

Structural relaxation around substitutional Cr³⁺ in MgAl₂O₄

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The structural environment of substitutional Cr³⁺ ion in MgAl₂O₄ spinel has been investigated by Cr K-edge Extended X-ray Absorption Fine Structure (EXAFS) and X-ray Absorption Near Edge Structure (XANES) spectroscopies. First-principles computations of the structural relaxation and of the XANES spectrum have been performed, with a good agreement to the experiment. The Cr-O distance is close to that in MgCr₂O₄, indicating a full relaxation of the first neighbors, and the second shell of Al atoms relaxes partially. These observations demonstrate that Vegard's law is not obeyed in the MgAl₂O₄-MgCr₂O₄ solid solution. Despite some angular site distortion, the local D_{3d} symmetry of the B-site of the spinel structure is retained during the substitution of Cr for Al. Here, we show that the relaxation is accommodated by strain-induced bond buckling, with angular tilts of the Mg-centred tetrahedra around the Cr-centred octahedron. By contrast, there is no significant alteration of the angles between the edge-sharing octahedra, which build chains aligned along the three four-fold axes of the cubic structure.

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I. INTRODUCTION

Most multicomponent materials belong to complete or partial solid solutions. The presence of chemical substitutions gives rise to important modifications of the physical and chemical properties of the pure phases. For instance, the addition of a minor component can improve significantly the electric, magnetic or mechanical behaviour of a material.^{1,2,3} Another evidence for the presence of impurities in crystals comes from the modification of optical properties such as coloration. Transition metal ions like Cr³⁺ cause the coloration of wide band gap solids, because of the splitting of 3*d*-levels under the action of crystal field.⁴ Despite the ubiquitous presence of substitutional elements in solids, their accommodation processes and their structural environment are still discussed,⁵ since they have important implications. For example, the interpretation of the color differences between Cr-containing minerals (e.g. ruby, emerald, red spinel) requires to know the structural environment of the coloring impurity.^{4,6,7,8} The ionic radius of a substitutional impurity being usually different from that of the substituted ion, the accommodation of the mismatch imposes a structural relaxation of the crystal structure. Vegard's law states that there is a linear relationship between the concentration of a substitutional impurity and the lattice parameters, provided that the substituted cation and impurity have similar bonding properties. Chemically selective spectroscopies, like Extended X-ray Absorption Fine Structure (EXAFS), have provided evidence that diffraction studies of solid solutions give only an average vision of the microscopic states and

that Vegard's law is limited.^{9,10,11} Indeed, a major result concerns the existence of a structural relaxation of the host lattice around the substitutional cation. This implies the absence of modification of the site occupied by a doping cation, when decreasing its amount in a solid solution. This important result has been observed in various materials, including III-V semi-conductors or mixed salts:^{12,13} e. g., in mixed alkali halides, some important angular buckling deviations have been observed.¹³ Recently, the use of computational tools, as a complement of EXAFS experiments, has been revealed successful for the study of oxide/metal epilayers.¹⁴ In oxides containing dilute impurities, this combined approach is mandatory. It has been recently applied to the investigation of the relaxation process around Cr dopant in corundum: in the α -Al₂O₃ - α -Cr₂O₃ system, the radial relaxation was found to be limited to the first neighbors around Cr, while the angular relaxation is weak.^{8,15}

In this work, we investigate the relaxation caused by the substitution of Al³⁺ by Cr³⁺ in spinel MgAl₂O₄, which gives rise to a solid solution, as observed for corundum α -Al₂O₃. The spinel MgAl₂O₄ belongs to an important range of ceramic compounds, which has attracted considerable interest among researchers for a variety of applications, great electrical, mechanical, magnetic and optical properties.¹⁶ The spinel structure is based on a cfc close-packing, with a Fd $\bar{3}$ m space group symmetry. Its chemical composition is expressed as AB₂X₄, where A and B are tetrahedral and octahedral cations, respectively, and X is an anion. These two types of cations define two different cationic sublattices, which may induce a very different relaxation process than in corundum. In the normal spinel structure, the octahedra host

