

ACQUISITION AND MODELING OF A SPECTRUM IN A NON THERMAL EQUILIBRIUM PLASMA FORMED IN AIR WITH WATER

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Abstract

Spectra in the range of 365-385 nm, corresponding to the Schumann-Runge system of O₂ ($B^3\Sigma_u^- - X^3\Sigma_g^-$) and to the second positive system of N₂ ($C^3\Pi_u - B^3\Pi_g$) are measured by optical emission spectroscopy in a discharge with liquid non-metallic electrodes (DLNME) in air with water at atmospheric pressure. They are simulated theoretically. This discharge generates a non-equilibrium plasma. In this paper, we first describe the experimental set up. Then, we explain the method of spectra simulation. By comparison of measured and simulated spectra, we determine the rotational and vibrational temperature and the ratio between densities of two upper electronic quantum levels of the two considered systems. The possible mechanism of spectra formation is discussed.

Key words

Schumann-Runge system of O₂, second positive system of N₂, non equilibrium plasma, discharge with liquid non-metallic electrodes, air, water, plasma.

1. Introduction

Interest for radiation studies has been revived in the field of plasma physics by the upcoming entry of probes into planet atmosphere (Titan, Mars...) [1, 2] and by industrial applications (circuit breakers, waste treatment...)[3, 4]. The number of papers concerning the plasma modeling has increased the last years [5, 6]. Unfortunately it appears a lack of data and many areas need further studies. For example to expand the radiation database especially those in ultraviolet and deep ultraviolet wavelength, to study the effect of radiation on

ionization equilibrium, to test the composition calculation code in non equilibrium plasma, etc. For this purpose, we bring some new spectroscopy data obtained in non equilibrium plasma formed in air and water vapor at atmospheric pressure. Moreover, we prolong our investigation of a new kind of discharge: the discharge with liquid non-metallic electrodes (DLNME). As a matter of fact DLMNE with tap water electrodes is an effective generator of non-equilibrium plasma at the pressures up to atmospheric pressure. The DLMNE burns steadily under a DC power supply and the construction of the discharge assembly is simple: special chamber is not required and the discharge burn in open air. DLMNE generates plasma contaminated by a water vapor with an amount of 20 to 45% (molar percentage) [7, 8].

In this paper, we first describe the discharge assembly, the main features of the discharge and the scheme of experimental set-up for the spectroscopic measurements at the ultraviolet and deep ultraviolet wavelengths. Secondly, we describe the diatomic spectra calculation of the second positive system of N_2 and the Schumann-Runge system of O_2 in the wavelength range of 365 to 385 nm. The method of calculation was used in [9] to simulate the second positive system of N_2 . Here it is evolved and applied to simulate the Schumann-Runge system of O_2 too. Thirdly, we apply it to the simulation of the experimental results to obtain the rotational and vibrational temperatures. We determine the ratio between densities of two upper electronic quantum levels of the two considered systems O_2 and N_2 . Finally, we discuss the results.

2. Experimental set-up and discharge parameters.

The experiments were carried out with the discharge between two tap water streams in open air. The water streams flow along ceramic chutes making a small angle with vertical. The metallic current leads were inserted into the streams and were covered by a water layer with a thickness of a few millimeters. The inter-electrode gap L (the air gap between water surfaces facing each other) can be changed from $L = 6$ mm up to $L = 10$ mm. The discharge axis z is directed from the anode to the cathode and put $z=0$ at the surface of the water anode (Fig.1). The discharge burnt steadily with a DC current supply in a volumetric (diffuse) form at a relatively high voltage and low current density. For example, at current $I = (50-100)$ mA (current density $j \sim (0.25-0.5)$ A/cm²) and discharge length $L = 6$ mm the voltage between

metallic leads was $V \sim 3\text{kV}$. Voltage drop across the water electrodes was of about half of this value. So, the voltage drop across the air gap was $\sim 1.5\text{ kV}$.

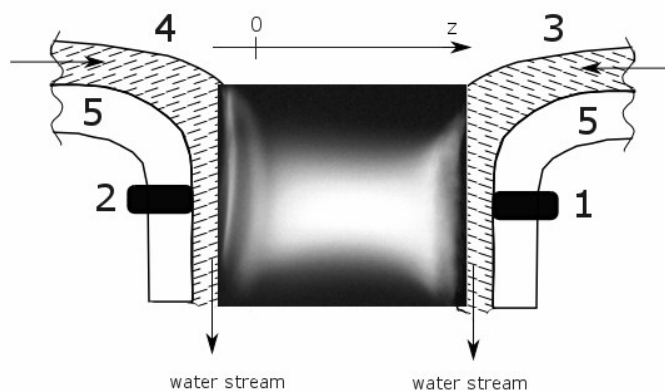


Figure.1: section view of the discharge assembly. 1,2 metallic current leads; 3 water-cathode; 4 water-anode; 5 ceramics chutes.

