

# Stationary accretion disks launching super fast-magnetosonic MHD jets

Jonathan Ferreira<sup>1</sup>

and

Fabien Casse<sup>2</sup>

## ABSTRACT

We present self-similar models of resistive viscous Keplerian disks driving non-relativistic magnetohydrodynamics (MHD) jets becoming super fast-magnetosonic. We show that in order to obtain such solutions, the thermal pressure must be a sizeable fraction of the poloidal magnetic pressure at the Alfvén surface. These steady solutions which undergo a recollimation shock causally disconnected from the driving engine, account for structures with a high temperature plasma in the sub-Alfvénic region. We suggest that only unsteady outflows with typical time-scales of several disk dynamical time-scales can be produced if the suitable pressure conditions are not fulfilled.

*Subject headings:* accretion, accretion disks — MHD — ISM: jets and outflows — galaxies: jets

## 1. Introduction

Self-collimated jets are now commonly observed originating from young stellar objects (YSOs), active galactic nuclei and galactic binaries (Livio 1997). All these flows share common properties like being always correlated with the accretion phenomenon (Hartigan et al. 1995; Falcke & Biermann 1996; Serjeant et al. 1998; Gallo et al. 2003). It has long been identified that jet self-confinement requires the presence of a large scale magnetic field in order to focus the outflowing plasma (Chan & Henriksen 1980). The “universal” paradigm of jet

---

<sup>1</sup>Laboratoire d’Astrophysique de Grenoble, 414 rue de la piscine, BP 53, F-38041 Grenoble, ferreira@obs.ujf-grenoble.fr

<sup>2</sup>Institute for Plasma Physics Rijnhuizen, P.O. Box 1207, 3430 BE Nieuwegein, Netherlands, fcasse@rijnh.nl

formation relies on the occurrence of bipolar magnetic fields threading the accretion disk. As a consequence, the theory of accretion disks had to be revisited in order to take into account the mass, angular momentum and energy extractions achieved by the jet. One notorious modification to the standard picture is the necessary radial stratification of the disk accretion rate, namely  $\dot{M}_a \propto r^\xi$  ( $\xi$  being a measure of the disk ejection efficiency). For instance  $\xi = 0$  describes a standard disk with no outflow while  $0 < \xi < 1$  stands for an ejecting Keplerian accretion disk (Ferreira 1997). If one wishes to obtain the exact ejection efficiency, one has to solve without any approximation the full magnetohydrodynamics (MHD) 2D structure of the disk.

Anomalous magnetic diffusivity must be present within the disk to allow accreting (and rotating) mass to cross the magnetic field lines whereas ejected mass becomes frozen in to the field. Only self-similar solutions taking into account the underlying resistive accretion disk hitherto provided this description (Ferreira & Pelletier 1995; Ferreira 1997; Casse & Ferreira 2000a,b). Within these solutions, once in ideal MHD regime, mass is magnetically accelerated along each field line and must successively cross three MHD critical points, namely the slow and fast magnetosonic ones (SM,FM) and the Alfvénic point (A). So far, none of the self-similar solutions was able to obtain both disk and jet flows, the latter crossing the three critical surfaces.

Using the same framework, Vlahakis et al. (2000) solved the ideal MHD jet equations and provided new solutions crossing these three critical points. However since these solutions were not connected to the underlying disk, the issue of super-FM jet production from accretion disk remained. In this letter, we intend to present the necessary conditions to get self-similar super-FM jets (Sect. 2), discuss the properties of typical solutions (Sect. 3) and conclude with some astrophysical implications that may be put to the test of observations.

## 2. Role of a sub-Alfvénic heating

Stationary jets are described by a set of axisymmetric ideal MHD equations. Thus the poloidal magnetic field writes  $\mathbf{B}_p = (\nabla a \times \mathbf{e}_\phi)/r$ , where  $a(r, z) = Cst$  describes a surface of constant magnetic flux. Disk winds are produced whenever a large scale magnetic field, close to equipartition with the disk thermal pressure (Ferreira & Pelletier 1995), is present over a range in anchoring radii  $r_o$ . The corresponding jet is made of magnetic surfaces nested one around each other with several integrals of motion. In the non-relativistic case, one gets ( $u_p$  poloidal velocity,  $\Omega$  angular velocity and  $\rho$  density): (1) the mass to magnetic flux ratio  $\eta(a)$  with  $\mathbf{u}_p = \eta(a)\mathbf{B}_p/\mu_o\rho$ ; (2) the angular velocity of a magnetic surface  $\Omega_*(a) = \Omega - \eta B_\phi/\mu_o\rho r$  and (3) the specific total angular momentum  $L(a) = \Omega_* r_A^2 = \Omega r^2 - r B_\phi/\eta$  transported