trivalent cations and exhibit D_{3d} site symmetry. This corresponds to a small distortion along the [111] direction, arising from a departure of the position of oxygen ligands from a cubic arrangement. Small amounts of chromium oxide improve the thermal and mechanical properties of spinel.¹ A color change from red to green is also observed with increasing Cr-content. In this article, we report new results on the local geometry around Cr^{3+} in spinel $MgAl_2O_4$, using a combination of EXAFS and X-ray Absorption Near Edge Structure (XANES). The experimental data are compared to those obtained by theoretical calculations, based on the Density Functional Theory in the Local Spin Density Approximation (DFT-LSDA): this has enabled us to confirm the local structure around substitutional Cr^{3+} and investigate in detail the radial and angular aspects of the relaxation.

The paper is organized as follows. Section II is dedicated to the methods, including the sample description (Sec. II A), the X-ray absorption measurements and analysis (Sec. II B), and the computational details (Sec. II C). Section III is devoted to the results and discussion. Conclusions are given in Sec. IV.

II. MATERIALS AND METHODS

A. Sample description

Two natural gem-quality red spinel single crystals from Mogok, Burma (Cr-1, Cr-2) were investigated. They contain respectively 70.0, 71.4 wt % Al_2O_3 , 0.70, 1.03 wt% Cr_2O_3 and 26.4, 25.3 wt% MgO . These compositions were analyzed using the Cameca SX50 electron microprobe at the CAMPARIS analytical facility of the Universities of Paris 6/7, France. A 15 kV voltage with a 40 nA beam current was used. X-ray intensities were corrected for dead-time, background, and matrix effects using the Cameca ZAF routine. The standards used were $\alpha-Al_2O_3$, $\alpha-Cr_2O_3$ and MgO .

B. X-ray Absorption Spectroscopy measurements and analysis

Cr K-edge (5989 eV) X-ray Absorption Spectroscopy (XAS) spectra were collected at room temperature at beamline BM30b (FAME), at the European Synchrotron Radiation Facility (Grenoble, France) operated at 6 GeV. The data were recorded using the fluorescence mode with a Si (111) double crystal and a Canberra 30-element Ge detector.¹⁷ We used a spacing of 0.1 eV and of 0.05 \AA^{-1} , respectively in the XANES and EXAFS regions. Data treatment was performed using ATHENA following the usual procedure and the EXAFS data were analyzed using IFEFFIT, with the support of ARTEMIS.¹⁸ The details of the fitting procedure can be found elsewhere.¹⁹ An uvarovite garnet, $Ca_3Cr_2Si_3O_{12}$, was used as model compound to derive the value of the amplitude reduction

factor S_0^2 (0.81) needed for fitting. For each sample, a multiple-shell fit was performed in the q-space, including the first four single scattering paths: the photoelectron is backscattered either by the first (O), second (Al or Cr), third (O) or fourth (Mg) neighbors. Treating identically the third and fourth paths, we used a unique energy shift Δe_0 for all paths, three different path lengths R and three independent values of the Debye-Waller factor σ^2 . In a first step, the number of neighbors N was fixed to the path degeneracy. In a second time, a single amplitude parameter was fitted for the last three shells, assuming a proportional variation of the number of atoms on each shell.

C. Computations

1. Structural relaxation

In order to complement the structural information from EXAFS, a simulation of the structural relaxation was performed to quantify the geometric surrounding around an isolated Cr^{3+} . The calculations were done in a neutral supercell of $MgAl_2O_4$, using a first-principles total energy code based on DFT-LSDA.²⁰ We used Plane Wave basis set and norm conserving pseudopotentials²¹ in the Kleiman Bylander form.²² For Mg, we considered $3s$, $3p$, $3d$ as valence states (core radii of 1.05 a.u., $\ell=2$ taken as local part) and those of Ref.15 for Al, Cr, O. We first determined the structure of bulk $MgAl_2O_4$. We used a unit cell, which was relaxed with $2 \times 2 \times 2$ k -point grid for electronic integration in the Brillouin Zone and cut-off energy of 90 Ry. We obtained a lattice constant of 7.953 \AA and an internal parameter of 0.263 (respectively -1.6 % and +0.3 % relative to experiment),²³ which are consistent with previous calculations.¹⁶ In order to simulate the Cr defect, we used a $2 \times 2 \times 2$ supercell, built using the relaxed positions of the pure phase. It contains 1 neutral Cr, 31 Al, 16 Mg and 64 O atoms. It was chosen large enough to minimize the interaction between two paramagnetic ions, with a minimal Cr-Cr distance of 11.43 \AA . While the size of the supercell is kept fixed, all atomic positions are relaxed in order to investigate long-range relaxation. We used the same cut-off energy and a single k -point sampling. The convergence of the calculation was verified by comparing it to a computation with a $2 \times 2 \times 2$ k -point grid, and discrepancies in the atomic forces are lower than 0.3 mRy/a.u. In order to compare directly the theoretical bond distances to those obtained by EXAFS spectroscopy, the initial slight underestimation of the lattice constant (systematic within the LDA)²⁴ was removed by rescaling the lattice parameter by -1.6 %. This rescaling is homothetic and does not affect the relative atomic positions.

