsilon ; s \neq s' ; 1 \leq s, s', s'' \leq n_{vib} \right\} \\
&\cup \left\{ Q_s^{\dagger 2} Q_{s'}^\dagger, Q_s^2 Q_{s'}^\dagger, Q_s^{\dagger 2} Q_{s'}^\dagger, Q_s^2 Q_{s'}^\dagger, \text{ such that, } |k_{s,s,s'}| > \varepsilon ; s \neq s' ; 1 \leq s, s' \leq n_{vib} \right\} \\
&\cup \left\{ Q_s^{\dagger 3} Q_{s'}^\dagger, Q_s^3 Q_{s'}^\dagger, Q_s^{\dagger 3} Q_{s'}^\dagger, Q_s^3 Q_{s'}^\dagger, \text{ such that, } |k_{s,s,s,s'}| > \varepsilon ; s \neq s' ; 1 \leq s, s' \leq n_{vib} \right\} \\
&\cup \left\{ Q_s^{\dagger 2} Q_{s'}^{\dagger 2}, Q_s^2 Q_{s'}^2, Q_s^2 Q_{s'}^2, \text{ such that, } |k_{s,s,s',s'}| > \varepsilon ; s \neq s' ; 1 \leq s, s' \leq n_{vib} \right\} \text{ ,} \\
A_3 &= \left\{ Q_s^\dagger Q_{s'}^\dagger Q_{s''}^\dagger, Q_s Q_{s'}^\dagger Q_{s''}^\dagger, Q_s Q_{s'} Q_{s''}^\dagger, Q_s Q_{s'} Q_{s''}^\dagger, \right. \\
&\quad \left. \text{such that, } |k_{s,s',s''}| > \varepsilon ; 1 \leq s, s', s'' \leq n_{vib} \text{ all distinct} \right\} \\
&\cup \left\{ Q_s^\dagger Q_{s'}^\dagger Q_{s''}^{\dagger 2}, Q_s^\dagger Q_{s'}^\dagger Q_{s''}^2, Q_s^\dagger Q_{s'} Q_{s''}^{\dagger 2}, Q_s^\dagger Q_{s'} Q_{s''}^2, Q_s Q_{s'} Q_{s''}^{\dagger 2}, Q_s Q_{s'} Q_{s''}^2, \right. \\
&\quad \left. \text{such that, } |k_{s,s',s'',s''}| > \varepsilon ; 1 \leq s, s', s'' \leq n_{vib} \text{ all distinct} \right\} \text{ ,} \\
A_4 &= \left\{ Q_s^\dagger Q_{s'}^\dagger Q_{s''}^\dagger Q_{s'''}^\dagger, Q_s Q_{s'}^\dagger Q_{s''}^\dagger Q_{s'''}^\dagger, Q_s Q_{s'} Q_{s''}^\dagger Q_{s'''}^\dagger, Q_s Q_{s'} Q_{s''} Q_{s'''}^\dagger, Q_s Q_{s'} Q_{s''} Q_{s'''}^\dagger, \right. \\
&\quad \left. \text{such that, } |k_{s,s',s'',s'''}| > \varepsilon ; 1 \leq s, s', s'', s''' \leq n_{vib} \text{ all distinct} \right\} \text{ ,} \tag{11}
\end{aligned}$$

where, in general, $\varepsilon = 0$. However, a non negative value can be used in some cases, to reduce the cardinal of A .

Then, the configuration space at order γ , is defined recursively to be the space, S_γ , in direct interaction with $S_{\gamma-1}$. It is made of all the configurations coupled by an operator of A with a configuration of $S_{\gamma-1}$:

$$\begin{aligned}
S_\gamma &= \{ | n_1, n_2, \dots, n_{n_{vib}} \rangle \in S, \text{ such that } \exists \alpha \in \mathbb{C}; \exists \hat{a} \in A; \exists | m_1, m_2, \dots, m_{n_{vib}} \rangle \in S_{\gamma-1}; \\
&\quad | n_1, n_2, \dots, n_{n_{vib}} \rangle = \alpha \hat{a} | m_1, m_2, \dots, m_{n_{vib}} \rangle \} \text{ .} \tag{12}
\end{aligned}$$

Note that with this definition, we have $S_{\gamma-1} \subseteq S_\gamma$, and that a non negative value for ε in Eqs.(11) can reduce the size of S_γ .

The construction of S_γ as defined in Eq.(12) is simple, for the action of the operators of A on HO basis functions is straightforward. This is in contrast with variation-perturbation methods [34,35], in which the iterative building of

the configuration space is based upon perturbational criteria such as,

$$S_\gamma = \{ |n_1^j, n_2^j, \dots, n_{n_{vib}}^j\rangle \in S \text{ such that, } \exists |n_1^i, n_2^i, \dots, n_{n_{vib}}^i\rangle \in S_{\gamma-1};$$

$$\text{and } \left| \frac{\langle n_1^j, n_2^j, \dots, n_{n_{vib}}^j | V_{cubic} | n_1^i, n_2^i, \dots, n_{n_{vib}}^i \rangle}{E_i - E_j} \right| > \varepsilon \}. \quad (13)$$

The construction of S_γ as defined in Eq.(13) is time consuming because the matrix elements of every configuration in $S_{\gamma-1}$ with millions of configurations of S have to be evaluated. Consequently, we reserve the use of the perturbative filter of Eq.(13) to the case where the size of the VCI matrices becomes critical, in order to eliminate weakly coupled configurations, and only when the last iterative γ -step is reached.

For each order γ , p configuration spaces, $S_\gamma^k, 1 \leq k \leq p$, can be constructed independently, corresponding to p spectral windows (as in Table 1). So, this approach lends itself in a natural way to a parallel implementation. The configuration spaces, S_γ^k , or cuts of them, can be distributed among a z -nodes cluster, where the i^{th} node is made of $P_i, 1 \leq i \leq z$, processors, within a parallel SPMD (Single Program Multiple Data) scheme.