away. Here,  $r_A$  is the Alfvén radius where mass reaches the Alfvén poloidal velocity. In this letter, we are interested in jets that may be heated by their surroundings so that an adiabatic description is inadequate. Instead, we will assume the presence of a heat flux  $\mathbf{q} = \nabla H - \nabla P/\rho$ , where  $H$  is the usual enthalpy for a perfect gas. Including this additional effect, one gets the generalized Bernoulli invariant  $E(a) + \mathcal{F}(s, a) = \frac{u^2}{2} + H + \Phi_G - r\Omega_* B_\phi/\eta$ , where  $\mathcal{F}(s, a) = \int_{s^+}^s \mathbf{q} \cdot \mathbf{e}_\parallel ds'$  is the heating term that depends on a curvilinear coordinate  $s$  along a given magnetic surface ( $s^+$  is roughly the SM point and  $\mathbf{B}_p = B_p \mathbf{e}_\parallel$ ). The total specific energy provided at the disk surface is  $E(a) \simeq \Omega_o^2 r_o^2 (\lambda - 3/2)$  for a thin disk, where  $\Omega_o$  is the Keplerian rotation at the anchoring radius  $r_o$  and  $\lambda = L/\Omega_o r_o^2$  is the magnetic lever arm. The shape of the magnetic surface is given by the Grad-Shafranov (GS) equation

$$(1 - m^2)J_\phi = J_\lambda + J_\kappa + J_\beta, \quad (1)$$

$$\text{where } J_\lambda = \rho r \left( \frac{d\mathcal{E}}{da} + (1 - g)\Omega_* r^2 \frac{d\Omega_*}{da} + g\Omega_* \frac{d\Omega_* r_A^2}{da} \right)$$

$$J_\kappa = r \frac{B_\phi^2 - m^2 B_p^2}{2\mu_o} \frac{d \ln \rho_A}{da} + m^2 \frac{\nabla a}{\mu_o r} \nabla \ln \rho$$

$$J_\beta = \frac{\rho}{B_p} (\nabla \mathcal{F} - \mathbf{q}) \cdot \mathbf{e}_\perp$$

Here,  $\mathbf{e}_\perp = \nabla a/|\nabla a|$ ,  $m = u_p/V_{Ap}$  is the Alfvénic Mach number and  $g = 1 - \Omega/\Omega_*$ . GS equation provides  $a(r, z)$  for a given set of invariants. Unfortunately, it is a PDE of mixed type: it is hyperbolic between the cusp (where  $u_p = V_c = C_s V_{Ap}/\sqrt{C_s^2 + V_A^2}$ ) and the slow-magnetosonic surface (where  $u_p = V_{SM,p}$ ), elliptic between the SM and the fast-magnetosonic surface (where  $u_p = V_{FM,p}$ ) and hyperbolic further out. The magnetosonic phase speeds involved in these definitions are the usual ones, i.e. waves travelling along the poloidal field. Solving Eq. (1) remains a major challenge in applied mathematics: it would require to *a priori* know the locus of these surfaces, whereas they emerge as the global solution evolves. In practice, one either solves the time-dependent problem with full MHD codes, or uses a method of variable separation.

Self-similar solutions allow to solve the full set of MHD equations without any approximation. The problem reduces to propagate the solution along a self-similar variable  $x = z/r$ , which involves the inversion of a matrix. Its determinant vanishes at three singular points where the following numbers become equal to unity:  $M_{SM} = V/V_{SM,n}$ ,  $M_A = V/V_{A,n}$  and  $M_{FM} = V/V_{FM,n}$ , where  $V = \mathbf{u}_p \cdot \mathbf{n}$  and  $V_{A,n} = \mathbf{V}_A \cdot \mathbf{n}$  are projections in the direction  $\mathbf{n}$  (see Fig. 1) and  $V_{SM/FM,n}^2 = \frac{1}{2} \left( V_A^2 + C_s^2 \pm \sqrt{(V_A^2 + C_s^2)^2 - 4C_s^2 V_{A,n}^2} \right)$  (Ferreira & Pelletier 1995). Not all these critical points coincide with the above mentioned points where the flow changes type:  $M_A = m$ ,  $M_{SM} \simeq u_p/V_c \simeq u_p/V_{SM,p}$  (in the cold Keplerian limit) but  $M_{FM} < n = u_p/V_{FM,p}$ . The critical FM surface is always located downstream in the hyperbolic region. The necessary conditions to provide cold super-Alfvénic jets from Keplerian