2. XANES simulations

As the analysis of the experimental XANES data is not straightforward, *ab initio* XANES simulations are required to relate the experimental spectral features to the local structure around the absorbing atom. The method used for XANES calculations are described in Ref. 25,26. The all-electron wave-functions are reconstructed within the projector augmented wave framework.²⁷ In order to allow the treatment of large systems, the scheme uses a recursion method to construct a Lanczos basis and then compute the cross section as a continued fraction.^{28,29} The XANES spectrum is calculated in the electric dipole approximation, using the same first-principles total energy code as the one used for the structural relaxation. It was carried out in the relaxed $2 \times 2 \times 2$ supercell (i.e 112 atoms), which contains one Cr atom and results from *ab initio* energy minimization mentioned in the previous subsection. The pseudopotentials used are the same as those used for structural relaxation, except for Cr. Indeed, in order to take into account the core-hole effects, the Cr pseudopotential is generated with only one $1s$ electron. Convergence of the XANES calculation is reached for the following parameters: a 70 Ry energy cut-off for the plane-wave expansion, one k -point for the self-consistent spin-polarized charge density calculation, and a Monkhorst-Pack grid of $3 \times 3 \times 3$ k -points in the Brillouin Zone for the absorption cross-section calculation. The continued fraction is computed with a constant broadening $\gamma=1.1$ eV, which takes into account the core-hole lifetime.³⁰

III. RESULTS AND DISCUSSION

Figure 1 shows the k^3 -weighted experimental EXAFS signals for Cr-1 and Cr-2 samples and the Fourier Transforms (FT) for the k -range 3.7 - 11.9 \AA^{-1} . The similarities observed suggest a close environment for Cr in the two samples (0.70 and 1.03 wt%-Cr₂O₃), which is confirmed by fitting the FT in the R -range 1.0 - 3.1 \AA (see Table I). The averaged Cr-O distance derived from EX-

TABLE I: Structural parameters obtained from the EXAFS analysis in the R range $[1.0$ - $3.1 \text{ \AA}]$ for Cr-1 and Cr-2 samples. The energy shifts Δe_0 were found equal to 1.3 ± 1.5 eV. The obtained RF factors were 0.0049 and 0.0045.

	$R(\text{\AA})$	N	$\sigma^2 (\text{\AA}^2)$	
Cr-O	1.98	6.0	0.0031	Cr-1
	1.98	6.0	0.0026	Cr-2
Cr-Al	2.91	5.3	0.0032	Cr-1
	2.91	5.4	0.0033	Cr-2
Cr-O	3.39	1.8	0.0079	Cr-1
	3.37	1.8	0.0077	Cr-2
Cr-Mg	3.39	5.3	0.0079	Cr-1
	3.39	5.4	0.0077	Cr-2