This method, that we call ‘‘parallel vibrational multiple window configuration interaction’’ method, generates p VCI matrices, which are much smaller than the full VCI one if γ and the $S_\gamma^k, 1 \leq k \leq p$, are properly chosen. Moreover, for each VCI matrix (or matrix block), the use of both MPI (Message Passing Interface) and computational efforts on loops optimisation enable to distribute tasks among the processors according to their respective clock speed and workload. However, a given configuration can be involved in several windows, specially as γ increases. This drawback is necessary to guarantee the homogeneity of the treatment of the spectral windows regardless of the initial choice, $S_0^k, 1 \leq k \leq p$. The latter, which is controlled by the user with the only restriction that $\forall k, |0, \dots, 0\rangle \in S_0^k$, makes the method particularly flexible.

The performances of the P-VMWCI algorithm are illustrated in Table 1 by the calculation of the ν_{CO} stretching frequency of the H_2CO molecule investigated in a previous work [37]. This table shows how the results converge with γ , for two initial windows of different sizes; a large window covering the $0\text{-}3500\text{cm}^{-1}$ range and a minimal-size window of 1cm^{-1} around the targeted ν_{CO} frequency. The results show that the computational costs are significantly lower with the latter window, whereas the calculated wave numbers are within a few tenth of cm^{-1} .

Note that for the sake of simplicity, we have omitted symmetry considerations in our presentation. However, in practice we make use of symmetry to deal only with symmetry-adapted matrix blocks and to reduce further the dimensions

of the matrices to diagonalize. The same remark holds true for the method presented in the next section.

2.3 VMFCI

Suppose that for a given partition P of the vibrational degrees of freedom of an n_{vib} oscillator system, the following two conditions are met:

(1) The vibrational Hamiltonian can be expanded in a factorized form:

$$H_{vib} = h_0 + \sum_{j_1=1}^{n_P} h_{j_1}(I_{j_1}) + \sum_{1 \leq j_1 < j_2 \leq n_P} h_{j_1, j_2}(I_{j_1}) h_{j_1, j_2}(I_{j_2}) + \cdots + h_{1,2,\dots,n_P}(I_1) h_{1,2,\dots,n_P}(I_2) \cdots h_{1,2,\dots,n_P}(I_{n_P}), \quad (14)$$

where,

$$P = (I_1, I_2, \dots, I_{n_P}) = (\{i_1^1, i_2^1, \dots, i_{k_1}^1\}, \{i_1^2, i_2^2, \dots, i_{k_2}^2\}, \dots, \{i_1^{n_P}, i_2^{n_P}, \dots, i_{k_{n_P}}^{n_P}\}). \quad (15)$$

is a partition of the n_{vib} degrees of freedom into n_P subsets I_1, I_2, \dots, I_{n_P} , of respectively k_1, k_2, \dots, k_{n_P} degrees, and where $h_{j_1, j_2, \dots, j_k}(I_{j_l})$ denotes a vibrational operator which only depends upon operators acting on the degrees in subset I_{j_l} . Note that this condition is satisfied for all possible partitions with the Hamiltonian of Eq.(1).

(2) We have n_P basis sets of vibrational wave functions, $\phi_{I_j}^m(q_{i_1^j}, \dots, q_{i_{k_j}^j})_{m \in \{1, d_j\}}$, with $1 \leq j \leq n_P$, spanning the Hilbert subspaces of dimension d_j , of physical interest for the groups of degrees of freedom in the I_j 's.

Let Q be another partition coarser than or equal to P , that is to say:

$$Q = (J_1, J_2, \dots, J_{n_Q}), \quad \text{with } n_Q \leq n_P, \\ \text{and } \forall j \in \{1, \dots, n_P\}, \quad \exists k \in \{1, \dots, n_Q\} \quad \text{such that, } I_j \subseteq J_k \quad (16)$$

The subsets J_k are referred to as ‘‘contractions’’ whose components are the I_j 's such that $I_j \subseteq J_k$. The number of components in J_k is denoted by l_k .

A VMFCI calculation consists in defining for each contraction, J_k , a mean field Hamiltonian obtained by averaging the vibrational Hamiltonian in the

mean field of the other contractions $J_l \neq J_k$ and by diagonalizing it in a basis set of product functions,

$$\Phi_{J_k}^M = \prod_{I_j \subseteq J_k} \phi_{I_j}^{m_j}(q_{i_1^j}, \dots, q_{i_{k_j}^j}), \quad (17)$$

where the superlabel M stands for the sequence of indices m_j of the component functions.

More precisely, one first builds a partial Hamiltonian by gathering all the terms of H_{vib} that involve exclusively operators acting on the $I_j \subseteq J_k$,

$$\begin{aligned} H_k = h_0 + & \sum_{j_1 \text{ such that, } I_{j_1} \subseteq J_k} h_{j_1}(I_{j_1}) + \sum_{j_1 < j_2 \text{ such that, } I_{j_1}, I_{j_2} \subseteq J_k} h_{j_1, j_2}(I_{j_1}) h_{j_1, j_2}(I_{j_2}) + \\ \dots + & \sum_{j_1 < \dots < j_{i_k} \text{ such that, } I_{j_1}, \dots, I_{j_{i_k}} \subseteq J_k} h_{j_1, \dots, j_{i_k}}(I_{j_1}) \dots h_{j_1, \dots, j_{i_k}}(I_{j_{i_k}}). \end{aligned} \quad (18)$$