In the previous experiments [7, 8], we investigated by means of electric probe, microwave radiation absorption and emission spectroscopy the discharge with a length $L \approx 6\text{ mm}$ in the same assembly. Obtained results were compared with the spectra simulation and were used for plasma composition calculations.

Our investigations show that the discharge can be distinctly separated into three regions: the near-cathode ($\sim 2.5\text{ mm}$ in length) and near-anode ($\sim 1.5\text{ mm}$ in length) regions and the column. The electric field in the column is approximately constant $E_c \approx (7-8) \times 10^2\text{ V/cm}$ but the column is not quite uniform. It somewhat narrows at the joint with the near cathode region and expands toward the anode. The gas in the column is heated up to the temperature $\approx 2000\text{ K}$ in the cathode end and $\approx 1500\text{ K}$ in the anode end and is contaminated by the water vapor. Water contamination was estimated as $\sim (30-40)\%$ and $\sim (15-25)\%$ in the cathode and in the anode ends of the column correspondingly. So, the parameter E/N_g changes from $\approx 20\text{ Td}$ to $\approx 15\text{ Td}$ (here N_g – is a heavy particles concentration). The mean value of the charged particle concentration n_c is about 10^{12} cm^{-3} . The concentration decreases at the anode end of the column 1.5-2 times as much as against the cathode one. The mean energy of electrons was estimated to be about 0.4 eV . The near electrode regions are significantly non-uniform. The mean value of E/N_g was estimated to be of the order of 10^2 Td . The emission of discharge is mainly in violet and ultra violet range. The emission of N_2 and O_2 molecules and OH radical were observed in the near electrode regions and in the column. The emission of

ion N_2^+ and hydrogen atom was registered in the near-cathode region only. In the infrared range the emission of oxygen atom was registered too.

At the present time our main interest is to examine the ultraviolet and the deep ultraviolet range of the discharge spectrum. So, the part of the experimental set-up for spectroscopic investigations was changed. We replaced the quartz lens by the spherical mirror to avoid the chromatic aberration. A block diagram of spectroscopic measurements is shown in figure 2.

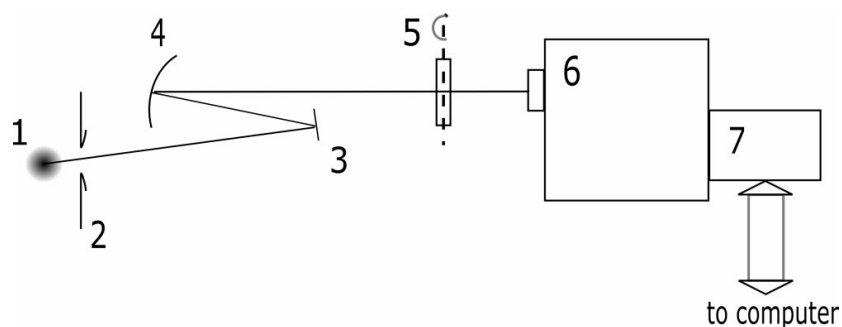


Figure 2: Block diagram of spectroscopic measurements. 1 discharge channel cross section; 2 diaphragm; 3 plain mirror; 4 spherical mirror; 5 plain-parallel quartz plate; 6 monochromator; 7 multichannel optical analyser with linear photodetector.

The necessity to use the plane mirror (3) is the result of some specific geometrical problems of our set-up. The spherical mirror (4) produced a reduced image of the discharge on the entrance slit of the monochromator (6), which is equipped with the grating of 1200 lines/mm providing the inverse dispersion of 1.3 nm/mm. The scanning of the image across the slit was carried out using a plain parallel quartz plate (5). A multichannel optical analyzer with a linear detector was used to record the radiation. The detector could record in a single measurement a part of spectrum of 22 nm in length. The spectral resolution with an entrance slit 0.1 mm is about 0.2 nm. Spectral sensitivity of our set-up was measured with the help of calibrated band lamp with a sapphire window. Equipment used provided the possibility to calibrate discharge spectra up to $\lambda \geq 240$ nm.

The discharge with a length $L \approx 6.5$ mm was examined. Each measurement of the spectrum was repeated three times. The results were summarized in the computer. This set-up permitted us to record spectra in the deep ultra violet range. Nevertheless, in this study, our main interest is the investigation of the part of the spectrum in the range 365-385 nm, which contains N_2 and O_2 emission.

3. Molecular spectrum calculations

In the range 365-385 nm, the spectrum is composed of two summed spectra. The first is due to the second positive system of N₂ (C³Π_u - B³Π_g) and the second is due to the Schumann-Runge system of O₂ (B³Σ_u⁻ - X³Σ_g⁻). To simulate the spectrum we have to take into account both systems.