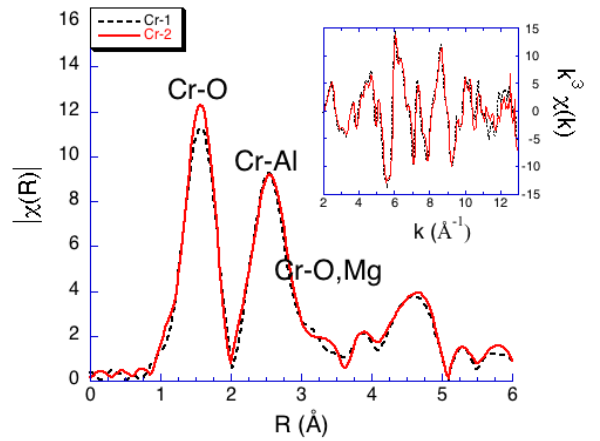


FIG. 1: Fourier-transform of k^3 -weighted EXAFS function for Cr-1 and Cr-2 samples (dashed and solid lines respectively). Inset: background-subtracted data

AFS data is equal to $1.98 \text{ \AA} (\pm 0.01 \text{ \AA})$, with six oxygen first neighbors. The second shell is composed of six Al atoms, located at $2.91 \text{ \AA} (\pm 0.01 \text{ \AA})$. Two oxygen and six magnesium atoms compose the further shells, at distances of 3.38 \AA and $3.39 \text{ \AA} (\pm 0.03 \text{ \AA})$. We investigated in detail the chemical nature of these second neighbors, by fitting the second peak on the FT (2.0 - 3.1 \AA) with either a Cr or an Al contribution, this latter corresponding to a statistical Cr-distribution (Cr/Al ~ 0.01). The only satisfactory fits were obtained in the latter case (Fig. 2).

Calculated and experimental interatomic distances are in good agreement (Table II), a confirmation of the EXAFS-derived radial relaxation around Cr³⁺ after substitution. The symmetry of the relaxed Cr-site is retained from the Al-site in MgAl₂O₄ and is similar to the Cr-site in MgCr₂O₄. It belongs to the D_{3d} point group, with an inversion center, three binary axes and a C_3 axis (Fig. 3a). This result is consistent with optical absorption³¹ and Electron-Nuclear Double Resonance experiments³² performed on MgAl₂O₄: Cr³⁺. Our first-principles calculations also agree with a previous investigation of the first shell relaxation, using Hartree-Fock formalism on an isolated cluster.³³ As it has been mentioned previously, the simulation can provide complementary distances (Fig. 3b): the Al1-O distances, equal to 1.91 \AA , are slightly smaller than Al-O distances in MgAl₂O₄. The Al1-Al2 distances are equal to 2.85 \AA , which is close to the Al-Al distances in MgAl₂O₄.

Apart from the radial structural modifications around Cr, significant angular deviations are observed in the doped structure. Indeed, the Cr-centred octahedron is slightly more distorted in MgAl₂O₄: Cr³⁺, with six O-Cr-O angles of 82.1° (and six supplementary angles of 97.9°): O-Cr-O is more acute than O-Cr-O in MgCr₂O₄ (84.5° , derived from refined structure)³⁴ and than O-Al-O in MgAl₂O₄ (either calculated in the present work, 83.5° , or derived from refined structure, 83.9°) (Fig. 3a). At a local scale around the dopant, the sequence of edge-

TABLE II: First, second and third neighbor mean distances (in Å) from central M^{3+} in the different structures considered in this work.

	MgAl ₂ O ₄ : Cr ³⁺ exp	MgAl ₂ O ₄ : Cr ³⁺ calc	MgAl ₂ O ₄ exp ^a	MgCr ₂ O ₄ exp ^b
Cr-O	1.98	1.99	—	1.99
Al-O	—	—	1.93	—
Cr-Al	2.91	2.88	—	—
Cr-Cr	—	—	—	2.95
Al-Al	—	—	2.86	—
Cr-O	3.37	3.34	—	3.45
Al-O	—	—	3.34	—
Cr-Mg	3.39	3.36	—	3.45
Al-Mg	—	—	3.35	—

^afrom Ref.23

^bfrom Ref.34

sharing octahedra is hardly modified by the substitution (Fig. 3b): the Cr-O-Al angles (95.1°) are similar to Cr-O-Cr in MgCr₂O₄ (95.2°) and Al-O-Al in MgAl₂O₄