Then, one averages $H_{vib} - H_k$ over a given state, that we have chosen to be, in this work, the product of the ground states, $\prod_{I_j \not\subseteq J_k} \phi_{I_j}^0(q_{i_1^j}, \dots, q_{i_{k_j}^j})$, of all the components of the ‘‘spectator’’ contractions (that is to say, not in the contraction J_k). We obtain the mean-field Hamiltonian :

$$H_k + \left\langle \prod_{I_j \not\subseteq J_k} \phi_{I_j}^0(q_{i_1^j}, \dots, q_{i_{k_j}^j}) \middle| H_{vib} - H_k \middle| \prod_{I_j \not\subseteq J_k} \phi_{I_j}^0(q_{i_1^j}, \dots, q_{i_{k_j}^j}) \right\rangle. \quad (19)$$

This Hamiltonian is diagonalized in the basis set of all product functions of Eq.(17), or in a subset of the latter obtained by selecting the product functions such that the sum of the energies of their components is below a given threshold. Additionally, extra threshold can be applied to the energy of any component.

In contrast with the traditional contraction method [38–42], where the mean field term is omitted in Eq.(19), it is relevant to iterate a VMFCI calculation with the same partition, except of course in the VCI case corresponding to the partition, $(\{1, 2, \dots, n_{vib}\})$. This way, one can achieve a vibrational self-consistent field configuration interaction (VSCFCI) calculation. The simplest example is the VSCF case [43,44] corresponding to the partition $(\{1\}, \{2\}, \dots, \{n_{vib}\})$, iterated until a chosen convergence criterion is met.

In summary, the VMFCI scheme is a particularly general variational method. By carrying out a basis set truncation after such a calculation, one can systematically achieve a drastic reduction of the basis set size to be used in following

calculations, corresponding to possibly coarser partitions, without affecting the end result.

The efficiency of the mean field CI treatment is illustrated in Table 2 for the low-lying vibrational levels of methane, calculated as in our previous work [5] from the Lee, Martin, Taylor potential energy surface (PES) [45]. This table compares 3 different “minimal symmetry preserving” (MSP) calculations to a harmonic and a converged (see Table 13 of the supplementary material of [5]) calculations. Let us recall that MSP calculations actually consist in contracting degenerate components together, in order to ensure that no symmetry breaking occurs, (in contrast with VSCF calculations). For methane, such a calculation reduces the 9 modal basis sets to 4 product basis sets by contracting together the modals (i.e. vibrational one-degree of freedom functions) of the two components of the E mode and the modals of the three components of the two T2 modes, the remaining mode carries the A1 representation, so it is non degenerate. Each MSP calculation step then consists in 4 separate diagonalizations of the Hamiltonian matrix within the latter basis sets. So, their computational costs are in the same range. The MSP-CI, which corresponds to the standard contraction method without mean field treatment, only accounts for the intra-mode anharmonic coupling. It does not improve significantly the harmonic results for modes 1 and 2 and goes in the wrong direction for modes 3 and 4. Oppositely, MSP-VMFCI and MSP-VSCFCI calculations, which introduce the mean field averaging with and without iterating, provide significantly better results. MSP-VSCFCI results always go in the right direction, with modes 1 and 2 closer to the converged values than with MSP-CI. Therefore, mean field contracted wave functions provide an efficient basis set to be used in further contraction steps, which is not the case of the standard contracted wave functions. The conclusions drawn from this example have been verified in all other systems studied so far.

3 Performances, convergence, and comparison of P-VMWCI and VMFCI approaches. An interesting test molecule: ethylene monoxyde.

Identified in the interstellar medium, ethylene monoxyde has been the subject of numerous recent investigations [6–12]. Its IR spectrum has been studied by many authors in the gas phase [47,48,51,52], the liquid phase [47], the solid phase [49,50] and more recently in thin films and in amorphous water ice [12]. Assignment of some bands differs from a publication to another principally because of Fermi resonances between A_1 and B_1 modes, and because of the band vicinity in the 800-900 cm^{-1} area where are expected ring deformation and the CH_2 rocking and twisting modes. Up to now, only harmonic or scaled harmonic force fields [49,51,53,54] have been calculated at *ab initio*, DFT and semi-empirical levels of theory to support or validate the different experimental

assignments. However, none of these harmonic studies allows one to dispel experimental ambiguities.

In this work, we have used an anharmonic potential energy surface (PES) which combines CCSD(T)/cc-pVTZ equilibrium geometry and harmonic constants with B3LYP/6-31+G(d,p) cubic and quartic force constants [55,56]. The accurate results obtained in previous investigations on medium size systems [55,57] have validated this combined approach. Furthermore, our anharmonic force field was built by taking into account energies, gradients and even Hessians but only for selected distorted geometries [58,59]. All constants were deduced from our EGH code [58].

In the present study, we have mainly focused attention on the fundamental transition wave numbers. However, we have also paid attention to some specific overtones expected to show up in the region around 3000 cm^{-1} where the CH_2 stretching vibrations are observed. An exhaustive analysis of the complete spectrum is in progress and will be published elsewhere.

The convergence of the P-VMWCI method is assessed in Table 3. This table illustrates how crucial the choice of the vibrational configuration space, (determined by its order γ), is for the accuracy of the results in the P-VMWCI approach. Three iterations are at least needed in the construction of the configuration space (see ν_1 for example). This is because, on the one hand, the force constants linking the fundamental and harmonic first excited states to their overtones or to combination bands are not very strong. As a matter of fact, in our C_2H_4O anharmonic force field, it is uncommon to find constants that exceed 100 cm^{-1} . However, on the other hand, many overtones and combination bands turn out to be quasi-degenerate, so, in the present case, it is the $\gamma = 2$, indirectly interacting configurations, which bring the main contribution to the description of the fundamental transitions. The P-VMWCI results for $\gamma = 3$, (see Table 5 where they are repeated), are nearly the same as the converged VMFCI ones for all the targeted vibrational levels.