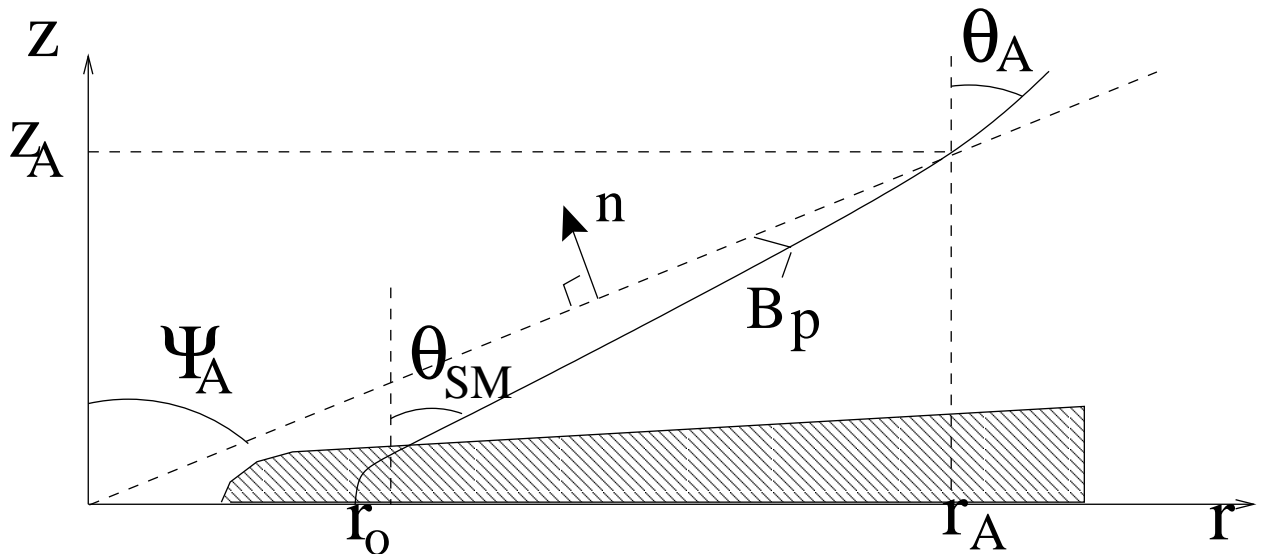


Fig. 1.— Geometry of a disk wind configuration and definitions of quantities related to the Alfvén critical surface. The unit vector  $\mathbf{n}$  is defined as  $(\mathbf{z}, \mathbf{r})/\sqrt{r^2 + z^2}$ .

disks were given in Ferreira (1997). Once fulfilled, a super-A solution propagates further away until collimation by the hoop-stress takes place. This produces an unavoidable decrease of the projected velocity ( $V \rightarrow -u_r \simeq 0$ ), even if the poloidal velocity reaches its asymptotic value of  $\Omega_o r_o \sqrt{2\lambda - 3}$ . The only way to allow for a super-FM solution with  $M_{FM} > 1$  is to lower this projection effect by forcing the magnetic surfaces to remain wide open, namely bringing the Alfvén surface closer to the disk (increase  $\Psi_A$ ). The self-similar expression of the GS equation in the *cold* regime can be written as  $\cos \theta_A = R(\theta_A; \Psi_A)$  at the Alfvén point (Casse & Ferreira 2000a). It is an implicit equation providing the jet opening angle  $\theta_A$  for a given position of the Alfvén surface  $\Psi_A$ . In the cold limit, one has  $\tan \theta_{SM} \sim \tan \Psi_A (1 - \lambda^{-1/2})$  for a given magnetic lever arm  $\lambda \simeq r_A^2 / r_o^2$  and initial opening angle  $\theta_{SM}$  (see Fig. 1). This initial opening angle is constrained by the underlying disk vertical equilibrium. The larger angle, the larger the magnetic compression and the less mass is being ejected. Only angles up to  $\sim 45^\circ$  ( $z_A \sim r_A$ ) have been proved to be possible from Keplerian accretion disks, either with isothermal (Ferreira 1997) or adiabatic jets (Casse & Ferreira 2000a), but none of these solutions can become super-FM.