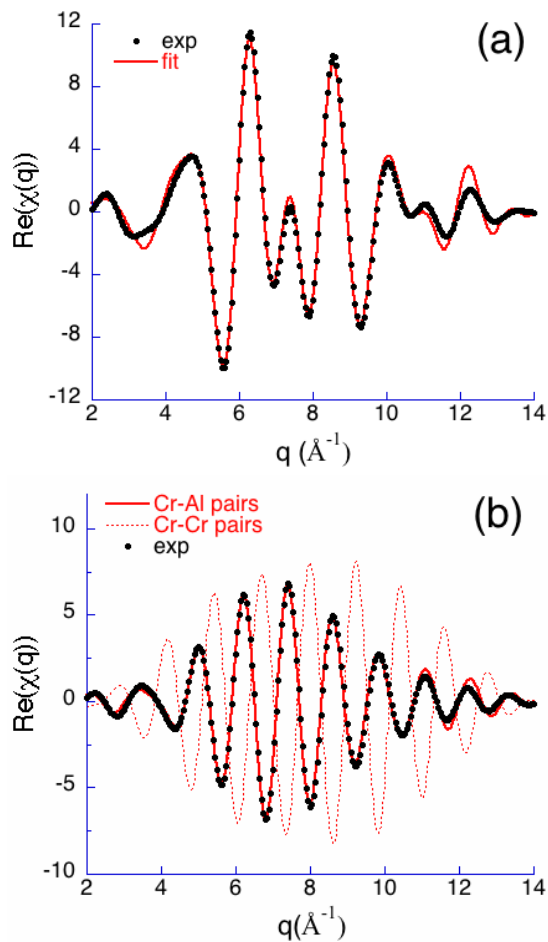


FIG. 2: (a) Inverse-FT of EXAFS data (dots) and fitted signal (solid line) for $R=1.0-3.1$ Å. (b) Inverse-FT of EXAFS data (dots) for $R=2.0-3.1$ Å, multi-shell fit with Cr-Al pairs (solid line) and theoretical function with Cr-Cr pairs (dashed line) in the same structural model.

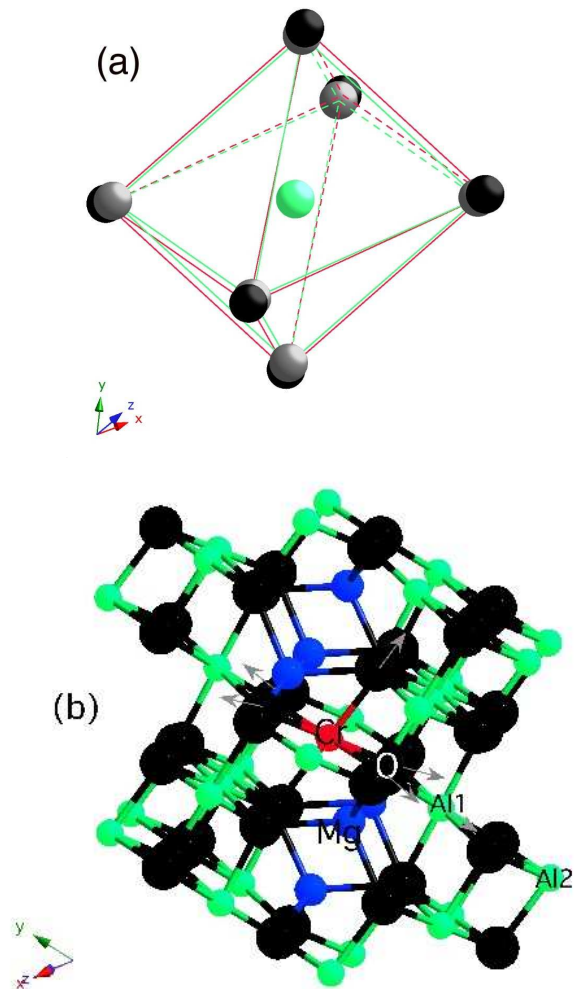


FIG. 3: (color online) (a) Cr-centred octahedron before relaxation (green) and after (red). (b) Model of structural distortions around Cr (red) in MgAl₂O₄: Cr³⁺. The O first neighbors (black) and the Al1 (green) second neighbors are displaced outward the Cr dopant in the direction of arrows.