Table 4 reports the results obtained with the VMFCI approach. All calculations start with a VSCF calculation, (there is no degenerate mode, so it is the MSP-VMFCI calculation), which is converged to 10^{-6} cm^{-1} after 7 iterations. The first column of the table reports the results obtained from a VCI contracting the 15 modes together directly after the VSCF, an energy truncation at 8400 cm^{-1} being applied to the sum of VSCF modal energies. The VMFCI results reported in the other columns are all obtained by applying the following 4-step contraction scheme :VSCF/VSCFCI($\nu_1-\nu_6-\nu_9-\nu_{13}$, $\nu_3-\nu_5-\nu_{12}$; 34072, 17000)/VSCFCI($\nu_1-\nu_6-\nu_9-\nu_{10}-\nu_{13}-\nu_{15}$; 19464)/VCI(Z). The step following the VSCF calculation introduces a separate contraction of the CH stretching modes (ν_1 , ν_6 , ν_9 and ν_{13}) and of the ring modes (ν_3 , ν_5 , ν_{12}). These contractions were suggested by preliminary calculations based on the ZPE

lowering criterion [5]. More precisely, VMFCI calculations were performed for all possible binary (105) and ternary (456) contractions, and the results were sorted by decreasing order of the ZPE stabilization with respect to the corresponding VSCF value. The larger effects clearly occurred for binary (6.2 to 6.9 cm^{-1}) and ternary (12.9 to 14.9 cm^{-1}) contractions involving the CH stretching modes, suggesting to contract in priority these modes together. The importance of the ternary contraction of the ring modes also suggested to contract these modes together. Note that at this stage, contracted modes are calculated in the mean field of the others, and that truncation energy thresholds of 34072 and 17000 cm^{-1} are applied to the stretching and ring mode contractions respectively. After achieving self-consistency (only one more iteration is needed), we introduce two more modes (ν_{15} and ν_{10}) into the CH stretching contraction, applying an energy cut-off of 19464 cm^{-1} to the resulting contraction. Again, only two VMFCI steps are needed to reach self-consistency for this contraction. Introducing the CH_2 rocking mode ν_{15} is justified by the ZPE stabilization of about 9 cm^{-1} of ternary contractions in which ν_{15} is coupled with CH stretching modes. Addition of the CH_2 twisting mode ν_{10} comes from the comparison of the VCI(8400) and a VMFCI similar to the 4-step scheme above but without contracting the ν_{10} mode and with a truncation at 7700 cm^{-1} in the final step, showing that an energy inversion occurred between the ν_1 and the $2\nu_{10}$ energy levels, with an energy difference between the levels as large as $\pm 50 \text{ cm}^{-1}$. A further analysis of the $\nu_1 - \nu_{10}$ contraction showed that ν_1 is strongly mixed with $2\nu_{10}$ (found at 2959 cm^{-1} in our best calculation). Note that ν_{13} and $\nu_{15} + 2\nu_4$ (3045 cm^{-1}) exhibited a similar inversion but with a smaller energy splitting ($\pm 4 \text{ cm}^{-1}$) not justifying the inclusion of ν_4 into the ($\nu_1 - \nu_6 - \nu_9 - \nu_{10} - \nu_{13} - \nu_{15}$) contraction. The fourth and last step consists in a VCI including all modes, with a global energy truncation at Z cm^{-1} . Results collected in the four last columns of Table 4 obey to the contraction scheme just described, showing the convergence with Z ranging from 8400 to 10721 cm^{-1} . This scheme is clearly more effective than the direct VCI after the VSCF, as can be seen from the zero point energy (ZPE) convergence: 12501 for VCI(8400), 12464.5 for VMFCI(8400), then 12464 cm^{-1} for the other VMFCIs (12463.7 cm^{-1} for VMFCI(10721)) and by inspecting the stretching modes in Table 4. The convergence of the fundamental wave numbers with increasing Z values is clear. So, the ZPE convergence also means that the excited energy levels have converged to about 1 cm^{-1} accuracy.

We have reported in Table 5 the best values of the P-VMWCI and VMFCI approaches. They are tabulated along with the available experimental data. The results of the two theoretical methods are very similar, the mean deviation being smaller than 0.2% i.e. 3.5 cm^{-1} . The largest difference is found to be 6 cm^{-1} for the ν_{10} (σ_{CH_2}) and ν_{15} (ρ_{CH_2}) modes.

4 Conclusion

The convergence of the two independent, theoretical approaches indicates their reliability. It entitles us to claim that the accuracy of our theoretical wave number values are essentially that of the CCSD(T)/B3LYP//cc-pVTZ/6-31+G(d,p) PES.

On the ground of our theoretical wave number values, six points can be underlined:

- Both ν_6 and ν_{13} CH_2 asymmetric stretching modes are fairly well reproduced by our calculations (within 1% of the observed values). The gap calculated between the two modes (9 and 14 cm^{-1}) is in perfect agreement with the observed value (12 cm^{-1}) on ethylene oxide crystals [50], if the lowest (and most intense) wave numbers are retained. However, the sign of the gap is the opposite in the most recent experiment on thin ethylene oxide films deposited at low temperature [12] (-12 cm^{-1} for the amorphous phase and -15 cm^{-1} for the crystalline phase) .
- The CH_2 symmetric stretching vibrations ν_1 and ν_9 are calculated 110 to 130 cm^{-1} below the asymmetric ν_6 and ν_{13} modes in contrast with the experimental values. A large part of this gap (≈ 80 to 100 cm^{-1}) is already present at the harmonic level. A Morse function fit to our polynomial PES is probably needed to remedy to these discrepancies. Moreover, several strong, coupled bands are expected in this crowded area of the spectral range. Theoretical investigations are in progress to analyse in more detail this issue.
- A perturbative treatment of the CH_2 symmetric stretching vibrations not reported here, has led to 3061 and 3015 cm^{-1} for A_1 (ν_1) and B_1 (ν_9) modes respectively whereas the other wave numbers are close to the converged, variational values. These particular discrepancies of the perturbational approach have to be linked with the presence of strong interactions between cycle deformations and implying also hydrogen bending modes. Variational calculations involving all the states of the fundamental and combination bands located in the [500-10000] cm^{-1} area have revealed that the ν_1 and ν_9 fundamental bands are mainly mixed with the ($\nu_5 + \nu_7 + \nu_8$ and $\nu_5 + \nu_{11} + \nu_{12}$) A_1 overtones and the ($\nu_2 + \nu_{10}$, $2\nu_8 + \nu_{12}, \nu_{11} + 2\nu_{15}$) B_1 overtones respectively.
- All CH_2 scissoring, rocking, twisting and wagging vibrations belonging to A_1 , B_1 and B_2 symmetries, (i.e. infra-red active), are in very good agreement with experimental data.
- The ring breathing (ν_3) and the ring deformation (ν_5) respectively calculated at 1271-1272 cm^{-1} and 881-879 cm^{-1} are in perfect agreement with the

observed bands reported at 1270 and 877cm^{-1} in [49,51] for ethylene oxide in the gas phase; The last ring deformation ν_{12} computed at $820\text{-}823\text{cm}^{-1}$ supports Nakanaga's assignment (822cm^{-1} [51]) against the weak absorption bands between 840 and 892cm^{-1} assigned by many workers [47,49] to this vibration.

- The two A_2 CH_2 twisting (ν_7) and rocking (ν_8) modes inactive in the IR gas phase are calculated respectively at ($1149\text{-}1152\text{ cm}^{-1}$) and ($1019\text{-}1024\text{ cm}^{-1}$). This latter value in agreement with the estimated wavenumber (above about 1000cm^{-1}) from microwave spectroscopy [48] differs by about 200 cm^{-1} from all the other IR assignments [12,47,49–51]. In the same way, for the twisting mode (ν_7) the difference between our results and the other assignment is about 100 cm^{-1} , see for example the wave number suggested by Schriver *et al* [12] to characterize this mode in crystalline and amorphous phases.

ACKNOWLEDGEMENTS

The Pau group acknowledges the Centre Informatique National de l'Enseignement Supérieur (CINES) for support of this work. J. L. thanks the Fond National de la Recherche Scientifique (FNRS, contracts FRFC and IISN) and the "Action de Recherches Concertées de la Communauté française de Belgique" for financial support. P. C.-C. thanks Jean-Marc Lacroix for his help in taking the best advantage of the JAD laboratory computer facilities and acknowledges the french ANR (Projet AHBE) for fundings.

References

- [1] N. Gohaud, D. Bégué, C. Darrigan, C. Pouchan, *J. Comp. Chem.* **26**, 743-754 (2005).
- [2] D. Bégué, N. Gohaud, R. Brown, C. Pouchan, *J. Math. Chem.* **40**, 197 (2006).
- [3] P. Cassam-Chenaï and J. Liévin, *Int. J. Quantum Chem.* **93**, 245-264 (2003).
- [4] P. Cassam-Chenaï, *J. Quant. Spectrosc. Radiat. Transfer* **82**, 251-277 (2003).
- [5] P. Cassam-Chenaï, J. Liévin, *Journal of Computational Chemistry* **27**, 627-640 (2006).
- [6] J.E. Dickens, W.M. Irvine, M. Ohishi, M. Ikeda, S. Ishikawa, A. Nummelin and A. Hjalmarsen. *Astrophys. J.* **489**, 753 (1997).
- [7] A. Nummelin, J.E. Dickens, P. Bergman, A. Hjalmarsen, W.M. Irvine, M. Ikeda and M. Ohishi. *Astron. Astrophys.* **337**, 275 (1998).
- [8] J. Pan, S. Albert, K.V.L.N. Sastry, E. Herbst, F.C. de Lucia, *Astro. J.* **499**, 517 (1998).
- [9] M. Ikeda, M. Ohishi, A. Nummelin, J. E. Dickens, P. Bergman, Å. Hjalmarsen, and W. M. Irvine, *Astrophys. J.* **560**, 792 (2001).
- [10] M. Ikeda, M. Ohishi, A. Nummelin, J. E. Dickens, P. Bergman, Å. Hjalmarsen, and W. M. Irvine, *Astrophys. J.* **571**, 560 (2002).
- [11] S. Chandra. *Astron. Astrophys.* **402**, 1 (2003).
- [12] A. Schriver, J.M. Coanga, L. Schriver-Mazzuoli and P. Ehrenfreund, *Chem. Phys.* **303**, 13-25 (2004).
- [13] S. Carter and J. M. Bowman, in "Rovibrational Bound States in Polyatomic Molecules", M. M. Law, I. A. Atkinson and J. M. Hutson Eds., (CCP6, Daresbury, 1999), pp. 60-67.
- [14] K. M. Dunn, J. E. Boggs and P. Pulay, *J. Chem. Phys* **85**, 5838 (1986).
- [15] A. Niño and C. Muñoz-Caro, *Comp. Chem.* **19**, 371-378 (1995).
- [16] C. Muñoz-Caro and A. Niño, QCPE Program Number: 665
- [17] G. M. Chaban, J. O. Jung, R. B. Gerber, *J. Chem. Phys* **111**, 1823 (1999).
- [18] F. Gatti, C. Iung, C. Leforestier and X. Chapuisat, *J. Chem. Phys* **111**, 7236 (1999).
- [19] A. Viel and C. Leforestier, *J. Chem. Phys* **112**, 1212 (2000).
- [20] J.C. Light and T. Carrington, *Adv. Chem. Phys.* **114**, 263 (2000).
- [21] N. J. Wright, R. B. Gerber, *J. Chem. Phys* **114**, 8763 (2001).