The wave numbers of a transition from an upper quantum state (*n'*, *v'*, *J'*) to a lower quantum state (*n''*, *v''*, *J''*) is obtained by calculation of the energy difference between the two states taking into account the allowed quantum rules [10, 11, 12]:

$$\sigma_{n'',v'',J''}^{n',v',J'} = T_{n'} + G_{n'}(v') + F_{n',v'}(J') - [T_{n''} + G_{n''}(v'') + F_{n'',v''}(J'')] \quad (1)$$

where *n* is the electronic quantum number, *v* the vibrational quantum number, *J* is the rotational quantum number. The wave number and energy terms are expressed in cm⁻¹. *T* is the electronic excitation energy of the quantum level (*n*), *G* is the vibrational energy of the quantum level (*n*, *v*) and *F* is the rotational energy of the quantum level (*n*, *v*, *J*).

At each wave number, the integrated volume emission (intensity) is calculated by the following expression :

$$I_{n'',v'',J''}^{n',v',J'} = Cte \times (\sigma_{n'',v'',J''}^{n',v',J'})^4 \times S_{v',v''} \times S_{J',J''} \times \frac{\phi \times N_{n'}}{(2 - \delta_{0,\Lambda'+\Lambda''}) \times (2S'+1)} \times \frac{\exp\left(-\beta \left[\frac{G(v')}{T_{vib}} + \frac{F_{v'}(J')}{T_{rot}} \right]\right)}{Q_{int}(T_{rot}, T_{vib})} \quad (2)$$

where $\beta = \frac{hc}{k}$ is equal to 1.4387685 cm.K. *h*, *c*, *k* respectively represent the Planck's constant, the velocity of light and the Boltzmann's constant. *Cte* is a constant. Factor *S_{v',v''}* is the strength band of the band (*v'*, *v''*). Our chosen values are given in table 1. The strength line *S_{J',J''}* is the Höln-London factor, which is calculated from Kovacs' tables [10]. The internal partition function *Q_{int}* depending on the rotational and vibrational temperatures is written as follows [13, 14] :

$$Q_{int}(T_{rot}, T_{vib}) = \sum_{v=0}^{v_{max}} \exp\left(-\beta \frac{G(v)}{T_{vib}}\right) \sum_{J=0}^{J_{max}(v)} \frac{g_J}{\zeta} \times \exp\left(-\beta \frac{F_v(J)}{T_{rot}}\right) \quad (3)$$

N_{n'} represents the density of the excited level *n'* of the diatomic molecule. *g_J* is the rotational statistical weight and ζ is equal to 2 for O₂ and N₂.

We have to note that equation (2) assumes two main assumptions. The first is that the population densities of vibrational and rotational levels satisfy the Boltzmann distribution at respectively T_{vib} and T_{rot} . The second is the Born-Oppenheimer approximation.

The calculated intensities (2) are convoluted with a Gaussian profile determined by its Full Width at Half-Maximum ($FWHM$) that we take equal to 0.19 nm. The contribution of all lines emitted is summarised in the considered spectral range. To obtain the wavelength from the wave number we take into account the index refraction of air [15]. Since the considered wavelength is not deep in ultraviolet, we do not take absorption into account [15, 16]. Then the simulated spectrum of each considered system is obtained for the following parameters: rotational temperature T_{rot} , vibrational temperature T_{vib} and upper level density $N_{n'}$ of electronic excitation quantum level n' . That is to say $C^3\Pi_u$ for N_2 and $B^3\Sigma_u^-$ for O_2 .

$(v'-v'')$	$S_{v'v''} (D^2)$	$(v'-v'')$	$S_{v'v''} (D^2)$
(0-16)	0.383241	(3-18)	0.215482
(0-17)	0.243796	(4-19)	0.093186
(1-17)	0.367441	(5-19)	0.133834
(2-17)	0.015282	(6-20)	0.091272
(2-18)	0.031089	(7-20)	0.104947

Table 1 a: $S_{v'v''}$ strength bands values of the Schumann-Runge system of O_2 taken from RADEN data base [17] used for the calculated spectra in 365-385 nm wavelength range, D is the Debye unit.

$(v'-v'')$	$S_{v'v''} (D^2)$
(0-2)	3.739799
(1-3)	4.985702
(2-4)	3.945647
(3-5)	2.238900

Table 1 b: $S_{v'v''}$ strength bands values of the second positive system of N_2 , sequence -2 taken from RADEN data base [17] used for the calculated spectra in 365-385 nm wavelength range.