Every super-FM solutions obtained by Vlahakis et al. (2000) exhibit Alfvén surfaces closer to the equatorial plane (i.e.  $\Psi_A \sim 60^\circ$ ), but being not connected to a resistive MHD disk, they did not have to fulfill the requirement of a quasi-static disk vertical equilibrium. Actually no Keplerian disk would probably survive the overwhelming magnetic compression imposed by the bending of the field lines (or allow the imposed mass effluvium). The

only possibility to have an Alfvén surface closer to the disk is to break this univocal link between  $\Psi_A$  and  $\theta_{SM}$ . This implies a change of some invariants (entropy and total specific energy) between the disk and the Alfvén surface. Physically this requires an extra force term in the GS equation, namely a strong outwardly directed pressure gradient in the sub-A region. Within the self-similar framework, it means building up a large thermal pressure, thus an additional heating starting above the disk. The generalized GS equation becomes  $\cos \theta_A = R(\theta_A; \Psi_A) + R_\beta(\theta_A; \Psi_A)$  where

$$\begin{aligned}
 R_\beta(\theta_A; \Psi_A) = & -\frac{g_A \beta_A}{4} \left( \frac{2}{g_A} \cos \theta_A + \frac{\sin \Psi_A}{\sin(\Psi_A - \theta_A)} \right. \\
 & \times \left. \left\{ \frac{\mathcal{F}_A}{C_{s,A}^2} - \frac{2}{g_A} - \frac{d \ln \rho_A}{d \ln r_o} - \frac{1}{\gamma - 1} \right\} \right. \\
 & \left. + \frac{\cos(\Psi_A - \theta_A)}{\sin \Psi_A} \left\{ \frac{r_A \mathbf{q} \cdot \mathbf{e}_{\parallel A}}{C_{s,A}^2 \cos \theta_A} - \frac{\partial \ln C_s^2}{\partial x} \Big|_A \right\} \right)
 \end{aligned} \tag{2}$$

is the contribution of this additional heat flux and  $\beta_A$  is the ratio of the plasma pressure  $P_A \equiv \rho_A C_{s,A}^2$  to the poloidal magnetic pressure at the Alfvén point. This equation shows that  $\beta_A$  large enough ( $\beta_A \gtrsim 1$ ) and  $R_\beta$  negative are two necessary conditions to increase  $\Psi_A$ . Indeed, since  $\theta_A$  is always smaller than  $\Psi_A$ , any tendency to increase  $\theta_A$  leads to a lowering of the Alfvén surface.

At the Alfvén surface,  $\beta_A = 2\omega_A^2 \frac{\epsilon^2 T_A}{\lambda T_o}$  where  $\omega_A = \Omega_* r_A / u_{p,A} \gtrsim 1$  (Ferreira 1997; Casse & Ferreira 2000a) and  $\epsilon = h/r$  is the disk aspect ratio. This general expression shows that any cold jet (isothermal  $T_A = T_o$  or adiabatic  $T_A \ll T_o$ ) always displays  $\beta_A \ll 1$ . In order to have any influence on the transverse equilibrium, this additional heating must provide a large increase in jet temperature, namely  $T_A \gtrsim T_o / \epsilon^2$ . The second condition ( $R_\beta < 0$ ) sheds light on the required heating function. The sum of the first two terms in (2) is usually always negative. Indeed, energy conservation gives  $\mathcal{F}_A / C_{s,A}^2 \geq \frac{\gamma}{\gamma-1} (1 - \frac{T_o}{T_A})$  because of the tremendous cooling due to the jet expansion. Since  $T_A$  must be large, the ratio  $\mathcal{F}_A / C_{s,A}^2$  is always large enough (but of order unity). The third term of (2) shows that the most favourable situation is the presence of additional heating mainly in the sub-A region, i.e. a vanishing heat flux ( $\mathbf{q} \cdot \mathbf{e}_{\parallel A} = 0$  or very small) and an already decreasing temperature (due to adiabatic cooling).

### 3. Self-similar numerical solutions

We follow basically the same integration procedure as in our previous works (see Casse & Ferreira (2000b) for more details). A heating function is assumed to be present, starting

at the disk surface but vanishing before the Alfvén point, with an adiabatic index  $\gamma = 5/3$ . Further up, we allow for a continuous transition to a polytropic energy equation,  $P \propto \rho^\Gamma$ . The X-type FM critical point allows to determine the critical value  $\Gamma_c$  of the polytropic index: if  $\Gamma < \Gamma_c$  thermal acceleration is too inefficient (breeze-like solution) whereas if  $\Gamma > \Gamma_c$  the strong decrease in enthalpy leads to a shock-like solution. Although Vlahakis et al. (2000) used an analogous way, our solutions strongly differ by the fact that jet invariants are fixed by the disk. Therefore, we need first to drastically increase the jet enthalpy before fine-tuning the polytropic index. As in solar wind models, we are playing around with one free parameter ( $\Gamma$ ) whilst one should solve the full energy equation.