- [22] N. Matsunaga, G. M. Chaban, R. B. Gerber, *J. Chem. Phys* **117**, 3541 (2002).
- [23] Hua-Gen Yu, *J. Chem. Phys* **121**, 6334 (2004).
- [24] Hee-Seung Lee and J. C. Light, *J. Chem. Phys* **120**, 4626 (2004).
- [25] F. Ribeiro, C. Iung, and C. Leforestier, *J. Chem. Phys* **123**, 54106 (2005).
- [26] R. Dawes and T. Carrington, *J. Chem. Phys* **122**, 134101 (2005).
- [27] L. B. Harding and W. C. Ermler, *J. Comp. Chem.* **6**, 13 (1985).
- [28] J. F. Gaw, A. Willets, W. H. Green and N. C. Handy, in *Advances in molecular vibrations and collision dynamics*, J. Bowman ed., (JAI Press, Greenwich, 1991).
- [29] W. Thiel, *Chimia Int. J. Chem.* **58**, 276 (2004).
- [30] V. Barone, G. Festa, A. Grandi, N. Rega and N. Sanna, *Chem. Phys. Lett.* **388**, 279-283 (2004).
- [31] V. Barone, *J. Chem. Phys* **122**, 14108 (2005).
- [32] E. J. Weniger, *Annals of Phys.* **246**, 133 (1996).
- [33] S. Brodersen and J.-E. Lolck, *J. Mol. Spectrosc.* **126**, 405-426 (1987).
- [34] C. Pouchan and K. Zaki, *J. Chem. Phys* **107**, 342 (1997).
- [35] I. Baraille, C. Larrieu, A. Dargelos, M. Chaillet, *Chem. Phys.* **273**, 91 (2001).
- [36] O. Christiansen, *J. Chem. Phys* **120**, 2149 (2004).
- [37] D. Bégué, S. Elissalde, E. Péré, P. Iratçabal, C. Pouchan, *J. Phys. Chem.* **A110**, 7793 (2006).
- [38] B. Maessen and M. Wolfsberg, *J. Phys.* **89**, 3876 (1985).
- [39] C. L. Chen, B. Maessen, and M. Wolfsberg, *J. Chem. Phys* **83**, 1795 (1985).
- [40] J. Tennyson, *Comp. Phys. Rep.* **4**, 1 (1986).
- [41] S. Carter and N. C. Handy, *Comp. Phys. Rep.* **5**, 15 (1986).
- [42] Z. Bačić and J. C. Light, *Annu. Rev. Phys. Chem.* **40**, 469 (1989).
- [43] G. D. Carney, L. L. Sprandel and C. W. Kern in "Advances in Chemical Physics", Vol. 37, I. Prigogine and S.A. Rice, Eds., (Wiley, New York, 1978), pp. 305-379.
- [44] R. B. Gerber and M. A. Ratner, *Chem. Phys. Lett.* **68**, 195 (1979).
- [45] T. J. Lee, J. M. L. Martin and P. R. Taylor, *J. Chem. Phys* **102**, 254 (1995).
- [46] R. Burcl, S. Carter, N. C. Handy, *Chem. Phys. Lett.* **373**, 357-365 (2003).
- [47] R.C. Lord, B. Nolin, *J. Chem. Phys* **24**, 656 (1956). And refs. therein to earlier works.

- [48] N. Yoshimizu, C. Hirose, S. Maeda, *Bull. Chem. Soc. Jap.* **48**, 3529 (1975).
- [49] N.W. Cant, W.J. Armstead, *Spectrochimica Acta* **A31**, 839 (1975).
- [50] J.E. Bertie, S.M. Jacobs, *J. Chem. Phys* **68**, 97 (1978).
- [51] T. Nakanaga, *J. Chem. Phys* **73**, 5451 (1980). And refs. therein to earlier works.
- [52] T. Nakanaga, *J. Chem. Phys* **74**, 5384 (1981).
- [53] M.A. Lowe, J.S. Alper, R. Kawiecki, P.J. Stephens, *J. Phys. Chem.* **90**, 41 (1986).
- [54] K. Frimand, K.J. Jalkanen, *Chem. Phys.* **279**, 161 (2002).
- [55] D. Bégué, Ph. Carbonnière, C. Pouchan, *J. Phys. Chem.* **A109**, 4611 (2005).
- [56] A.D. Boese, W. Klopper, J.M.L. Martin, *Int. J. Quantum Chem.* **104**, 830 (2005).
- [57] P. Carbonniere, T. Lucca, C. Pouchan, N. Rega, V. Barone, *J. Comp. Chem.* **384**, 26 (2005).
- [58] P. Carbonnière, D. Bégué, A. Dargelos, C. Pouchan, *Chem. Phys.* **300**, 41 (2004).
- [59] R. Dawes, D.L. Thompson, Y. Guo, A.F. Wagner, M. Minkoff, *J. Chem. Phys* **126**, 184108 (2007).

List of Figure captions

Figure 1: Schematic representation of ethylene oxide.