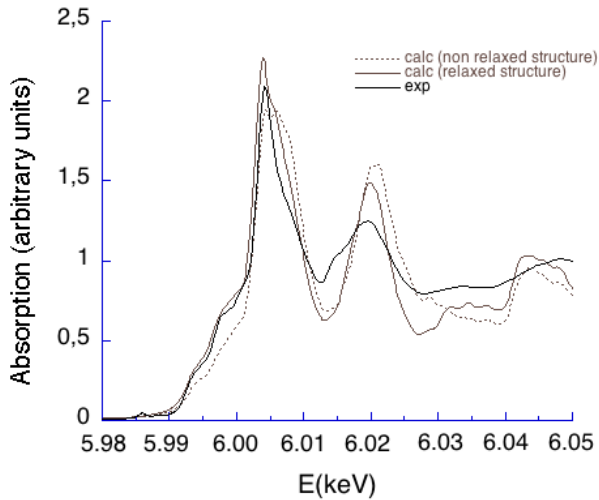


FIG. 4: Cr K-edge XANES spectra in $\text{MgAl}_2\text{O}_4: \text{Cr}^{3+}$. The experimental signal (thick line) is compared with the theoretical spectra calculated in the relaxed structure (solid line) and in the non-relaxed structure (dotted line)

(95.8°). However, the six Al-centred octahedra connected to the Cr-octahedron are slightly distorted (with six O-Al-O angles of 86.7°), compared to O-Cr-O angles in MgCr_2O_4 (84.5°) and O-Al-O angles in MgAl_2O_4 (83.9°). This modification affects in a similar way the three types of chains composed of edge-sharing octahedra, in agreement with the conservation of the C_3 axis. On the contrary, the relative tilt angle between the Mg-centred tetrahedra and the Cr-centred octahedron is very different in $\text{MgAl}_2\text{O}_4: \text{Cr}^{3+}$ (with Cr-O-Mg angle of 117.4°) than in MgCr_2O_4 and MgAl_2O_4 (with respectively, Cr-O-Mg and Al-O-Mg angles of 124.5° and 121.0°)

The experimental XANES spectrum of natural $\text{MgAl}_2\text{O}_4: \text{Cr}^{3+}$ is shown in Fig. 4. It is similar to that of a synthetic Cr-bearing spinel.³⁵ A good agreement with the one calculated from the ab initio relaxed structure is obtained, particularly in the edge region: the position, intensity and shape of the strong absorption peak (peak c) is well reproduced by the calculation. The small features (peaks a and b) exhibited at lower energy are also in good agreement with the experimental ones. In our calculation, the pre-edge features (visible at 5985 eV on the experimental data) cannot be reproduced, since we only considered the electric dipole contribution to the X-ray absorption cross-section: indeed, as it has been said previously, the Cr-site is centrosymmetric in the relaxed structure, which implies that the pre-edge features are due to pure electric quadrupole transitions. The sensitivity of the XANES calculation to the relaxation is evaluated by computing the XANES spectrum for the non-relaxed supercell, in which one Cr atom substitutes an Al atom in its exact position. The result is plotted in Fig. 4: the edge region (peaks a, b and c) is clearly not as well reproduced as in the relaxed model, and peak e is not visible at all. Therefore, we can conclude that the

structural model obtained from our ab initio relaxation is reliable.

The Cr-O distance is larger than the Al-O distance in MgAl_2O_4 , but is similar to the Cr-O distance in MgCr_2O_4 (Table II). This demonstrates the existence of an important structural relaxation around the substitutional Cr^{3+} ion, which is expected since Cr^{3+} has a larger ionic radius than Al^{3+} (0.615 \AA vs 0.535 \AA).³⁶ The size mismatch generates indeed a local strain, which locally expands the host structure. As a result, the O atoms relax outward the Cr defect. This radial relaxation is accompanied with a slight angular deviation of the O first neighbors, as compared to the host structure. The magnitude of the radial relaxation may be quantified by a relaxation parameter ζ , defined by the relation:¹⁰

$$\zeta = \frac{R_{\text{Cr-O}}(\text{MgAl}_2\text{O}_4: \text{Cr}^{3+}) - R_{\text{Al-O}}(\text{MgAl}_2\text{O}_4)}{R_{\text{Cr-O}}(\text{MgCr}_2\text{O}_4) - R_{\text{Al-O}}(\text{MgAl}_2\text{O}_4)} \quad (1)$$