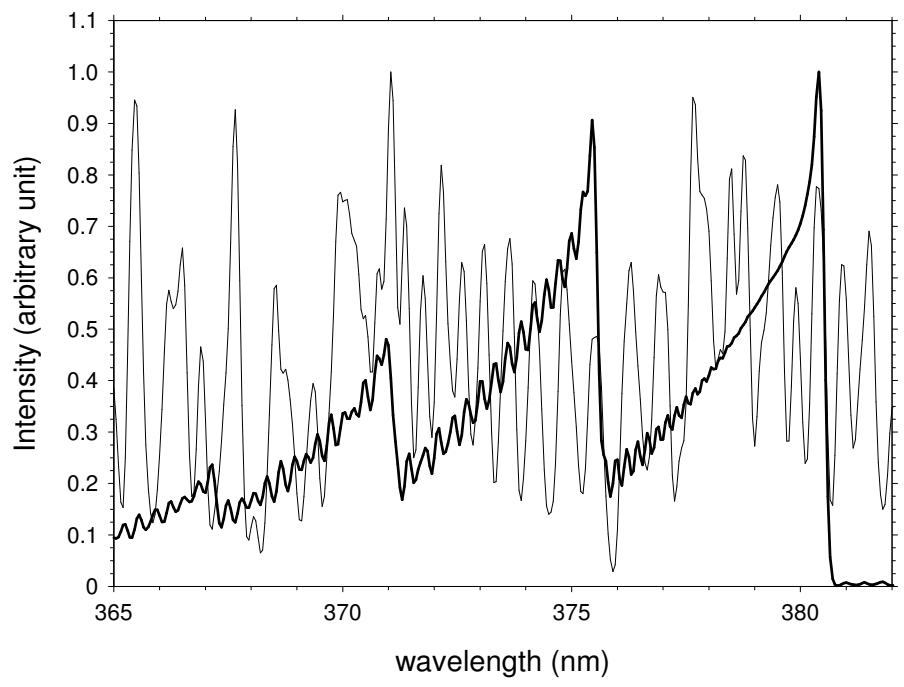


Figure 3 : Calculated intensities (arbitrary unit) of Schumann-Runge system of O₂ ($B^3\Sigma_u^- - X^3\Sigma_g^-$) (thin line) and second positive system of N₂ ($C^3\Pi_u - B^3\Pi_g$) (thick line) versus wavelength. Rotational temperature, vibrational temperature and FWHM are respectively fixed at 2000 K, 4000 K and 0.19 nm.

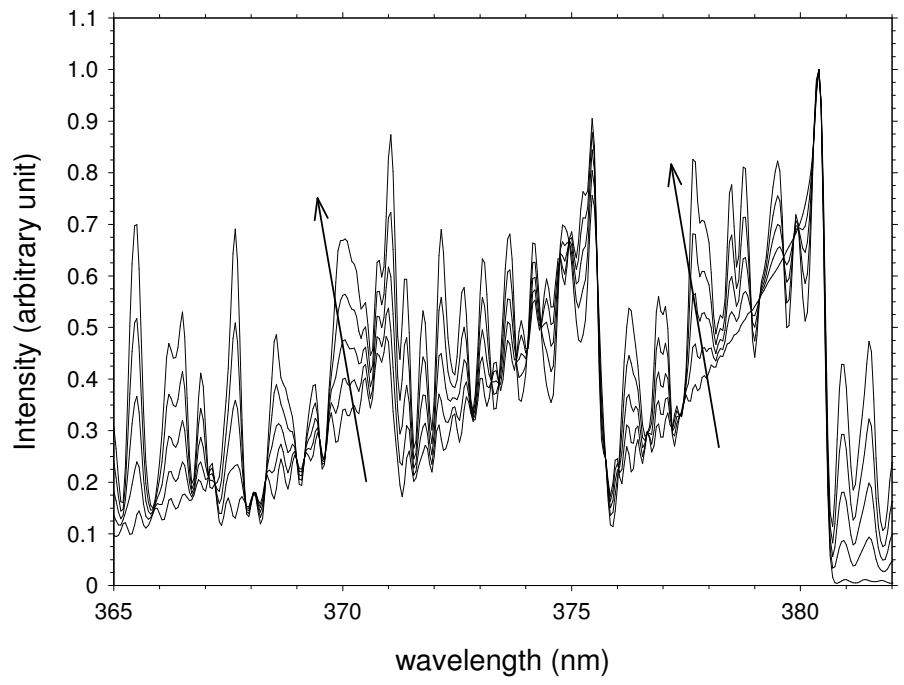


Figure 4 : Resulting Spectra (Schumann-Runge system of O₂ and second positive system of N₂) for several χ^* (0.01, 0.20, 0.50, 1.00, 2.00) values versus wavelength. ($T_{rot}=2000$ K, $T_{vib}=4000$ K, FWHM=0.19 nm).