γ	[3500]			[1]		
	S_γ ^a	N_{op} ^b	ν_{CO}	S_γ ^a	N_{op} ^b	ν_{CO}
0	18(0.1)	–	1781.2	2	–	1781.2
1	976(3.3)	7913	1754.8	336(1.1)	768	1755.2
2	6610(22.3)	554004	1750.8	3449(11.6)	180376	1750.9
3	17783(59.9)	3981840	1750.2	12526(42.2)	2062647	1750.4
4	26737(90.1)	10608135	1750.0	23329(78.6)	7550757 ^c	1750.2

Table 1

Comparison of P-VMWCI approach performances considering two spectral windows with a decreasing density of states : Illustration with the ν_{CO} stretching mode of the H_2CO molecule, obtained from a potential function computed at the CCSD(T)/cc-pVQZ level of theory [37]. The [3500] window, which covers the 0-3500 cm^{-1} spectral area, is initially composed of 18 configurations. The second window, namely the [1] window, is 1 cm^{-1} wide around the perturbational value of the ν_{CO} wave number and only contains the ν_{CO} wave function (plus the ground state). Considering a reduced-sized window enables to have 25% operations less. This also reduces the problem size by 12% and CPU needs by 50%. Accuracy for the ν_{CO} mode is equal to 0.17 cm^{-1} when $\gamma = 4$.

^a Size of the variational matrix at step γ . Values in parenthesis are the percentage of configurations contained in S_γ with respect to the total number $N = 29680$ of configurations; N corresponds to 7 excitation quanta for the τ_{CH_2} and ν_{CH_2} modes, and 6 excitation quanta for the ρ_{CH_2} , σ_{CH_2} , ν_{CO} and ν_{asCH_2} modes. The P-VMWCI automatically rejects configurations which do not meet these criteria.

^b The N_{op} column displays the number of operations required by the action of the operators in A to build the configuration space of step γ .

	Harmonic level	MSP-CI	MSP-VMFCI	MSP-VSCFCI	Converged
ν_4	1345	1356	<i>1295</i>	<i>1318</i>	1309
ν_2	1570	<i>1567</i>	<i>1527</i>	<i>1532</i>	1528
$2\nu_4$	2691	2714	<i>2591</i>	<i>2638</i>	2588
$2\nu_4$	2691	2719	<i>2597</i>	<i>2643</i>	2610
$2\nu_4$	2691	2719	<i>2597</i>	<i>2643</i>	2622
ν_1	3036	<i>3013</i>	<i>2972</i>	<i>2972</i>	2925
ν_3	3157	3214	3176	<i>3062</i>	3027
$2\nu_2$	3141	<i>3131</i>	<i>3051</i>	<i>3061</i>	3051
$2\nu_2$	3141	<i>3134</i>	<i>3054</i>	<i>3064</i>	3054
$3\nu_4$	4036	4079	<i>3896</i>	<i>3966</i>	3868
$3\nu_4$	4036	4087	<i>3905</i>	<i>3974</i>	3905
$3\nu_4$	4036	4088	<i>3905</i>	<i>3974</i>	3915
$3\nu_4$	4036	4088	<i>3906</i>	<i>3974</i>	3929
$3\nu_2$	4711	<i>4694</i>	<i>4573</i>	<i>4588</i>	4573
$3\nu_2$	4711	<i>4699</i>	<i>4579</i>	<i>4594</i>	4579
$3\nu_2$	4711	<i>4699</i>	<i>4579</i>	<i>4594</i>	4579

Table 2

Contraction methods with and without mean field averaging. The wave numbers in cm^{-1} of the vibrational levels of methane are tabulated for different minimal symmetry preserving (MSP) methods (i.e. methods which contract degenerate components together, otherwise the symmetry is broken [46]). MSP-CI, which correspond to the traditional contraction method goes in the wrong direction for modes 3 and 4, that is in half of the cases. MSP-VSCFCI always go in the right direction and modes 1 and 2 are closer to the converged value than with MSP-CI. (HO modal basis set with quantum number less than in 10 all MSP calculations. The Lee, Martin, Taylor PES was used [45]).

	Assignment	P-VMWCI		
		$\gamma = 1$	$\gamma = 2$	$\gamma = 3$
A_1	ν_1	3056	2977	2922
	ν_2	1502	1501	1499
	ν_3	1272	1272	1271
	ν_4	1136	1136	1120
	ν_5	882	881	881
A_2	ν_6	3042	3032	3027
	ν_7	1157	1154	1152
	ν_8	1026	1025	1024
B_1	ν_9	3012	2912	2908
	ν_{10}	1474	1474	1474
	ν_{11}	1131	1131	1130
	ν_{12}	824	822	820
B_2	ν_{13}	3057	3046	3041
	ν_{14}	1152	1151	1151
	ν_{15}	802	801	800

Table 3

Convergence of the P-VMWCI scheme. Fifteen minimal ($\pm 1\text{cm}^{-1}$ around each selected wave number) initial windows are used for the calculation of the fundamental wave numbers. Every tensor product of HO modals up to $n_s = 7$ for each mode s has been included in the iterative selection process. At order $\gamma = 3$, the VCI matrices have a size of about 50000×50000 . They have been diagonalized by a recently implemented block-Davidson algorithm.

	Assignment	VSCF/VCI(8400) (42113bf)	VMFCI(8400) (46525bf)	VMFCI(9200) (91052bf)	VMFCI(10000) (172204bf)	VMFCI(10721) (298194bf)
A_1	ν_1^a	2994	2927	2921	2920	2919
	ν_2	1501	1500	1500	1497	1497
	ν_3	1273	1274	1273	1271	1272
	ν_4	1128	1128	1126	1123	1123
	ν_5	881	881	879	879	879
A_2	ν_6	3093	3040	3034	3033	3032
	ν_7	1153	1153	1151	1149	1149
	ν_8	1024	1024	1020	1019	1019
B_1	ν_9	3040	2922	2915	2914	2913
	ν_{10}	1473	1471	1471	1468	1468
	ν_{11}	1130	1130	1128	1125	1125
	ν_{12}	825	825	823	823	823
B_2	ν_{13}^a	3105	3052	3044	3042	3041
	ν_{14}	1151	1151	1149	1147	1147
	ν_{15}	801	796	794	793	794