We find $\zeta = 0.83$ (taking the Cr-O experimental distance), close to the full relaxation limit ($\zeta = 1$), which is more than in ruby $\alpha\text{-Al}_2\text{O}_3: \text{Cr}^{3+}$ ($\zeta = 0.76$).⁸ Vegard's law, which corresponds to $\zeta = 0$, is thus not obeyed at the atomic scale. The Cr-Al distance is intermediate between the Al-Al and Cr-Cr distances in MgAl_2O_4 and MgCr_2O_4 , which accounts for a partial relaxation of the second neighbors, but the third and fourth shells (O, Mg) do not relax, within the experimental and computational uncertainties. The chains of Al-centred octahedra are radially affected only at a local scale around Cr: the Al second neighbors relax partially outward Cr, with a Al-O bond slightly shortened. The angular deviations are also moderate (below 1°), since the sequence of octahedra is not modified, but these Al-centred octahedra are slightly distorted. Indeed, these octahedra being edge-shared, the number of degrees of freedom is reduced, and the polyhedra can either distort or tilt a little, one around another. It is interesting to point out that the three chains of octahedra are orientated along the three four-fold axes of the cubic structure, which are highly symmetric directions. On the contrary, an angular relaxation (3.5°) is observed for the Mg atoms, but with the absence of radial modifications. This must be connected to the fact that the tetrahedra share a vertex with the Cr-centred octahedron, a configuration which allows more flexibility for relative rotation of the polyhedra.

The extension of the relaxation process up to the second shell is not observed in the corundum solid solution, in which it is limited to the first coordination shell.¹⁵ Such a difference between these two solid solutions can be related to the lattice rigidity: the bulk modulus B is smaller in MgAl_2O_4 than in $\alpha\text{-Al}_2\text{O}_3$, 200 GPa and 251 GPa, respectively.³⁷ This difference directly arises from the peculiarity of the structure of these two crystals: in the spinel structure, one octahedron is edge-shared to 6 Al octahedra and corner-shared to 6 Mg-centred tetrahedra (Fig. 3b). In corundum, each octahedron is face-shared with another, in addition to corner and edge-sharing bonds: this is at the origin of the rigidity of the

corundum structure, which is less able to relax around a substitutional impurity such as Cr^{3+} , and relaxation is thus limited to the first neighbors.

IV. CONCLUSIONS

This study provides a direct evidence of the structural relaxation during the substitution of Cr for Al in MgAl_2O_4 spinel. The local structure determined by X-ray Absorption Spectroscopy and first-principles calculations show similar Cr-O distances and local symmetry in dilute and concentrated spinels. This demonstrates that, at the atomic scale, Vegard's law is not obeyed in the MgAl_2O_4 - MgCr_2O_4 solid solution. Though this result has been obtained in other types of materials (semiconductors, mixed salts), it is particularly relevant for oxides like spinel and corundum: indeed, the application of Vegard's law has long been a structural tool to interpret, within the so-called "point charge model",⁴ the color of minerals containing transition metal ions. In spinel, the full relaxation of the first shell is partially accommodated by strain-induced bond buckling, which was found to be weak in corundum: important angular tilts of the Mg-centred tetrahedra around the Cr-centred octahedron have been calculated, while the angles between

Cr- and Al-bearing edge-sharing octahedra are hardly affected. The improved thermal and mechanical properties of Cr-doped spinel may be explained by remanent local strain fields induced by the full relaxation of the structure around chromium, as it has been observed in other solid solutions.² Another important consequence of relaxation concerns the origin of the partition of elements between minerals and liquids in geochemical systems.⁵ Finally, the data obtained in this study will provide a structural basis for discussing the origin of color in red spinel and its variation at high Cr-contents. Indeed, the origin of the color differences between Cr-containing minerals (ruby, emerald, red spinel, alexandrite) is still actively debated.^{6,8,38}

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