In figure 3 the spectra in arbitrary units of the intensity are plotted versus wavelength of both considered systems. The two spectra are presented separately to realize wavelength position of each system. We can notice that the systems perturb each other so the interpretation of experimental spectra is difficult. Consequently we introduce a new parameter χ^* that is the ratio between densities of two upper electronic quantum levels of the two considered systems:

$$\chi^* = \frac{[O_2(B^3\Sigma_u^-)]}{[N_2(C^3\Pi_u)]} \quad (4)$$

In figure 4, we have plotted the intensity of the resulting spectrum versus the wavelength for several ratios χ^* (0.01, 0.2, 0.5, 1, 2). The rotational temperature has been fixed to 2000 K, and the vibrational temperature to 4000 K. We note that the resulting spectrum depends mainly on the ratio χ^* and consequently on the density of the $C^3\Pi_u$ level for N_2 and $B^3\Sigma_u^-$ level for O_2 . So, the comparison with experimental results is a new source of comprehensive results.

4. Comparison between experimental and simulated spectra; results and discussion.

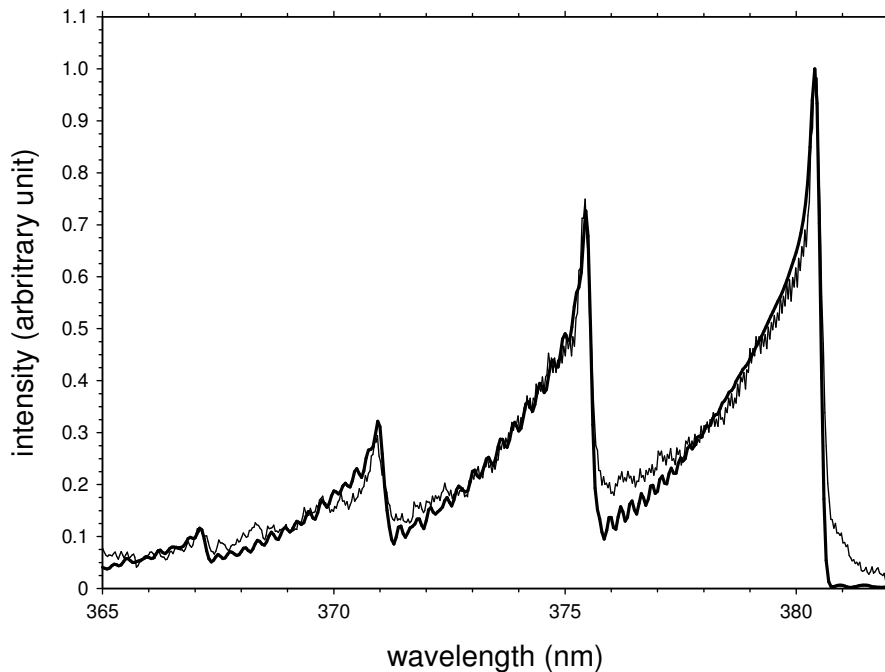


Figure 5 a: Comparison between the experimental spectrum (thin line) and the simulated spectrum (thick line) with the best fitting parameters T_{rot} , T_{vib} and χ^* : 1400 K, 3400 K and 0.01 respectively at a distance of 1mm from the anode.

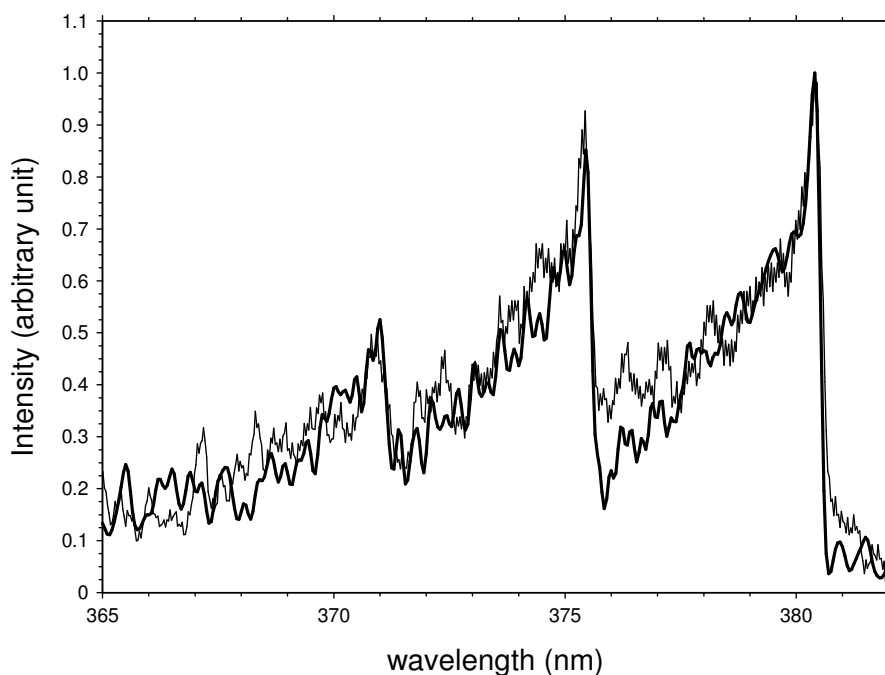


Figure 5 b: Comparison between the experimental spectrum (thin line) and the simulated spectrum (thick line) with the best fitting parameters T_{rot} , T_{vib} and χ^* : 2000 K, 3800 K and 0.25 respectively at a distance of 1.9 mm from the anode.