Table 4

Convergence of the VMFCI scheme with the final step truncation threshold: the VMFCI(Z) scheme used in this study is: VSCF/VSCFCI(ν_1 - ν_6 - ν_9 - ν_{13} , ν_3 - ν_5 - ν_{12} ; 34072, 17000)/VSCFCI(ν_1 - ν_6 - ν_7 - ν_9 - ν_{10} - ν_{13} ; 19464)/VCI(Z), that is to say, after a VSCF, the CH stretching modes, ν_1 , ν_6 , ν_9 , ν_{13} , have been contracted together in the mean field of the other modes with a truncation threshold on the sum of the energies of product basis function components equal to 34072 cm^{-1} , at the same step the ring modes, ν_3 , ν_5 , ν_{12} , have been contracted together with a truncation threshold of 17000 cm^{-1} ; after achieving self-consistency (only one more iteration was needed) the CH stretching modes have been contracted with ν_7 (CH_2 twist) and ν_{10} (CH_2 scissor) with truncation of the basis set at 19464 cm^{-1} (self-consistency achieved in two steps); finally, all the modes were contracted with truncation at $Z \text{ cm}^{-1}$. This scheme proved more effective than the direct VCI after the VSCF.

^a In the VMFCI calculations ν_1 was strongly mixed with $2\nu_{10}$ (2959 cm^{-1}), and ν_{13} with $\nu_{15} + 2\nu_4$ (3045 cm^{-1}), so that, our assignment is only indicative.

Assignment		Gaz phase		Liquid phase	Solid Phase			Computed		type of motion
		IR		Raman	amorphous	crystalline		P-VMWCI	VMFCI	
		[51]	[49]	[47]	[12]	[50]	[12]			
A_1	ν_1	-	3018	3005	3011	3024	3005	2922	2919	ν_{s,CH_2}
	ν_2	1497	1498	1490	1492	1481-1495	-	1499	1497	σ_{CH_2}
	ν_3	1270	1270	1266	1267	1266-1268	1266	1271	1272	Ring breath.
	ν_4	-	1148	1120	-	1119-1129	1147	1120	1123	ω_{CH_2}
	ν_5	877	877	867	856	857-875	854	881	879	Ring deform.
A_2	ν_6	-	ia	3063	3073	3050-3051	3073	3027	3032	ν_{as,CH_2}
	ν_7	ia	ia	(1345)	1043	1043-1046	1046	1152	1149	τ_{CH_2}
	ν_8	1020 ^a	ia	807	821	837-851	818	1024	1019	ρ_{CH_2}
B_1	ν_9	-	3006	3005	3001	2996-3006	2995	2908	2913	ν_{s,CH_2}
	ν_{10}	1470	1472	-	1467	1455-1467	1467	1474	1468	σ_{CH_2}
	ν_{11}	-	1151	1150	1169	1159-1169	1152	1130	1125	ω_{CH_2}
	ν_{12}	822	840	867	-	816-825	859	820	823	Ring deform.
B_2	ν_{13}	3065	3065	3063	3061	3062-3075	3058	3041	3041	ν_{as,CH_2}
	ν_{14}	-	1142	1150	-	1146-1161	1160	1151	1147	τ_{CH_2}
	ν_{15}	808	821	-	794	794-798	796	800	794	ρ_{CH_2}

Table 5

Experimental and calculated wavenumbers (in cm^{-1}) for the ethylene oxide compound. ia: inactive, ν_s : symmetrical stretching, ν_{as} : asymmetrical stretching, ρ : rocking, σ : scissoring, τ : twisting, ω : wagging, breath.: breathing, deform.: deformation.

^a From ref.[48] according to [51]. Actually Yoshimizu et al. [48] assigned this wave number to ν_7 , however their results support a value for ν_8 above about 1000 cm^{-1}

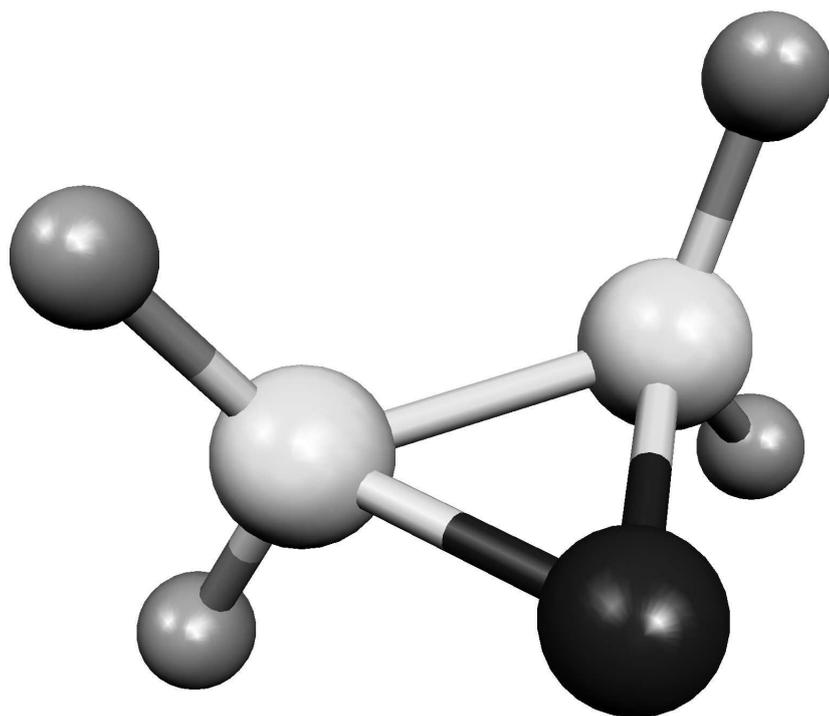


Figure 1. Bégué, Journal of Chemical Physics