Figure 2 shows a typical super-FM solution obtained with  $\Gamma_c = 1.45$ . The energy input required can be measured by the ratio  $f = \mathcal{F}(x_A, a)/E(a)$  since most of the heating occurs in the sub-A region. Solutions displayed here required  $f$  of several  $10^{-3}$ , allowing to get  $\Psi_A \simeq 65^\circ$  with  $\beta_A \simeq 0.1$  (condition  $T_A \sim T_o/\epsilon^2$  is verified). Note that smaller temperature values would also allow super-FM jets but they would just be terminated much sooner as in Vlahakis et al. (2000). In general 2D flows, the “causal horizon” (here the  $M_{FM} = 1$  surface) is the envelope of one of the two families of characteristics (Tsinganos et al. 1996) and not the surface of parabolicity  $n = 1$  (see Fig. 3). Any perturbation occurring to the flow downstream to the  $M_{FM} = 1$  surface is unable to cross this horizon. This result is generic to 2D solutions, the only bias introduced by self-similarity is the conical shape of such surfaces, not their separate existence. This has strong consequences on numerical experiments, as already pointed out by Ustyugova et al. (1999). To ensure the absence of feedback from the imposed boundary conditions, the Mach cones (defined locally as the tangents to the characteristics) must be directed out of the computational domain at its boundaries.

#### 4. Astrophysical implications

The present computed MHD flows are the first-ever steady-state solutions describing an overall accretion-ejection structure from the resistive accretion disk to the super-FM jet region. The strict stationarity of such accretion-ejection engines depends critically on the thermal properties of the sub-Alfvénic region. If the plasma pressure, measured at the Alfvén point, is a sizeable fraction of the poloidal magnetic pressure, MHD jets from Keplerian accretion disks can become super-FM. In the super-FM region, the jet is always facing a recollimation that ends up as a shock. The further jet propagation requires numerical time-dependent simulations. Around a protostar, such thermal pressure gradient occurs whenever temperatures as high as several  $10^5$  K are reached along the inner streamline. This is compatible with recent observations of blueshifted UV emission lines (Gómez de Castro

& Verdugo 2001) and some absorption features (Takami et al. 2002). Unfortunately, the heating source can only be inferred from its effects and its origin remains a crucial issue. For instance YSOs accretion disks are assumed to be highly magnetized so one may safely expect that some accretion energy is also dissipated in the upper disk layers and provides coronal heating (Galeev et al. 1979; Heyvaerts & Priest 1989). This is actually shown by both numerical simulations (Miller & Stone 2000) and some observational indication of accretion powered coronae (Kwan 1997). Moreover, since the central object has a hard surface, the shock of the infalling material provides another source of UV radiation (as well as X-rays), illuminating the disk and heating the sub-A region (Ferro-Fontán & Gómez de Castro 2003). An alternative to this additional heating would be the presence of a high pressure inner flow (a “spine”) forcing the MHD disk wind to open up. In YSOs such a flow could be provided by the interaction between the protostellar magnetosphere and the disk (Ferreira et al. 2000; Matt et al. 2002; Romanova et al. 2002). Temperatures required around a compact object imply a relativistic plasma. In this case, the inner pressure could be provided by an inner beam composed of relativistic electron-positron pairs, heated and accelerated inside the hollow part of the disk wind (Renaud & Henri 1998).

On the other hand if an accretion-ejection engine cannot provide this additional heating or if there is no inner “spine”, then the thermal pressure is negligible at the Alfvén surface and jets remain sub-FM. Recollimation towards the axis leads to the formation of a shock and the overall structure is therefore unsteady. However, no MHD signal can propagate upstream along the magnetic field towards the disk. Instead, in this hyperbolic region, the information that a shock has occurred is first carried away by MHD waves travelling along the characteristics until the  $n = 1$  surface is reached (see Fig. 3). Once in the elliptic domain, the fastest mode travels along the magnetic field down to the disk. As a consequence, the time taken by MHD waves to inform the disk is always larger than the one given by e.g. computing the time  $\tau = \int ds/V_{FM,p}$  taken by the fast mode along the same fieldline. As an illustration, let us take the cold sub-FM solutions of Ferreira (1997), as pictured in his Fig. 6. For the solutions recollimating right after the Alfvén surface this time  $\tau$  is roughly equal to the orbital period  $\tau_o$  at the anchoring radius, whereas for those recollimating much farther away, one gets  $\tau \gtrsim 10^2 \tau_o$ . The presence of sporadic jet events with time scales much larger than disk dynamical time scales (Raga et al. (2002), Gallo et al. (2003) and references therein) could fit into the picture of an accretion-ejection engine trying to adjust itself.