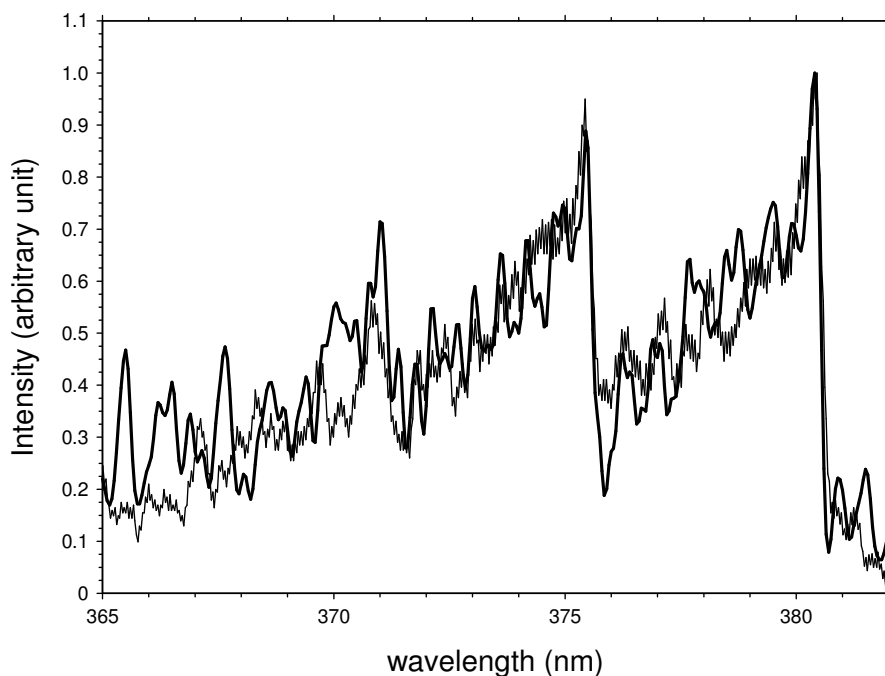


Figure 5 c: Comparison between the experimental spectrum (thin line) and the simulated spectrum (thick line) with the best fitting parameters T_{rot} , T_{vib} and χ^* : 2400 K, 4000 K and 0.70 respectively at a distance of 4.2 mm from the anode.

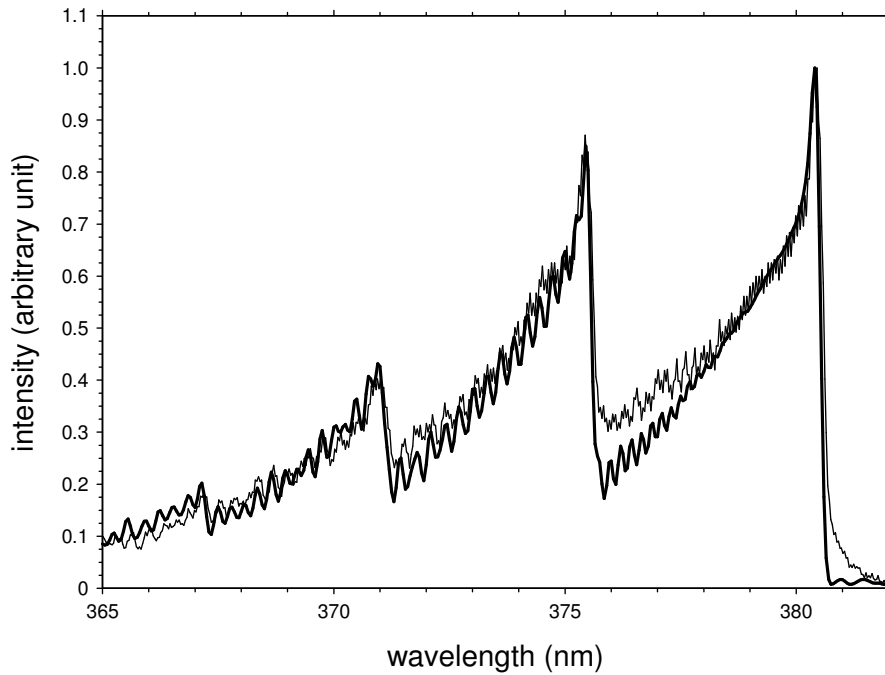


Figure 5 d: Comparison between the experimental spectrum (thin line) and the simulated spectrum (thick line) with the best fitting parameters T_{rot} , T_{vib} and χ^* : 2000 K, 3600 K and 0.03 respectively at a distance of 5.6 mm from the anode.