The amount of large scale poloidal magnetic flux trapped in accretion disks is completely unknown. The above astrophysical implications only hold if this flux is large enough so that an equipartition field spans at least one decade in radius in the disk. Indeed, in such circumstances, there is no physical reason for strong gradients in jets and one may expect an almost plane Alfvén surface (Krasnopolsky et al. 1999; Casse & Keppens 2004). This kind of

jets display dynamical properties (acceleration and collimation) that weakly depend on the radial (inner and outer) boundary conditions, as in self-similar models. On the contrary, if the flux is small and concentrated at the inner edge of the disk, one would expect an almost spherical expansion of the field lines as in X-wind models (Shu et al. 1994). Observations allowing to infer jet velocity patterns and to relate them to the source (Garcia et al. 2001; Bacciotti et al. 2002; Pesenti et al. 2003) are necessary to discriminate between these two extreme pictures.

F.C. is a postdoctoral fellowship of the European Community's Human Potential Programme PLATON under contract HPRN-CT-2000-00153. F.C. would also like to thank the team SHERPAS for its hospitality during his stay at the LAOG.

## REFERENCES

- Bacciotti, F., Ray, T.P., Mundt, R. et al. 2002, *ApJ*, 576, 222
- Casse, F., Ferreira, J. 2000a, *A&A*, 353, 1115
- Casse, F., Ferreira, J. 2000b, *A&A*, 361, 1178
- Casse, F., Keppens, R. 2004, *ApJ*, (astro-ph/0310322)
- Falcke, H., Biermann, L. 1996, *A&A*, 308, 321
- Chan, K.L., Henriksen, R.N. 1980, *ApJ*, 241, 534
- Ferreira, J., Pelletier, G. 1995, *A&A*, 295, 807
- Ferreira, J. 1997, *A&A*, 319, 340
- Ferreira, J., Pelletier, G., Appl, S. 2000, *MNRAS*, 312, 387
- Ferro-Fontán, C., Gómez de Castro, A.I. 2003, *MNRAS*, 342, 427
- Galeev, A.A., Rosner, R., Vaiana, G.S. 1979, *ApJ*, 229, 318
- Gallo, E., Fender, R. P., Pooley, G. G. 2003, *MNRAS*, 344, 60
- Garcia, P.J.V., Cabrit, S., Ferreira, J., Binette, L. 2001, *A&A*, 377, 609
- Gómez de Castro, A.I., Verdugo, E. 2001, *ApJ*, 548, 976

- Hartigan, P., Edwards, S., Ghandour, L. 1995, *ApJ*, 452, 736
- Heyvaerts, J., Priest, E.R. 1989, *A&A*, 216, 230
- Krasnopolsky, R., Li, Z.Y., Blandford, R. 1999, *ApJ*, 526, 631
- Kwan, J. 1997, *ApJ*, 489, 284
- Livio, M. 1997, *IAU Colloq.* 163, D.T. Wickramasinghe, G.V. Bicknell & L. Ferrario (ASP Conf. Ser. 121), 845
- Matt, S., Goodson, A.P., Winglee, R.M. et al. 2002, *ApJ*, 574, 232
- Miller, K.A., Stone, J.M. 2000, *ApJ*, 534, 398
- Pesenti, N., Dougados, C., Cabrit, S., O'Brien, D., Garcia, P., Ferreira, J. 2003, *A&A*, 410, 155
- Raga, A.C., Velázquez, P.F., Cantó, J. et al. 2002, *A&A*, 395, 647
- Renaud, N., Henri, G. 1998, *MNRAS*, 300, 1047
- Romanova, M.M., Ustyugova, G.V., Koldoba, A.V., Lovelace, R.V.E 2002, *ApJ*, 578, 420
- Serjeant S., Rawlings, S., Lacy, M. et al. 1998, *MNRAS*, 294, 494
- Shu, F., Najita, J., Ostriker, E. et al. 1994, *ApJ*, 429, 781
- Takami, M., Chrysostomou, A., Bailey, J. et al. 2002, *ApJ*, 568, L53
- Tsinganos, K., Sauty, C., Surlantzis, G., Trussoni, E., Contopoulos, J. 1996, *MNRAS*, 283, 811
- Ustyugova, G.V., Koldoba, A.V., Romanova, M.M., Chetchetkin, V.M., Lovelace, R.V.E. 1999, *ApJ*, 516, 221
- Vlahakis, N., Tsinganos, K., Sauty, C., Trussoni, E. 2000, *MNRAS*, 318, 417

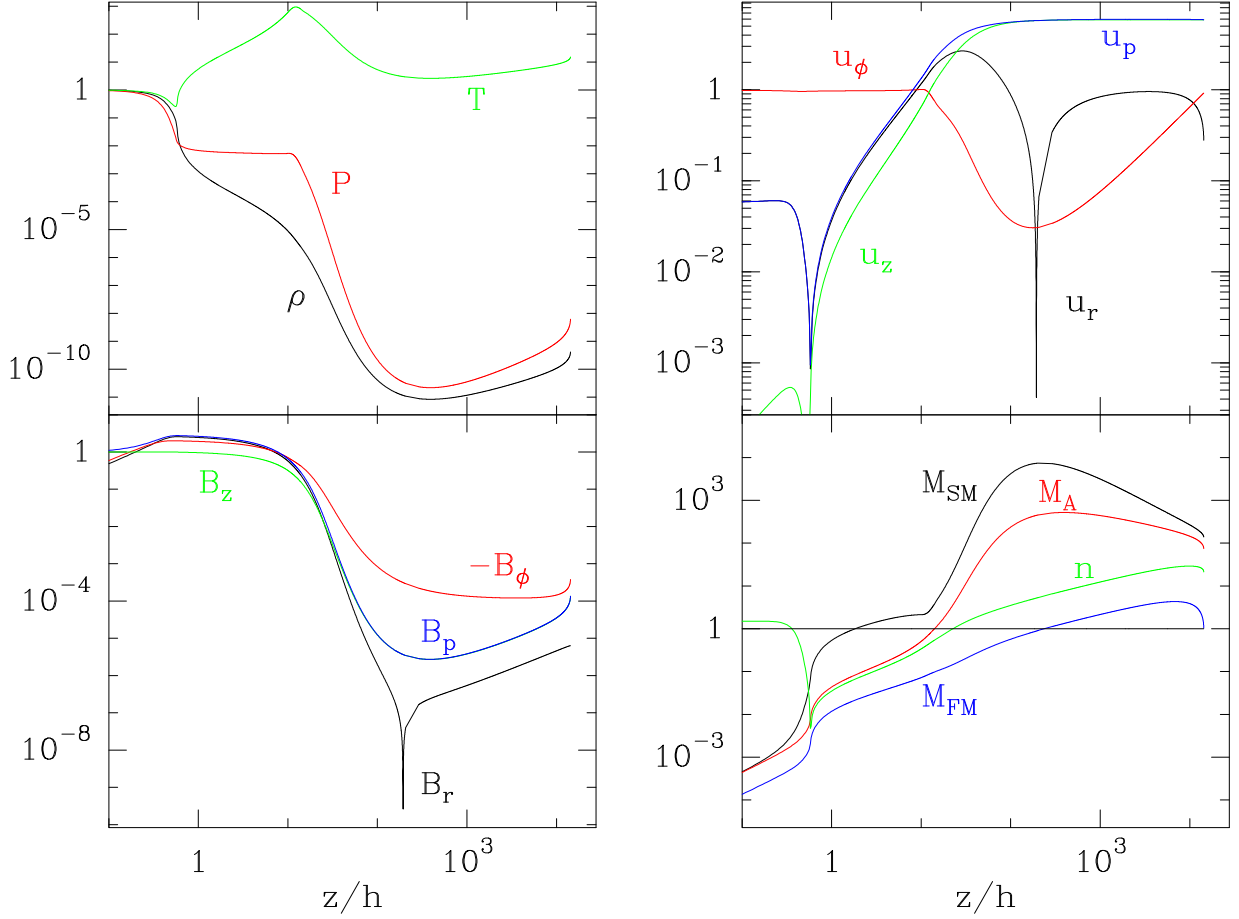


Fig. 2.— Typical super-FM disk wind with  $\xi = 0.03, \epsilon = 0.03$  ( $h = \epsilon r$ ). Density, pressure and temperature are normalized to their value at the disk midplane, the magnetic field components to  $B_z(z = 0)$  and the velocities to the Keplerian speed at the anchoring radius  $r_o$ . All magnetic field components remain comparable from the disk surface to the Alfvén point. Note that the density profile inside the disk, where both  $u_r$  and  $u_z$  are negative, is very different from a gaussian. Recollimation takes place at  $z \simeq 3 \cdot 10^3 r_o$ .