The resulting simulated spectrum in the considered wavelength range depends on three parameters: the rotational temperature T_{rot} , the vibrational temperature T_{vib} and the parameter χ^* . By fitting the experimental results, we have tried to determine those parameters. For this purpose, we first determine χ^* from spectrum part in the wavelength range around 370 nm and around 377 nm. Afterwards, with this value of χ^* , we compare spectra for different values of T_{rot} in the 376-381 nm wavelength range. As a matter of fact the variation of T_{vib} has no effect on the spectra in this wavelength range if the spectra are normalized in intensity at the band-head (0-2) of $N_2(2S^+)$. Finally, T_{vib} is determined in the wavelength interval of 365-385 nm. In figures 5 we show the result of the best fitting. We note that spectra shown in fig.5a and 5d were measured in the near-electrode regions and spectra shown in fig.5b and 5c were measured in the discharge column.

It can be seen that the measured and simulated spectra are in rather good accordance. But there are some discrepancies in the details.

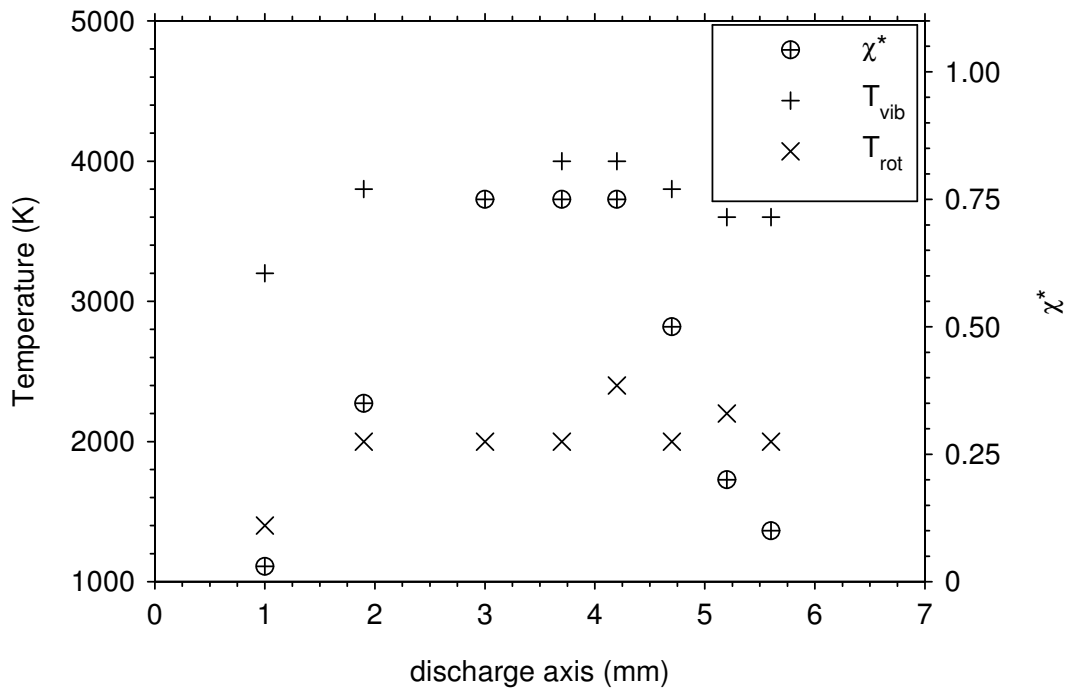


Figure 6: T_{vib} , T_{rot} and χ^* obtained along the discharge axis.

In figure 6, we have plotted the axial distribution of obtained rotational and vibrational temperatures and χ^* parameters. It can be seen that the parameter χ^* is approximately constant in the main part of the column ($1.5 \leq z \leq 4$ mm) and a small decrease can be observed in the near anode end. But in the near electrode regions the χ^* parameter decreases significantly. This behavior can be explained taking into account the axial dependences of the N_2 and O_2 emission intensities. N_2 emission has pronounced near-electrodes maxima [7]. O_2 emission is distributed much more homogeneously in the whole interelectrode gap and does not display maxima near the electrodes. As it was shown in our previous work [7], the electric field increases significantly in near-electrodes regions. So, one can conclude that the populations of N_2 ($\text{C}^3\Pi_u$) and of O_2 ($\text{B}^3\Sigma_u^-$) levels are determined by various processes.