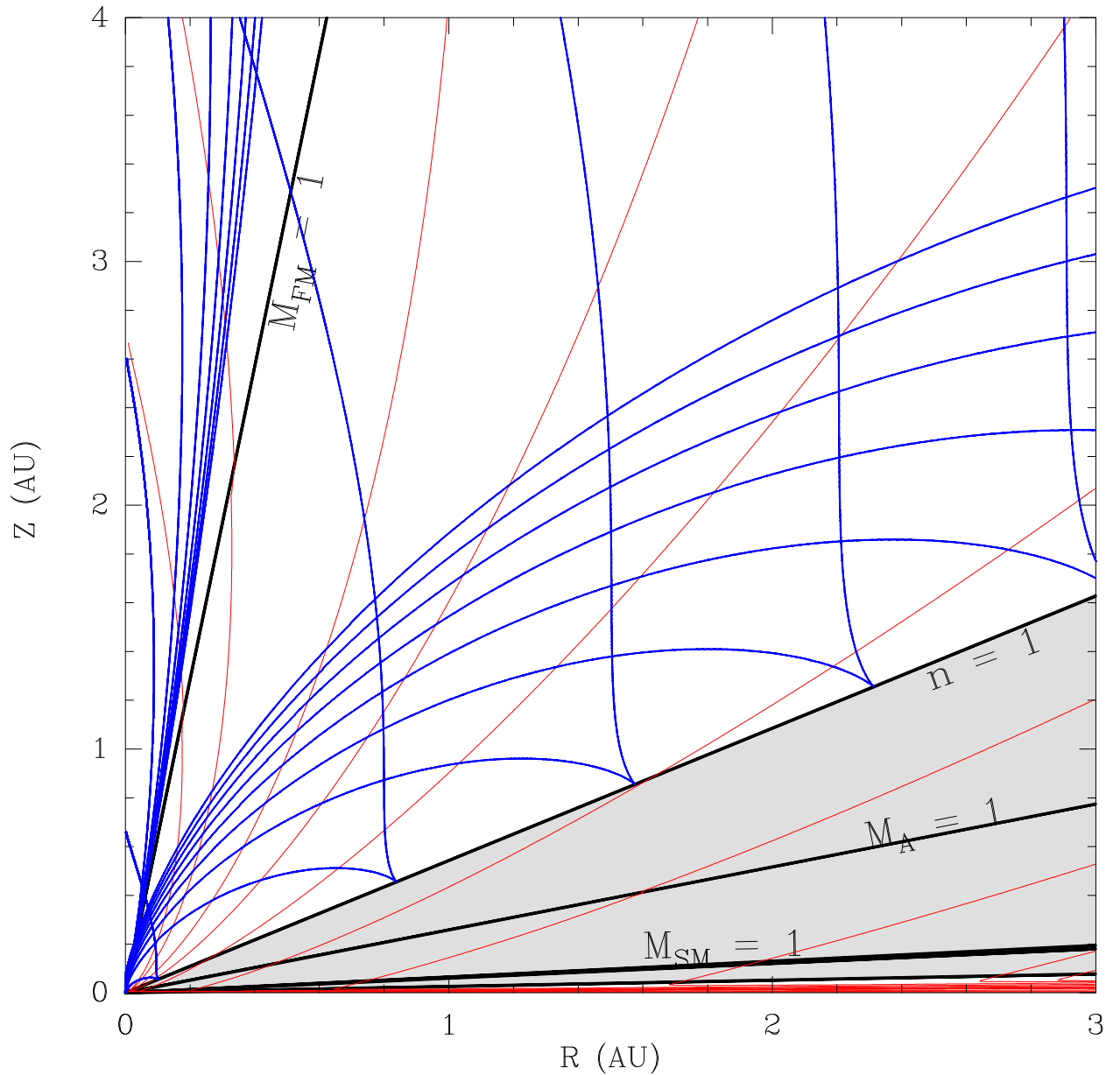


Fig. 3.— Poloidal cross section showing the three critical surfaces (SM, A and FM), some characteristics (blue lines, in the hyperbolic domain) as well as the two elliptic regions (shaded). Contrary to Vlahakis et al. (2000), the streamlines (red lines) are computed from the midplane of the resistive accretion disk. This solution has  $\xi = 0.09, \epsilon = 0.03$  and  $\Gamma_c = 1.56$ .