In [8], the mean electron energy value in the plasma column is obtained by the comparison of the electrical probe and microwave emission absorption measurements with the results of the composition calculation. We use this value of electron energy to calculate the absolute value of the emission of some species (N_2 , N_2^+ , O I , H_α). We have assumed that these levels are populated in accordance with Boltzmann distribution. The comparison with the results of spectroscopic measurements was in surprisingly good agreement. Calculating O_2 spectra in our considered wavelength range with the same electron energy and the same

assumption about Boltzmann distribution (the same calculation code with $T_{rot}=2100\text{K}$, $T_{vib}=3800\text{K}$), we observe a great difference with experimental result (figure 7). To obtain a closed normalized spectra to experimental spectra, we have to decrease the total concentration of O_2 by a factor of $5 \cdot 10^3$ that is not acceptable taking our previous results into account [8]. We can conclude that O_2 ($\text{B}^3\Pi_u$) is not populated in accordance with Boltzmann distribution at the above mentioned temperature.

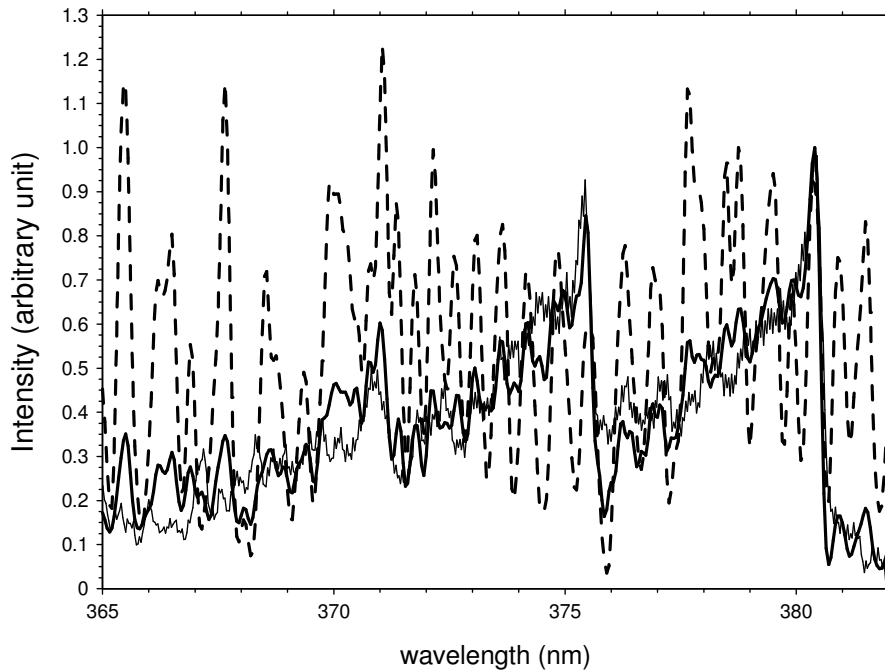


Figure 7: Comparison of normalized spectra. Experimental spectrum (distance of 1.9 mm from the anode) (Thin line), calculated spectra ($T_{rot}=2100\text{K}$, $T_{vib}=3800\text{K}$, $\text{FWHM}=0.19\text{ nm}$) with $[\text{O}_2]=10^{24}\text{ m}^{-3}$ and $[\text{N}_2]=4 \cdot 10^{24}\text{ m}^{-3}$ (dashed curve) and with $[\text{O}_2]=2 \cdot 10^{20}\text{ m}^{-3}$ and $[\text{N}_2]=4 \cdot 10^{24}\text{ m}^{-3}$ (bold curve).

The rotational temperature and vibrational temperatures have a value respectively around 2100 K and around 3800 K in the main part of discharge column. The value of T_{rot} is in a good agreement with our previous results but the value of T_{vib} somewhat lower. T_{vib} was overestimated in [7] because in the past we did not take into account O_2 emission.

Conclusion

The results obtained in this work demonstrate that the comparison of spectra simulation with experimental spectra of DLMNE, which contain the second positive system of N_2 and the Schumann-Runge system of O_2 in the wavelength range of 365 to 385 nm, give rather good results. But there exists some discrepancies in the details.

In our previous papers [7, 8], we showed a good agreement between the composition calculation, the measurements of the electrons concentration and the intensity of emission of some species ($N_2(2+)$ system, N_2^+ , O I, H_α) in the column of DLMNE. We showed also that the water vapour proportion is high near the cathode zone and slowly decreases toward the anode.

Our new results show that the population of the $B^3\Sigma_u^-$ of O_2 does not follow the Boltzmann distribution assumed in the composition calculation. Some preliminary results of the measurements of NO(A) emission show analogous regularity. We'd like to note that the emissions of N_2 , N_2^+ , O I, H_α mentioned above come from the levels with high excitation energy. On the contrary, $O_2(B-X)$ and NO(A-X) emissions come from the levels with lower electronic excitation energy. We intend to show the results of NO(A) emission investigations in our next publication.

So we can think that $O_2(B)$ and NO(A) are quenched with a species as H_2O and/or OH because in our discharge exists a relatively high contamination by the water vapour. Furthermore, H_2O and OH are known as effective quenchers [18, 19]. We intend to prolong this work and to try to confirm the latter explanation proposed here.

5. References

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